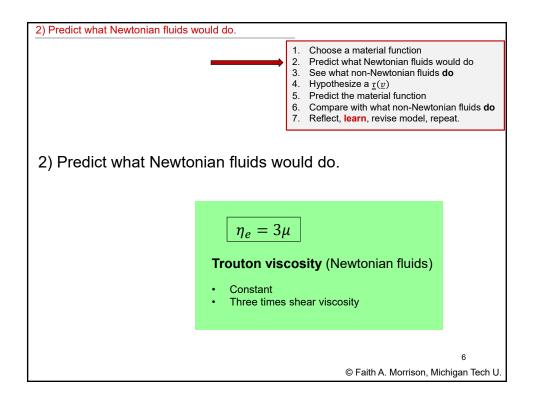
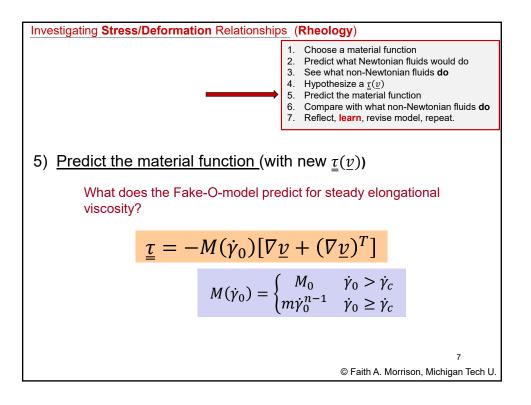
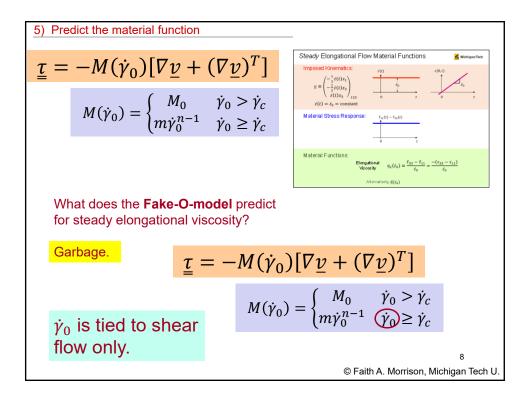
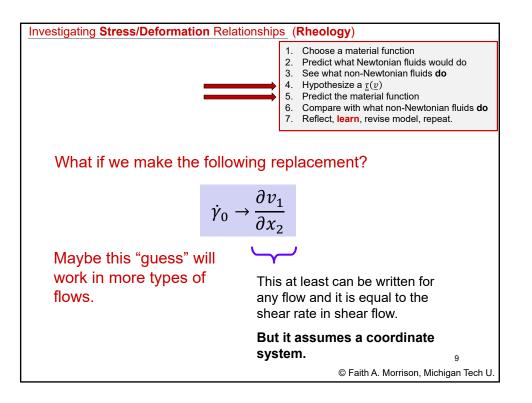


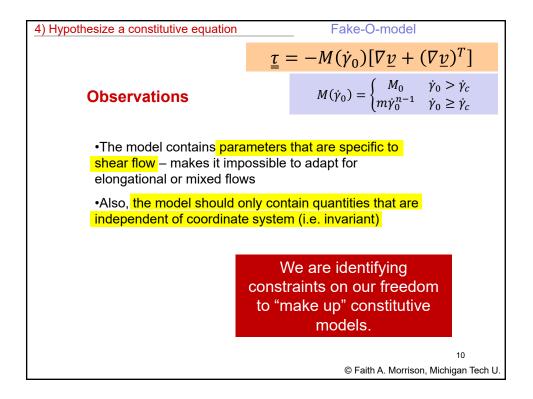
2) Predict what Newtonian fluids would do.				
		 Choose a material function Predict what Newtonian fluids would do See what non-Newtonian fluids do Hypothesize a <u>t</u>(<u>v</u>) Predict the material function Compare with what non-Newtonian fluids do Reflect, learn, revise model, repeat. 		
2) Predict what Newtonian fluids would do.				
		Steady Elongational Flow Material Functions		
	?	Imposed Kinematics: $g \equiv \begin{pmatrix} -\frac{1}{2} \ell(3x_1) \\ -\frac{1}{2} \ell(3x_2) \\ \frac{1}{4} \ell(3x_2) \\ \frac{1}{4} \ell(3x_2) \\ 0 \\ \frac{1}{4} \ell(3x_2) \\ 0 \\ \frac{1}{4} \ell(3x_2) \\ 0 \\ \frac{1}{4} \ell(3x_2) \\ \frac{1}{$		
	$\underline{\underline{\tau}} = -\mu \underline{\dot{Y}}$	Material Stress Response:		
		Material Functions: Elengational Vecourly $\eta_r(\ell_0) = \frac{\ell_{13} - \ell_{11}}{\ell_0} = \frac{-(\tau_{13} - \tau_{11})}{\ell_0}$		
		5		
		© Faith A. Morrison, Michigan Tech U.		

