

What CM Unit Ops  
have unsteady heat xfer

1. start up rxr  
(shut down) dist column  
eva p  
boiler
2. furnaces - hot spots
3. Unsteady
  - step change
  - programmed, time-dependent  
operation

# Unsteady Heat Xfer

Section B  
⑬

- mixing materials w/ different temp
- reaction (exothermic)
- distillation  
start up  
shut down

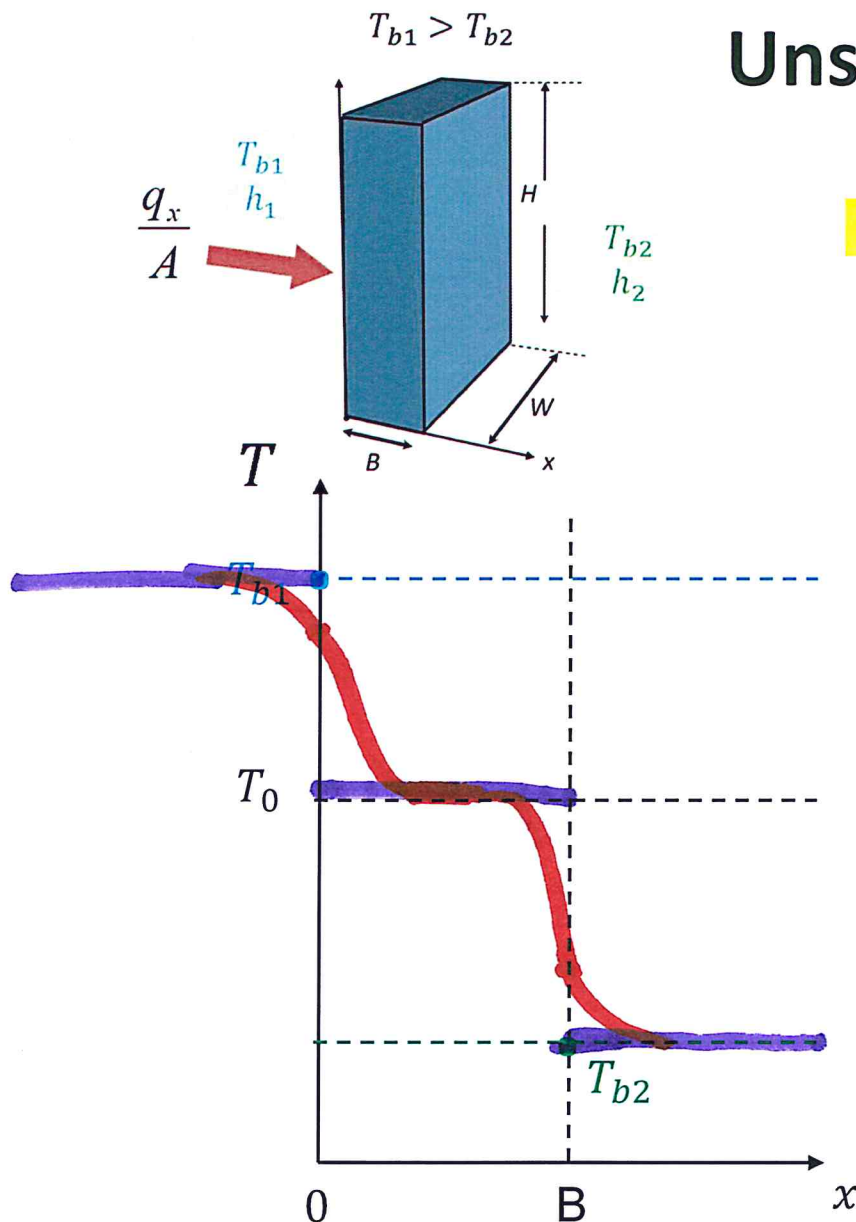
$$\frac{q_x}{A} = -k \frac{dT}{dx}$$

- digester (rxr)
- evaporator - (boiler)



## Unsteady Heat Transfer

Example: A wide, tall slab initially uniformly at  $T_0$  is suddenly subjected to flowing fluid on its two broad faces. The left fluid is at  $T_{b1}$  and its heat transfer to the wall is characterized by heat transfer coefficient  $h_1$ , while the right side is at  $T_{b2}$  and characterized by  $h_2$ . What is the temperature distribution across the slab as a function of time?



### What do we think will happen?

- Will there be heat transfer resistance at the boundaries?
- Will there be a linear temperature profile in the slab?
- Femtoseconds after the change, what does the profile look like?
- What will the solution trend towards as time goes on ( $\rightarrow \infty$ )?

