

Wednesday

21 APRIL 2021

MODULE 4 F. MORRISON  
CM3120



Michigan Tech

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## Requests for today?

2 Apr 21

16 Apr 21

Today

21 Apr 2021

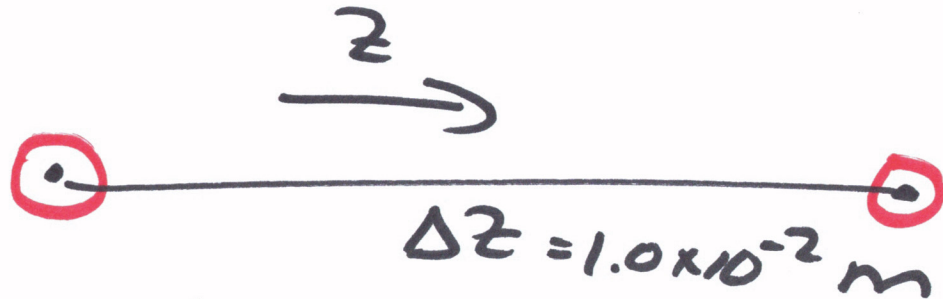
- ✓ . 4.3 (see also Example 5)
- ✓ . 4.7 (Module 4)
- ✓ . 4.8 (EMCD) (Lecture II)
- ✓ . 4.11 (devise Heissler chart)
- ✓ . 4.12
- ✓ . 4.16
- 4.4

4.8

WATER A  
AIR B

steady  
EMKD  
 $N_A = -N_B$   
 $T = 298\text{K}$

(3)



$$C_A = 0.0050 \frac{\text{kmol A}}{\text{m}^3}$$

$$C_B = 0.0360 \frac{\text{kmol B}}{\text{m}^3}$$

$$C_A = 0.0045 \frac{\text{kmol A}}{\text{m}^3}$$

$$C_B = 0.0365 \frac{\text{kmol B}}{\text{m}^3}$$

What is  $N_{Az}$  [=]  $\frac{\text{kmol}}{\text{m}^2 \text{s}}$

We know  $\frac{\Delta X_A}{\Delta z} \Rightarrow$  we can use Fick's Law (x part law) to obtain  $N_{Az}$  (3)

$$N_{Az} = X_A (N_{Az} + N_{Bz}) - C D_{AB} \frac{dX_A}{dz}$$

$\underbrace{\quad \quad \quad}_{=0 \text{ EMCD}}$

$$N_{Az} = -C D_{AB} \frac{dX_A}{dz} = -D_{AB} \frac{\Delta C_A}{\Delta z}$$

*Table 6.2-1 (p. 260)*  
 $= 0.260$

IDEAL GAS:

$$PV = nRT$$
$$\frac{n}{V} = \frac{P}{RT}$$

4.11

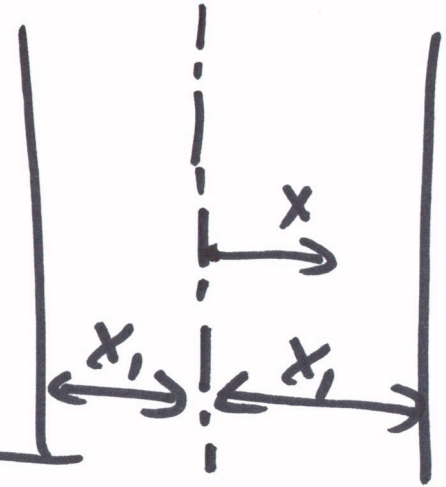
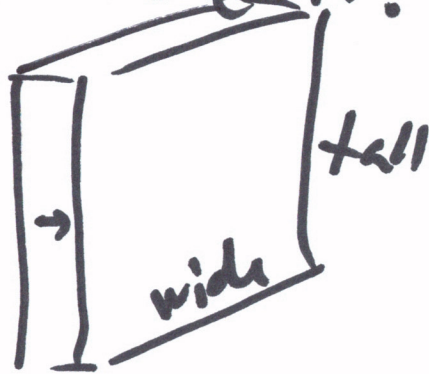
4

What mass x fn  
problem looks like  
a Heissler (heat-x fn)  
problem?

