## How to Add 95% Confidence Interval Error Bars in Excel 2010

Faith A. Morrison (fmorriso@mtu.edu)
Department of Chemical Engineering
Michigan Technological University

21 Feb 2012; modified 25 Feb 2013; modified 15Jan2014

This is a brief document with one method of adding 95% confidence interval error bars to plots produced in Excel 2010. Without special measures, Microsoft Excel will not add error bars with the meaning of a 95% confidence interval. Please send your feedback on these instructions and I will improve them. I would like to thank Ross Koepke for showing me how to do this.

The data used in this example are shown in Table 1. Varying numbers of replicates viscosity of a 20wt% aqueous sugar solution were taken using Cannon-Fenske viscometers. From the raw data we calculate the mean value of the viscosity samples (Excel function AVERAGE), the standard deviation of the sample s (STDEV.S), the number of replicates n (COUNT), and the standard error of the sample (s/Vn). We use the Students T distribution to calculate  $t_{0.025}$ , the number of standard errors on either side of the mean that we must include in order to construct a 95% confidence interval (TINV(2\*0.025,n-1)). The interval of viscosity around the mean that encloses the 95% confidence interval is  $t_{0.025}$  multiplied by the standard error (see Table 1).

To display the 95% confidence intervals in error bars using Excel, we proceed as follows. A plot of viscosity versus concentration is constructed using a Scatter plot (Figure 1). After producing the plot,

- 1. Click on the *Chart Area* of your graph and select the *Layout Tab*, *Error Bars*, and *More Error Bars Options*.
- 2. Under Vertical Error Bars, choose Custom, Specify Value.
- 3. For both *Positive Error Value* and *Negative Error Value*, select the range in the spreadsheet that contains the increment that corresponds to the 95% Student's T confidence interval.
- 4. Excel produces both vertical and horizontal error bars by default. To delete the horizontal error bars, click on the *Chart Area*, and in *Selection Field* (upper left corner), select the chart element x-error bars and then delete.

In the final step above we used the *Selection Field*. The *Selection Field* can be found in the upper-left corner of Excel when you have the *Layout tab* selected under *Chart Tools*. The *Selection Field* makes it easy to select (or delete) a chart element that may be otherwise difficult to select with the mouse.

<u>Warning</u>: There is a bug in Excel 2010 that is mentioned on some websites. If you create a fresh graph with custom error bars, you should have no problems. If you then copy that graph, intending to modify the error bars in a new graph, there is a bug that keeps the cell reference to the original error bars. I found no way to override this. On the web they say you can delete the error bars and then re-apply them, but that did not fix it for me. I conclude that it is not safe to copy a graph with custom error bars.

Table 1: Data and analysis of viscosity replicates of aqueous sugar solutions at  $20^{\circ}$ C; there are errors in the concentration values at high concentration.

| t <sub>0.025</sub> | increment (students's T<br>95%) | standard errof of sample | std dev of the sample | n  | wt% sugar | average viscosity (cp) | viscosity ( | cp) 20oC (. | approximat | e)       |         |         |         |         |        |          |        |        |        |
|--------------------|---------------------------------|--------------------------|-----------------------|----|-----------|------------------------|-------------|-------------|------------|----------|---------|---------|---------|---------|--------|----------|--------|--------|--------|
| 2.45               | 0.14                            | 0.055                    | 0.15                  | 7  | 10        | 1.27                   | 0.936       | 1.3067      | 1.31365    | 1.314    | 1.3266  | 1.32994 | 1.337   |         |        |          |        |        |        |
| 2.26               | 0.09                            | 0.038                    | 0.12                  | 10 | 20        | 1.89                   | 1.656       | 1.725935    | 1.793      | 1.906    | 1.913   | 1.958   | 1.9644  | 1.97    | 1.9784 | 2.017991 |        |        |        |
| 2.20               | 0.12                            | 0.053                    | 0.18                  | 12 | 30        | 3.49                   | 3.2872      | 3.34        | 3.355      | 3.39     | 3.409   | 3.409   | 3.46    | 3.503   | 3.5411 | 3.55     | 3.803  | 3.885  |        |
| 2.26               | 0.45                            | 0.199                    | 0.63                  | 10 | 40        | 7.86                   | 6.697       | 6.897       | 7.5415     | 7.945486 | 8.069   | 8.11    | 8.167   | 8.189   | 8.264  | 8.69     |        |        |        |
| 2.57               | 0.42                            | 0.165                    | 0.40                  | 6  | 45        | 10.23                  | 9.79        | 9.819       | 10.173     | 10.2     | 10.63   | 10.767  |         |         |        |          |        |        |        |
| 2.18               | 3.97                            | 1.823                    | 6.57                  | 13 | 50        | 19.46                  | 9.367       | 9.75        | 13.025     | 19.56    | 19.786  | 20.2    | 20.3    | 20.5    | 20.8   | 20.817   | 20.927 | 22.208 | 35.739 |
| 2.36               | 6.39                            | 2.701                    | 7.64                  | 8  | 60        | 80.53                  | 63.247      | 79.383      | 80.11      | 81.48    | 81.8631 | 84.3174 | 84.7742 | 89.1    |        |          |        |        |        |
| 2.36               | 9.06                            | 3.830                    | 10.83                 | 8  | 65        | 212.09                 | 197         | 203.42      | 205.5319   | 211.731  | 212.24  | 215.3   | 218.9   | 232.558 |        |          |        |        |        |

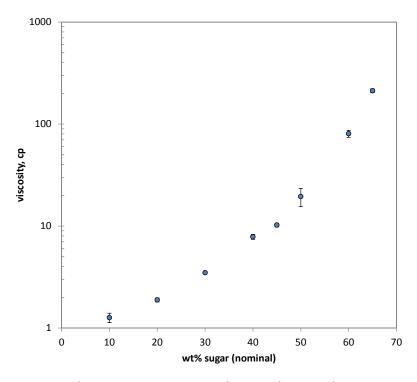


Figure 1: Student viscosity data on aqueous sugar solutions; there are known errors in the values of the concentration for the higher concentrations. Error bars indicate the 95% confidence intervals based on the Students T distribution.