Graphical Designs

Donald L. Kreher Michigan Technological University

September 10, 2010

Abstract

Given a graph Γ a collection of subgraphs $\mathscr B$ of Γ is said to be a Γ -Graphical t-design of index λ if

- 1. whenever $B \in \mathcal{B}$ and $\alpha \in \text{Aut } \Gamma$, then $\alpha(B) \in \mathcal{B}$;
- 2. every t-edge subgraph of Γ , is contained in exactly λ of the subgraphs in \mathscr{B} .

The Γ -graphical designs of index 1 with $\Gamma = K_n, K_{m,n}$ and $K_{\underbrace{n,n,n,\dots,n}_r}$ will be presented.