Initially

*sponge  
wet*

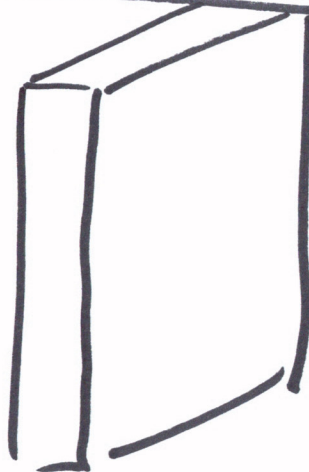
$$W_A = W_{A0} \\ \forall x \quad t < 0$$



Suddenly

submerged  
in an environment

$$W_{A_b}$$



*sponge  
drying*

4.12

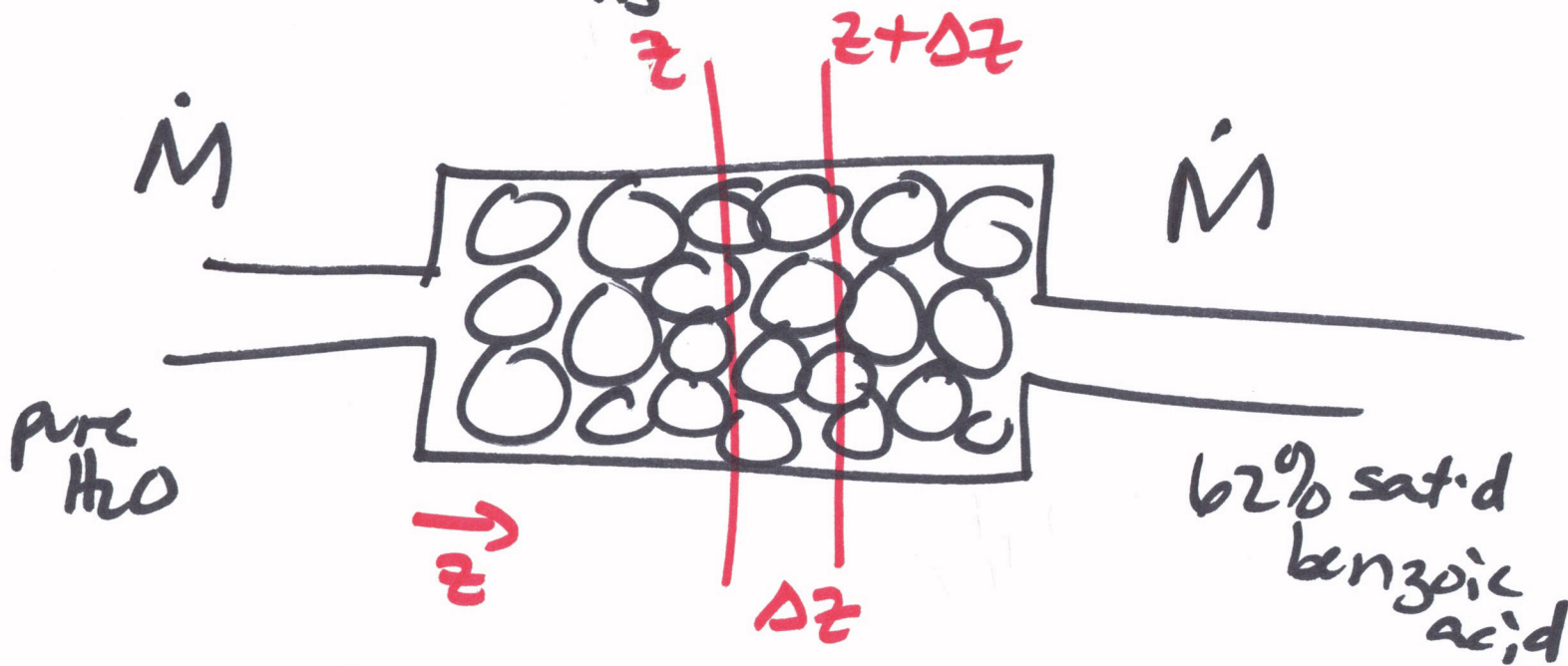
(5)