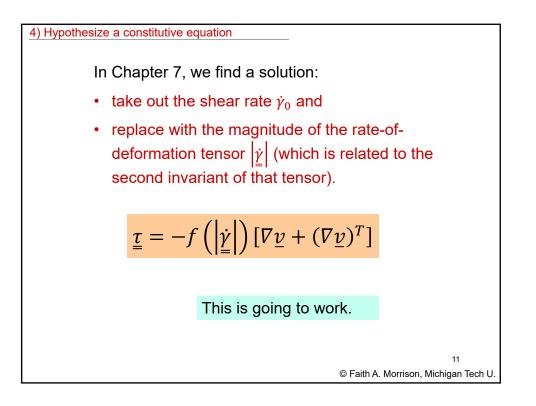


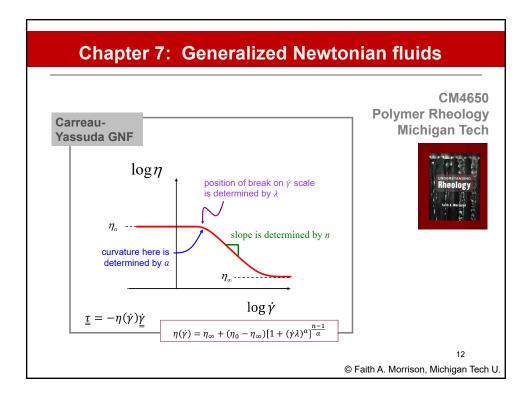


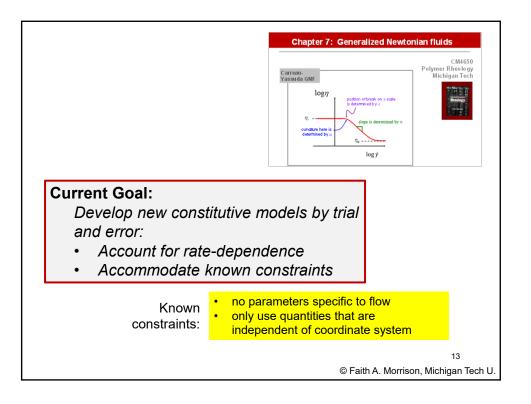


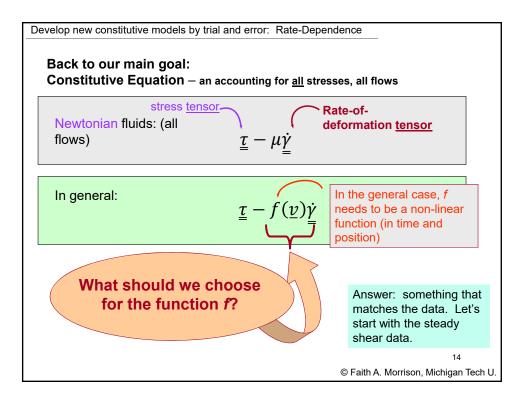


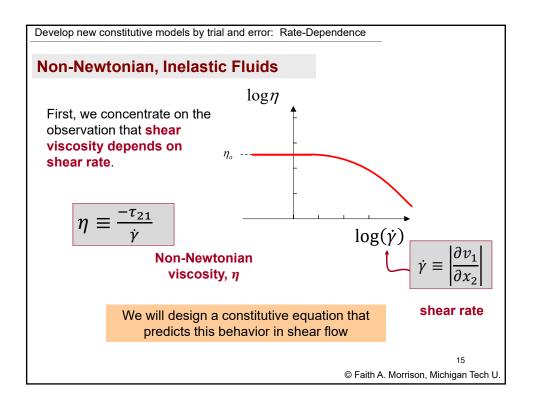


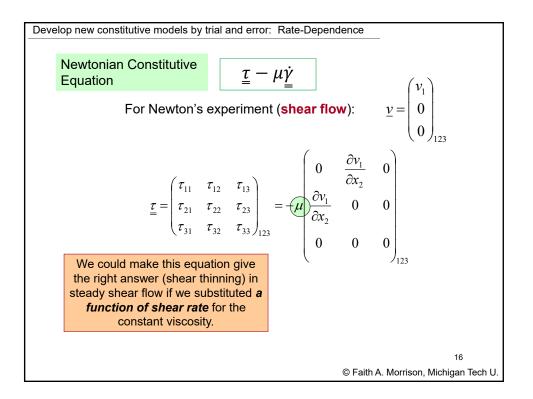


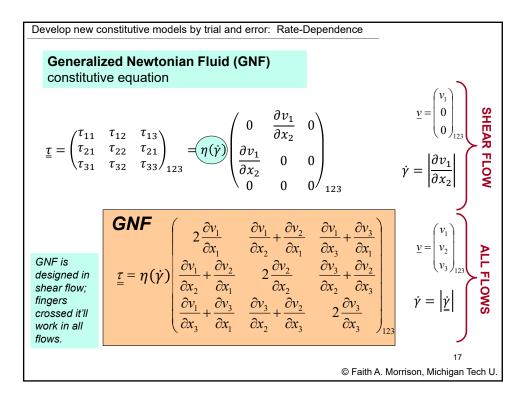


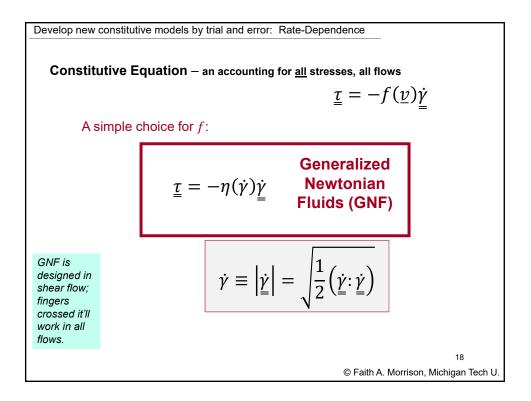


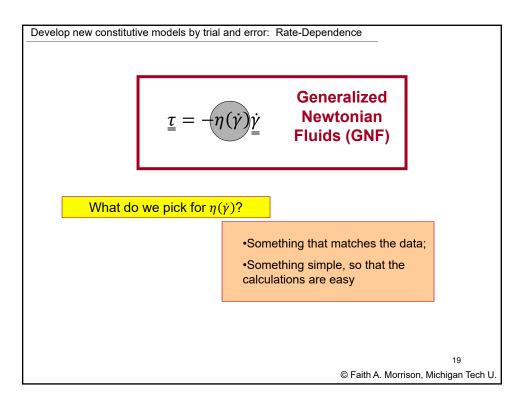


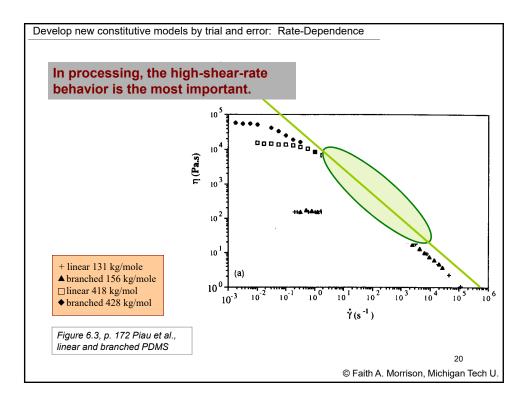


