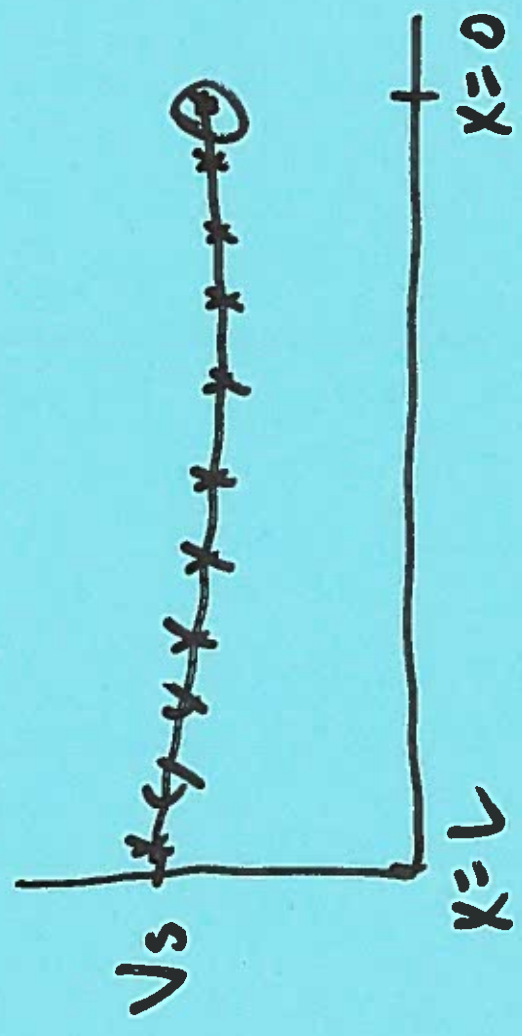
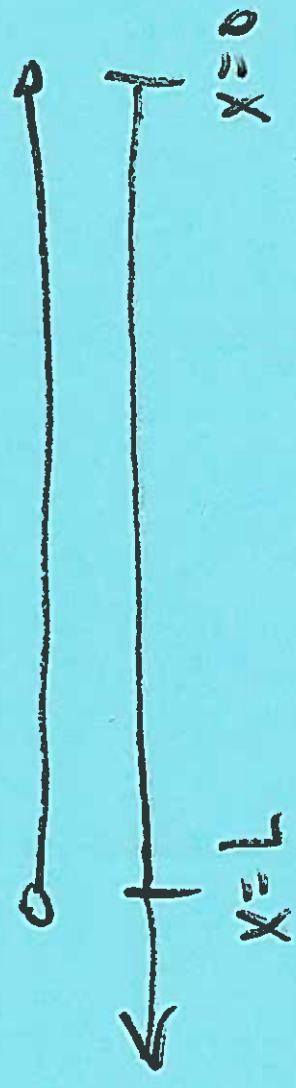


Topics for Today:

- Announcements
 - Detailed term project outlines (i.e. [Table of Contents](#) + List of references
 - ASPEN software - remote.mtu.edu
 - Office hrs: EERC 123, WF 4-6pm. Instructor's office: EERC 614
 - Recommended problems & all solutions: Ch.7 solns posted.
- Chapter 7 - Network Equations, Admittance Approaches
 - How's your linear algebra? Time to make use of it...
 - Basic strategy for building up [Y] for whole network
 - Quick recap of xfmrs and lines.
 - Generators
 - Example of building [Y] for 4-bus system.
 - Network Reduction (Kron Reduction)
 - Solution of matrix equations (system of linear equations)
 - Upcoming homework - intro to Matlab, matrices, equations.