$$a = 23 \frac{\text{cm}^2}{\text{cm}^3}$$

volumetric  
flow rate  
of liquid

superficial  
velocity

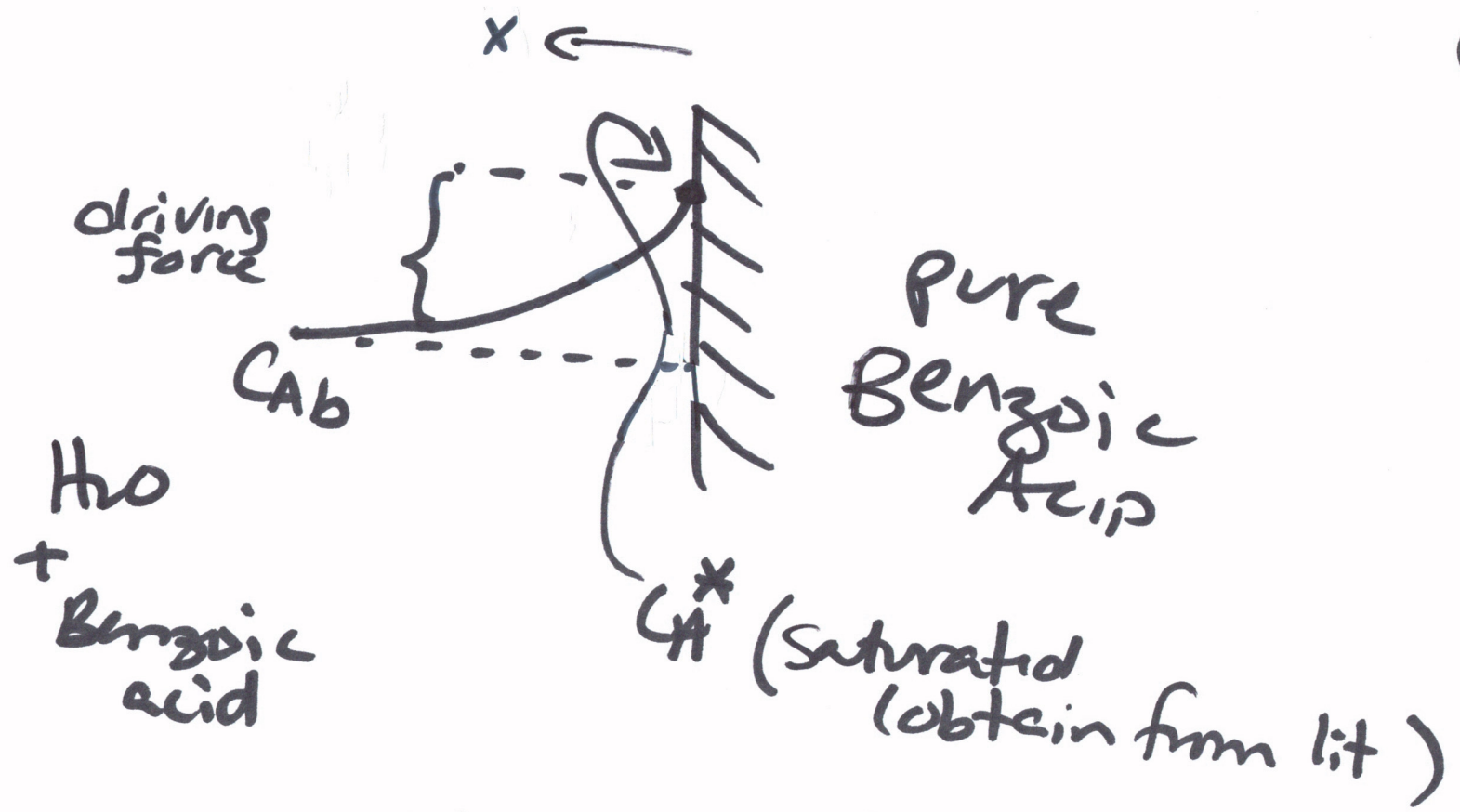
$$v^0 = 5.0 \frac{\text{cm}}{\text{s}} = \frac{\dot{V}}{A_{xs}}$$