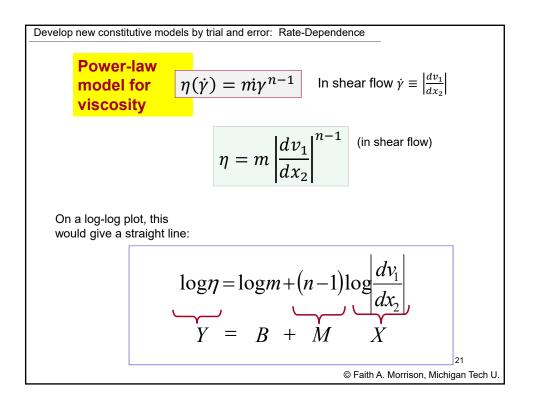


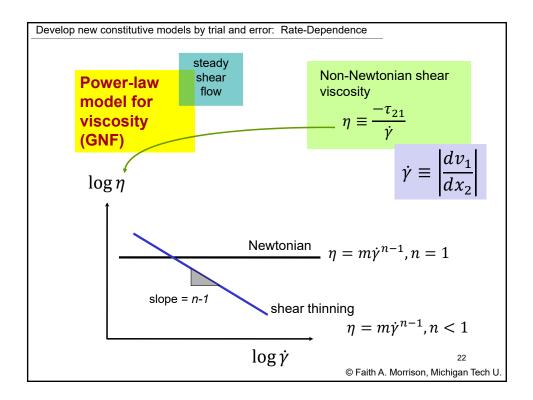


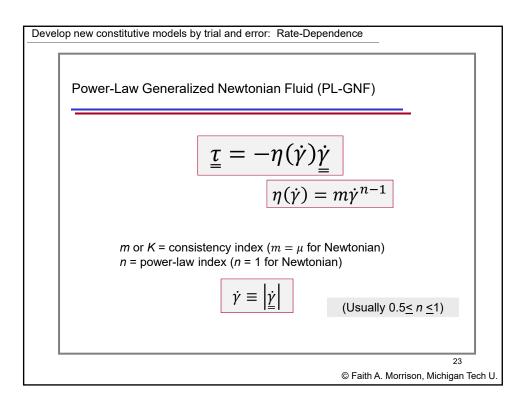


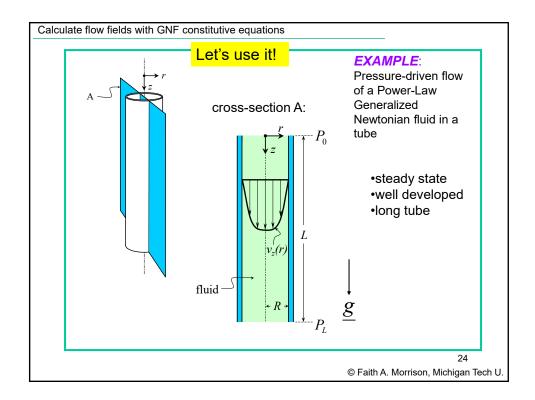


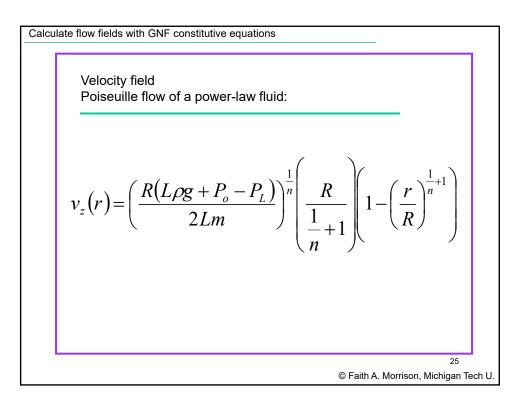


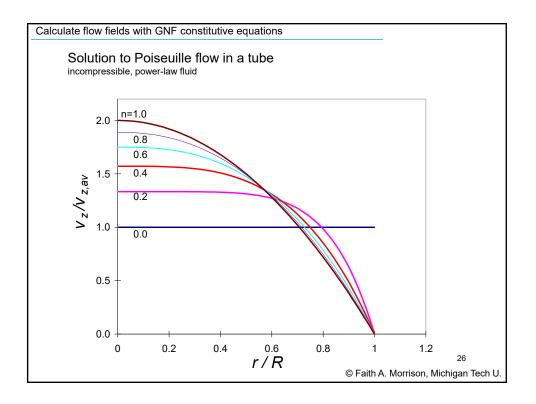


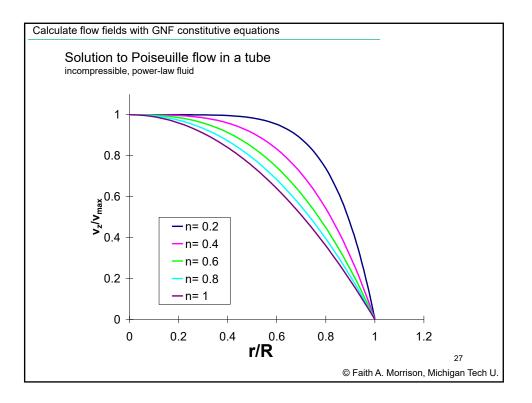


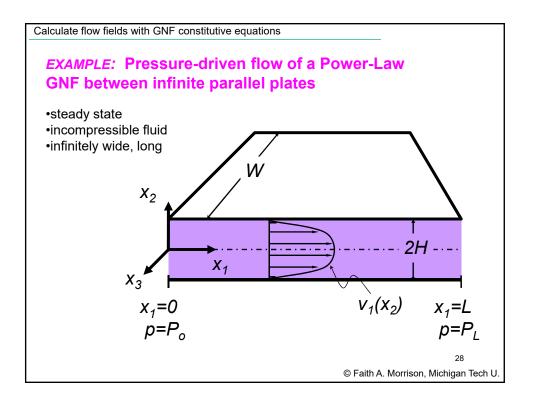


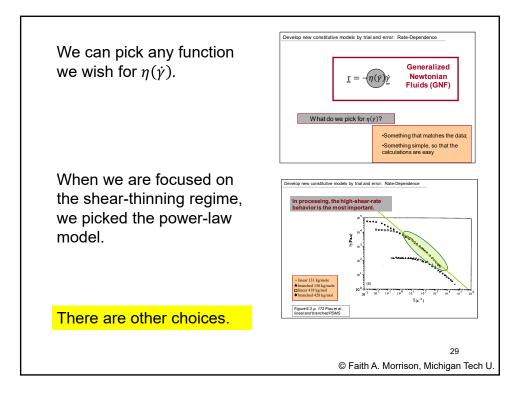


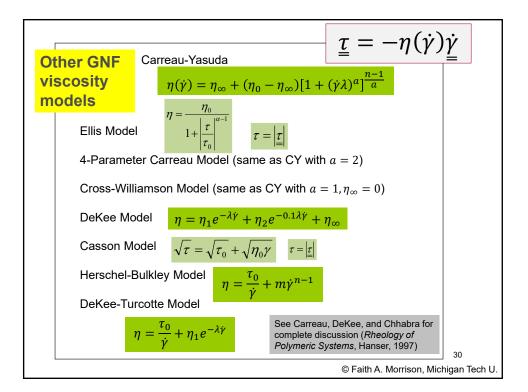