Heat Transfer: Steady vs. Unsteady

$h_i$  are large

$T$

$T_{b1}$

$T_{b1}$

$\Rightarrow \frac{1}{h}$  (resistance) is small

$\Rightarrow T_b = T_w$   
forall time "for all time"

$T_0$

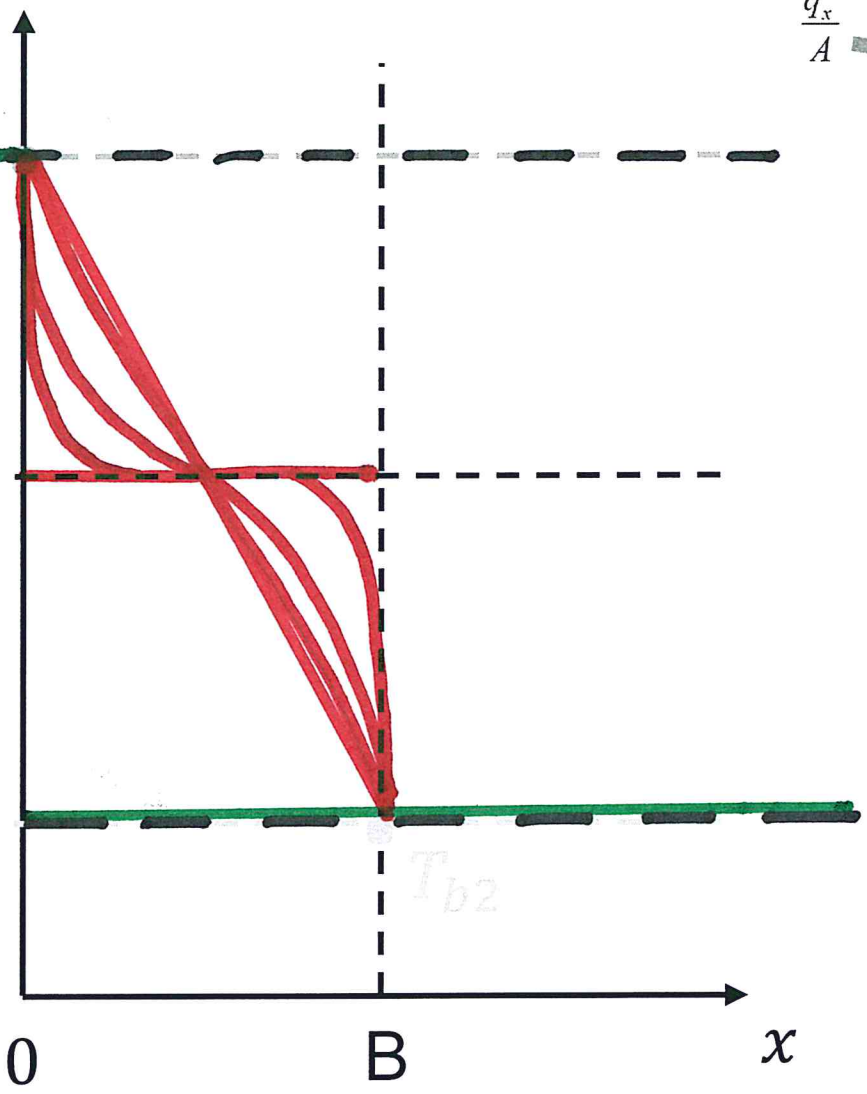
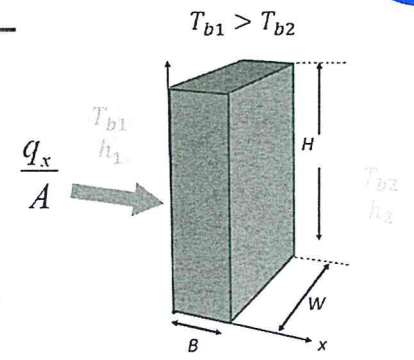
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B

