| | CM465 |
|--|--------------|
| Steady Shear Flow Material Functions | Michigan Teo |
| Imposed Kinematics: $\underline{v} \equiv \begin{pmatrix} \hat{\gamma}(t) x_2 \\ 0 \\ 0 \\ 1z_3 \\ \hat{\gamma}(t) = \dot{\gamma}_0 = \text{constant} \end{pmatrix}$ $\vec{\gamma}_{21}(0, t)$ $\vec{\gamma}_{0}$ $\vec{\gamma}_{0$ | Rheology |
| Material Stress Response: $\vec{r}_{21}(t)$ \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{0} \vec{T}_{10} | |
| $ \begin{array}{ll} \text{Material Functions:} & \text{First normal-stress} \\ \text{coefficient} & \Psi_1(\dot{\gamma}_0) \equiv \frac{\tilde{\tau}_{11} - \tilde{\tau}_{22}}{\dot{\gamma}_0^2} = \frac{-(\tau_{11} - \tau_{22})}{\dot{\gamma}_0^2} \\ \text{Viscosity} & \eta(\dot{\gamma}_0) \equiv \frac{\tilde{\tau}_{21}}{\dot{\gamma}_0} = \frac{-\tau_{21}}{\dot{\gamma}_0} & \text{Second normal-stress coefficient} \\ \Psi_2(\dot{\gamma}_0) \equiv \frac{\tilde{\tau}_{22} - \tilde{\tau}_{33}}{\dot{\gamma}_0^2} = \frac{-(\tau_{22} - \tau_{23})}{\dot{\gamma}_0^2} \\ \end{array} $ | |

| Chapter 5: Material Functions | 5 | | |
|--|---|--|--|
| Shearly Shear Flow Material Functions $regressed Internations r = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 &$ | CM4650 Polymer Rheology Michigan Tech | | |
| | What are | | |
| m | material functions, | | |
| ar | and why do we need | | |
| | them? | | |
| | 2 © Caith A. Marriana, Miching, Tach III | | |
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| 2) Predict what Newtonian fluids would do. | | | |
|--|--|--|--|
| | Choose a material function Predict what Newtonian fluids would do See what non-Newtonian fluids do Hypothesize a <u>r(v)</u> Predict the material function Compare with what non-Newtonian fluids do Reflect, learn, revise model, repeat. | | |
| 2) Predict what Newtonian fluids would do. | | | |
| | Step Strain Shear Flow Material Functions | | |
| ? | Imposed Kinematics: | | |
| | Material Stress Response: $t_{x,O} = \frac{1}{0} + \frac{1}{0} $ | | |
| | $ \begin{array}{ll} \mbox{Material Functions:} & \mbox{Pist normal-stress} \\ \mbox{Relaxation} & G(t,\gamma_0) \equiv \frac{t_{11}(t,\gamma_0)}{\gamma_0} = \frac{-t_{11}(t,\gamma_0)}{\gamma_0} \\ \mbox{modulus} & \mbox{Ge}_{V_1}(t,\gamma_0) \equiv \frac{t_{11}-t_{12}}{\gamma_0^2} \\ \mbox{Relaxation} & \mbox{Ge}_{V_1}(t,\gamma_0) \equiv \frac{t_{11}-t_{12}}{\gamma_0^2} \\ \mbox{Relaxation} & \mbox{Relaxation} & \mbox{Ge}_{V_1}(t,\gamma_0) \equiv \frac{t_{11}-t_{12}}{\gamma_0^2} \\ \mbox{Relaxation} & Rela$ | | |
| | | | |
| | 97 | | |
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| 2) Predict what Newtonian fluids would do. | | | | |
|--|-------------------|--|--|--|
| | | Choose a material function Predict what Newtonian fluids would do See what non-Newtonian fluids do Hypothesize a <u>t</u>(<u>v</u>) Predict the material function Compare with what non-Newtonian fluids do Reflect, learn, revise model, repeat. | | |
| 2) Predict what Newtonian fluids would do. | | | | |
| | | Step Strain Shear Flow Material Functions | | |
| | Answer: mostly | Imposed Kinematics: $ \begin{array}{c} U \equiv \begin{pmatrix} (1) \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0$ | | |
| | zero | Material Stress Response: ratio | | |
| | | $ \begin{array}{l} \mbox{Material Functions:} \\ \mbox{Relaxation} \\ \mbox{modulus} & \mathcal{C}(t,\gamma_0) \equiv \frac{t_{21}(t,\gamma_0)}{\gamma_0} = \frac{-t_{21}(t,\gamma_0)}{\gamma_0} \\ \end{array} \\ \begin{array}{l} \mbox{Relaxation} \\ $ | | |
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