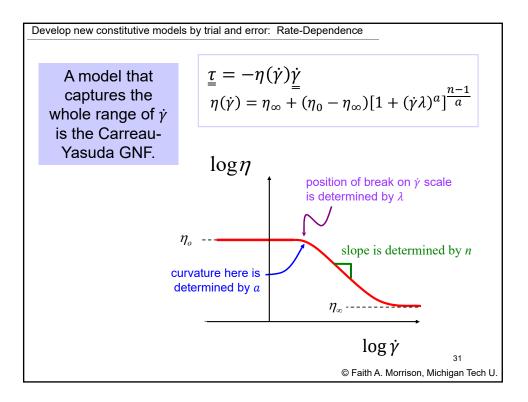


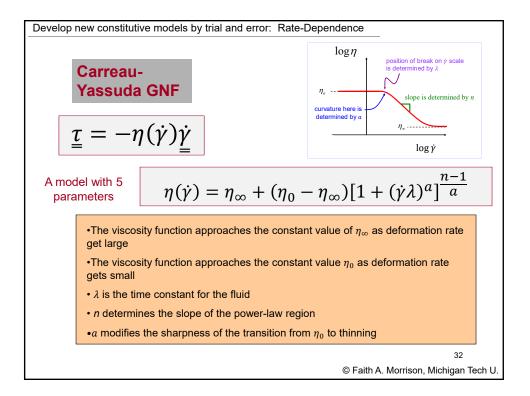


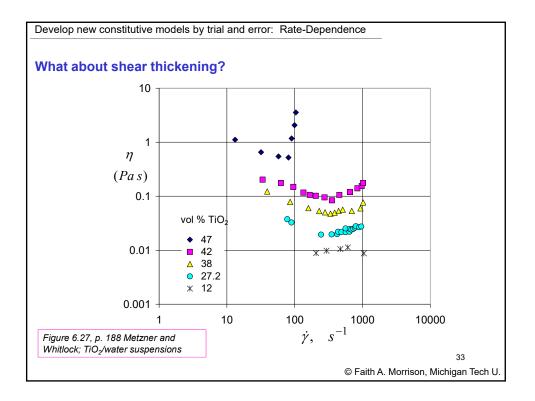


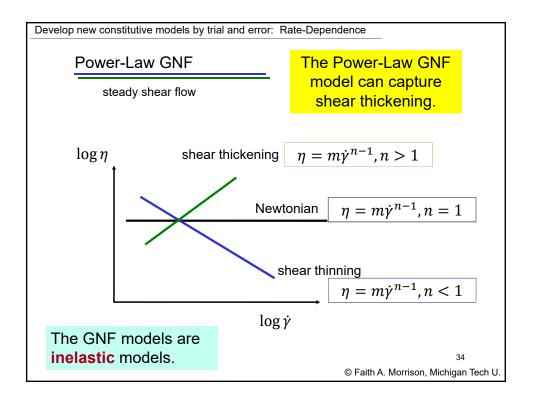


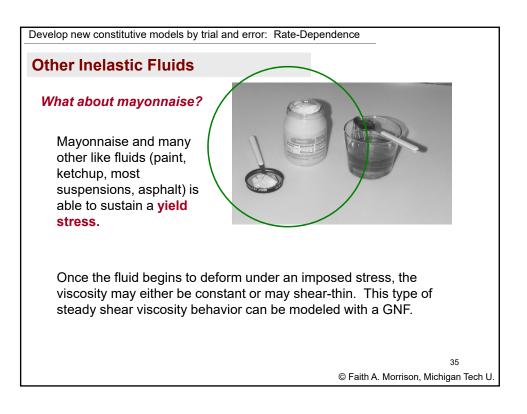


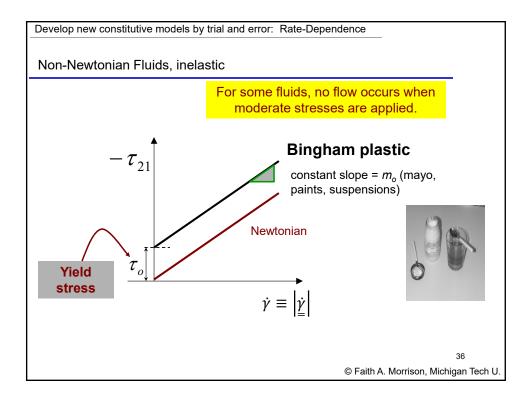


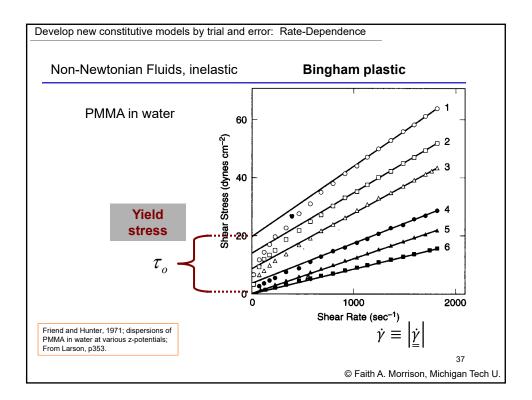


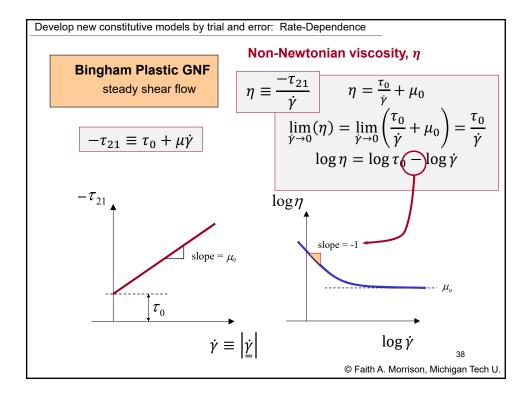


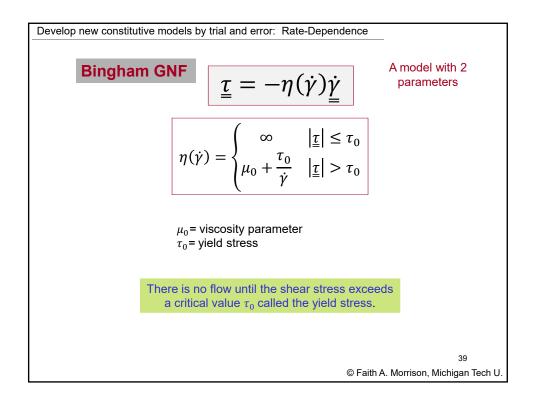