$x$

$T_{b2}$

$T_{b2}$



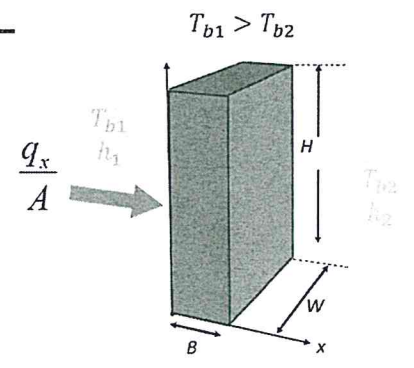
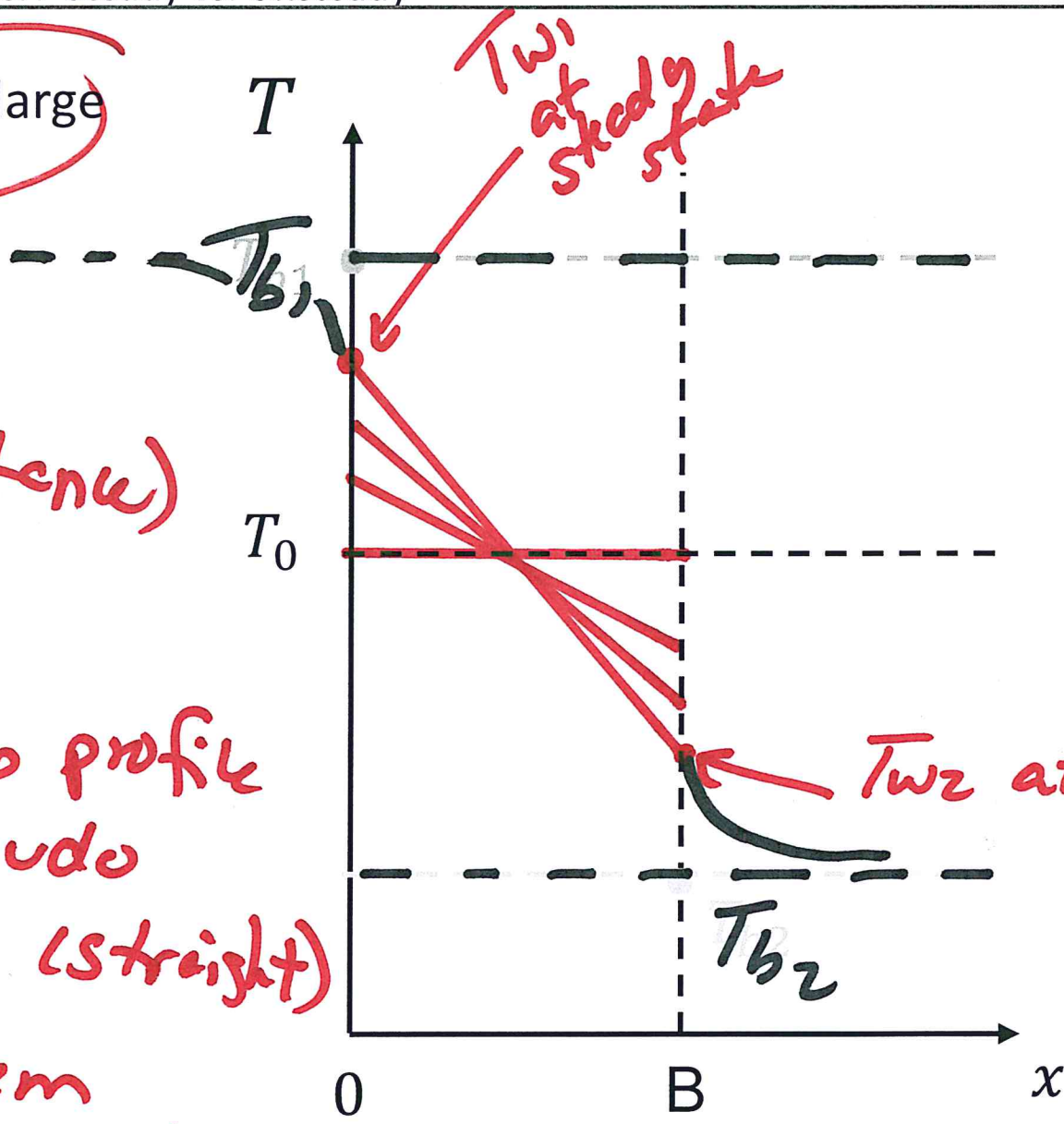
Heat Transfer: Steady vs. Unsteady

$k$  is large

$\Rightarrow \frac{B}{k}$  (resistance) is small

$\Rightarrow$  temp profile is "pseudo steady" (straight)

As system approaches steady state





# Heat Transfer: Steady vs. Unsteady

- Neither slab conduction nor fluid convection dominates

both  
resistances  
 $\frac{B}{k}$ ,  $\frac{1}{h}$  affect  
time evolution  
of  $T(x)$