C.V.:  $A_{xs} \Delta z$

$A_{xs}$  = cross section  
of bed

6



$$N_{A_x} = k_c (C_A^* - C_{Ab})$$

# Unsteady Macroscopic Species A Mass Balance

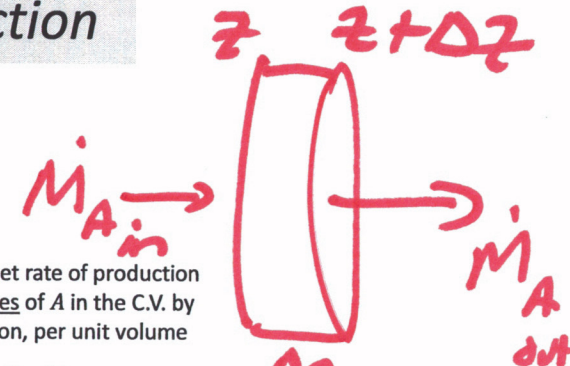
accumulation = net flow in + production + introduction

$$\frac{d}{dt} (\mathcal{M}_{A,sys}) = -\Delta \dot{\mathcal{M}}_A + R_A V_{sys} - \sum_j (N_A S)_j$$

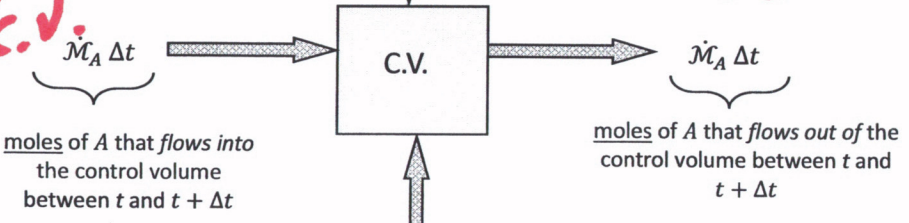
pseudo steady state

no rxn in C.V.

MOLES



$R_A$  = net rate of production of moles of A in the C.V. by reaction, per unit volume



introduction of moles of A into the C.V. by mass transfer across the  $j^{th}$  bounding control surface  $S_j$  (C.S.)

$\mathcal{M}_{A,sys} = c_A V_{sys}$  = total moles of A in the C.V.

$\Delta \dot{\mathcal{M}}_A = \sum_{j,outs} \dot{\mathcal{M}}_{A,j} - \sum_{j,ins} \dot{\mathcal{M}}_{A,j}$  = bulk out

$R_A$  = net rate of production of moles of A in the C.V. by reaction, per unit volume

$V_{sys}$  = system volume

$N_{A_j} = K \Delta c_{df}$  = molar flux of A out through the  $j^{th}$  C.S.

$S_{sys} = \sum_j S_j$   
 $\Delta$  is "out" - "in"  
 C.S. = control surface  
 C.V. = control volume

$N_A = k_c (C_A^* - C_A)$   
 $S = a A_{xs} \Delta z$

Ⓔ

$$0 = \left( \cancel{v^0 A_{xs}} \left. \frac{C_A}{z+\Delta z} \right|_{z+\Delta z} - \cancel{v^0 A_{xs}} \left. \frac{C_A}{z} \right|_z \right) + k_c a \cancel{A_{xs}} \Delta z (C_A^* - C_A)$$

$$\lim_{\Delta z \rightarrow 0} \frac{C_A|_{z+\Delta z} - C_A|_z}{\Delta z} = \frac{k_c a}{v^0} (C_A^* - C_A)$$

$$\frac{dC_A}{dz} = \frac{k_c a}{v^0} (C_A^* - C_A)$$

$$(-1) \int_0^{C_{A_L}} \frac{-dC_A}{C_A^* - C_A} = \int_0^L \frac{k_c a}{v^0} dz$$

assume  $k_c = \text{const}$

- $C_{A_L} = 0.62 C_A^*$
- integrate
- solve for  $k_c$

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