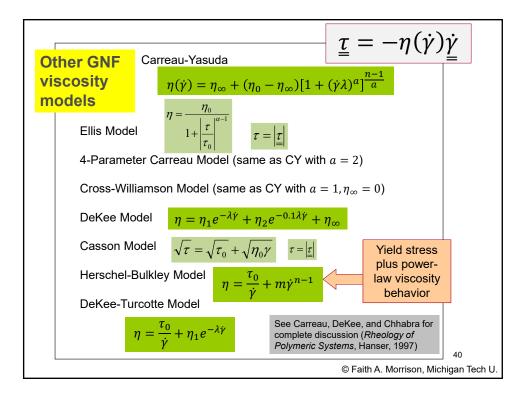


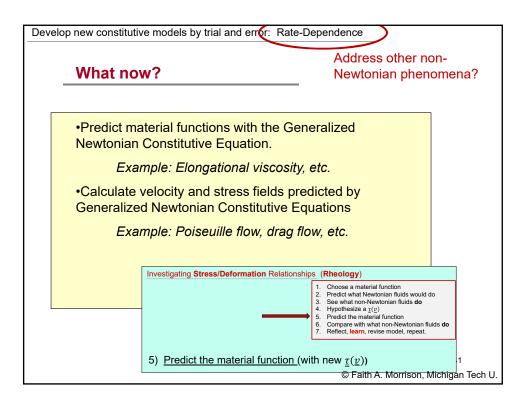


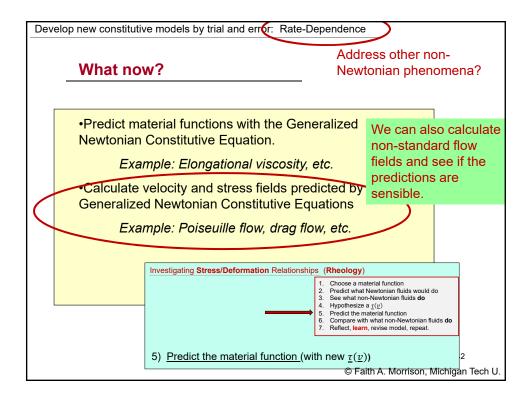


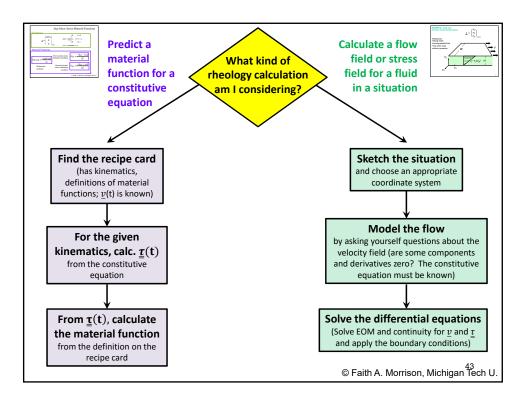


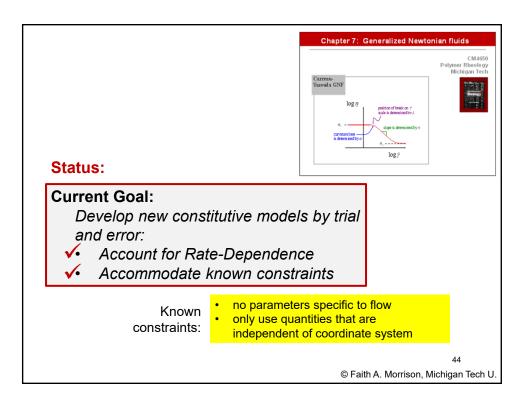


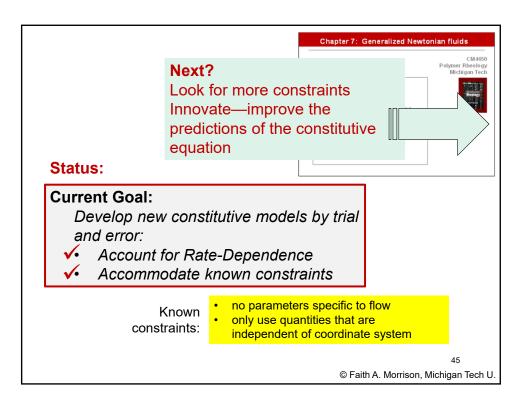


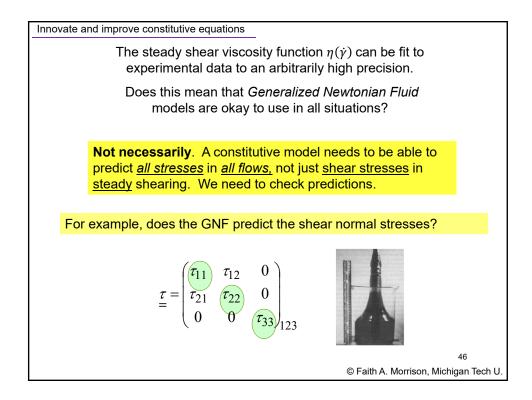


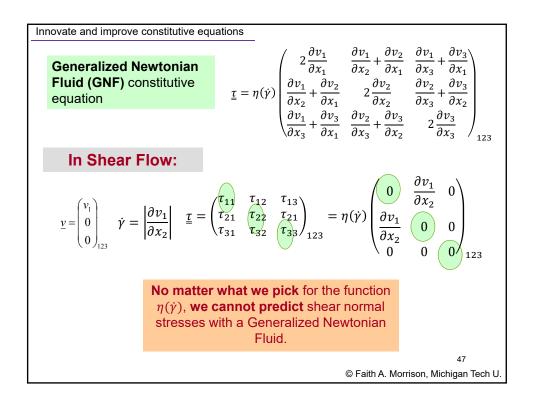


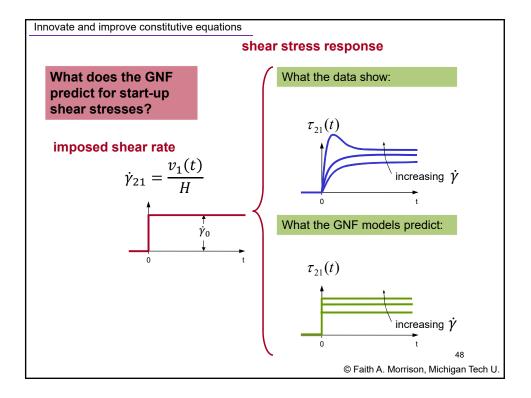


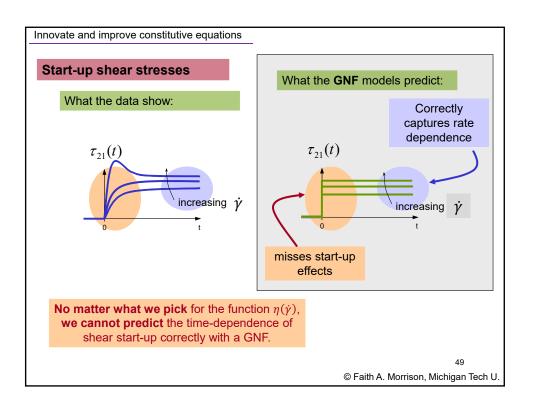


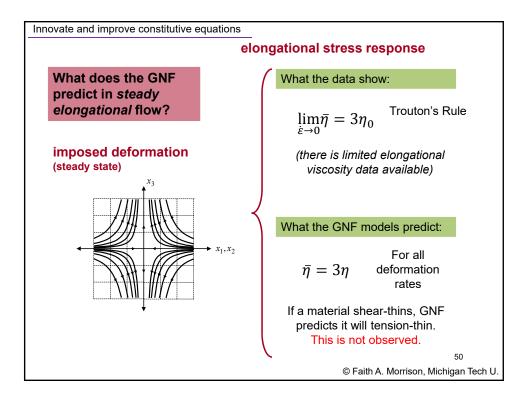




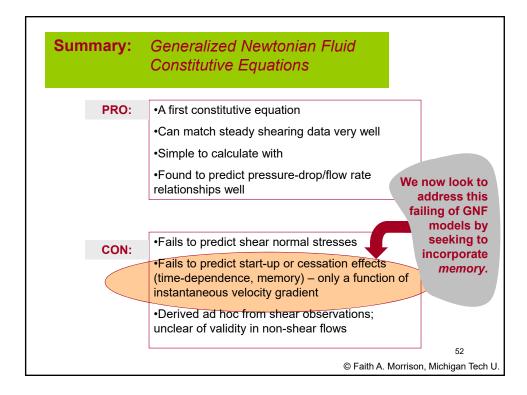








Summary:	Generalized Newtonian Fluid Constitutive Equations	
PRO:	•A first constitutive equation	
	•Can match steady shearing data very well	
	•Simple to calculate with	
	•Found to predict pressure-drop/flow rate relationships well	
CON:	•Fails to predict shear normal stresses	
	•Fails to predict start-up or cessation effects (time-dependence, memory) – only a function of instantaneous velocity gradient	
	•Derived ad hoc from shear observations; unclear of validity in non-shear flows	
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Innovate and improve constitutive equations			
What we know so far			
Rules for Constitutive Equations			
$\underline{\underline{\tau}}(t) = f\left(\underline{\underline{\dot{\gamma}}}, I_{\underline{\dot{\gamma}}}, III_{\underline{\dot{\gamma}}}, III_{\underline{\dot{\gamma}}}, \text{material info}\right)$			
The stress expression:			
•Must be of tensor order			
•Must be a tensor (independent of coordinate system)			
•Must be a symmetric tensor			
•Must make predictions that are independent of the observer			
•Should correctly predict observed flow/deformation behavior			
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