- Spreadsheet
 - ASPEN
 - L^F
 - SC
 - ~~Phasor~~ Arc Flash
 - Relay Coordination
 - CYME - Optimal LF
- ATP
 - Line Constants
 - Time-domain
- Feedback control
 - Relay Prot
 - Matlab
 - Simulink
 - SimPower



Close look at $\gamma = \alpha + j\beta$

3

$$\gamma = \sqrt{Zy} = \sqrt{(0.2 + j0.6) \text{ } \Omega/\text{mi} * j7.3 \text{ } \mu\text{S}/\text{mi}}$$

Very high ωR

\Rightarrow may assume lossless?

$$= 0.0034 / \text{mi} + j0.00212 \text{ rad}/\text{mi}$$

$$= 0.0034 \frac{\text{neper}}{\text{mi}} + j0.00212 \text{ rad}/\text{mi}$$

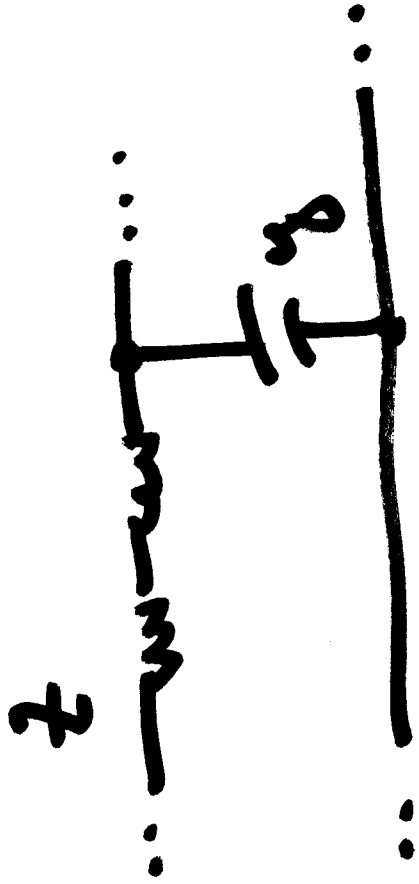
Tells us how much attenuation/mi the wave will experience.

$$\text{For } 250 \text{ mi: Atten} = (0.0034 \frac{\text{neper}}{\text{mi}})(250 \text{ mi}) = 0.85 \text{ or } 8.5\%$$

$$Z_c = \sqrt{\frac{Z}{y}} \Rightarrow \text{Real for lossless.}$$

$$\sim \frac{300 \Omega}{(250 - 400 \Omega)}$$

$$\sim 70 - 86 \Omega \text{ (cables)}$$



$$Z_c = \sqrt{\frac{R + j\omega L}{j\omega C}}$$



Reflections

2

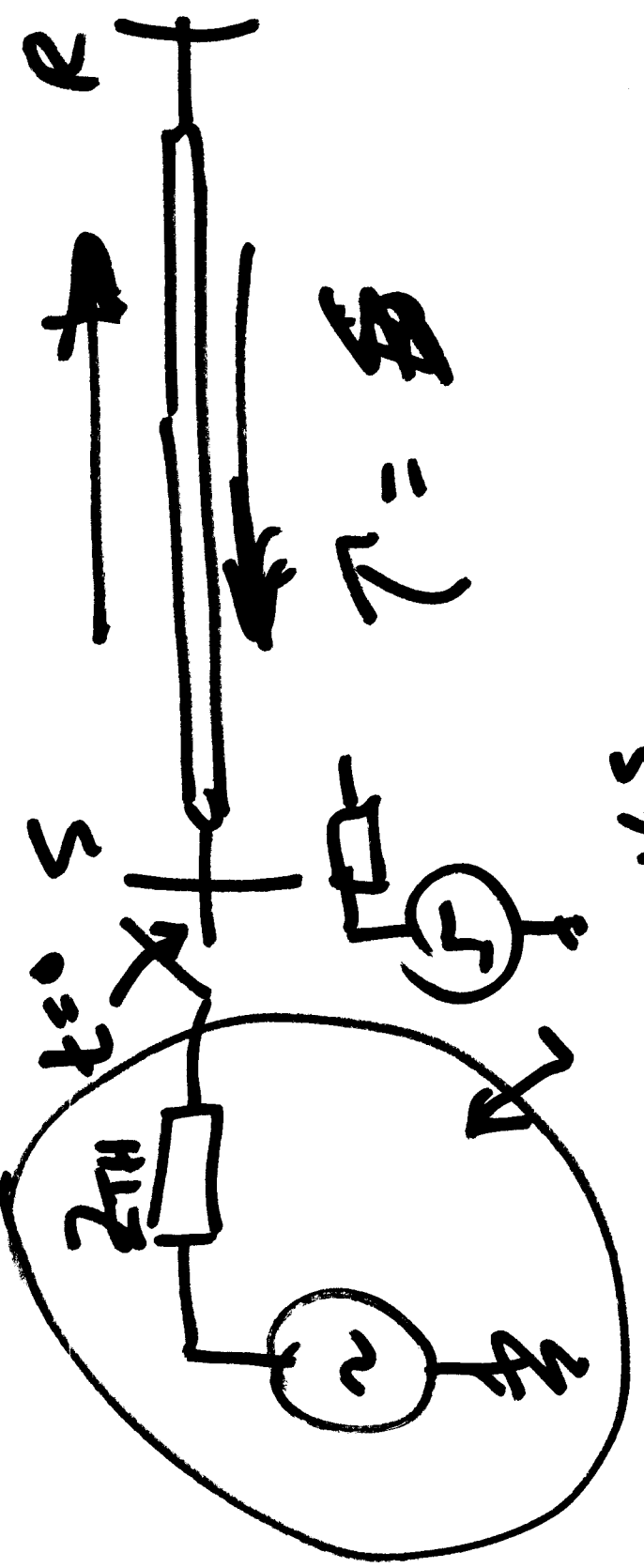
Voltage Reflection Coefficient:

$$\frac{V_R^-}{V_R^+} = \frac{Z_R - Z_C}{Z_R + Z_C} = \rho_s$$

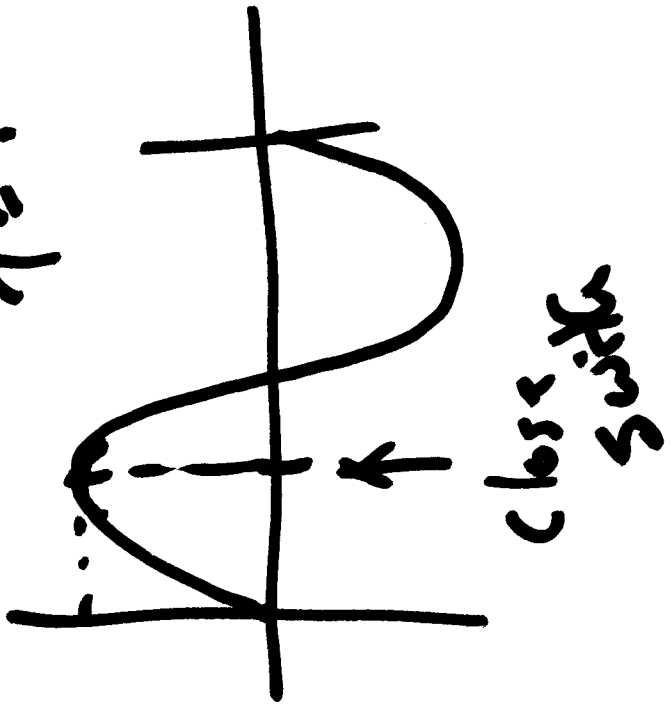
Current Reflection Coefficient

$$\frac{i_R^-}{i_R^+} = -\frac{V_R^-}{V_R^+} = -\rho_s$$

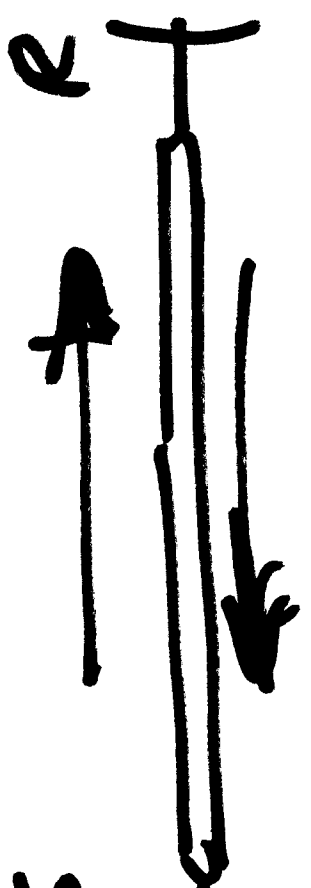




$\tau = 0.165$

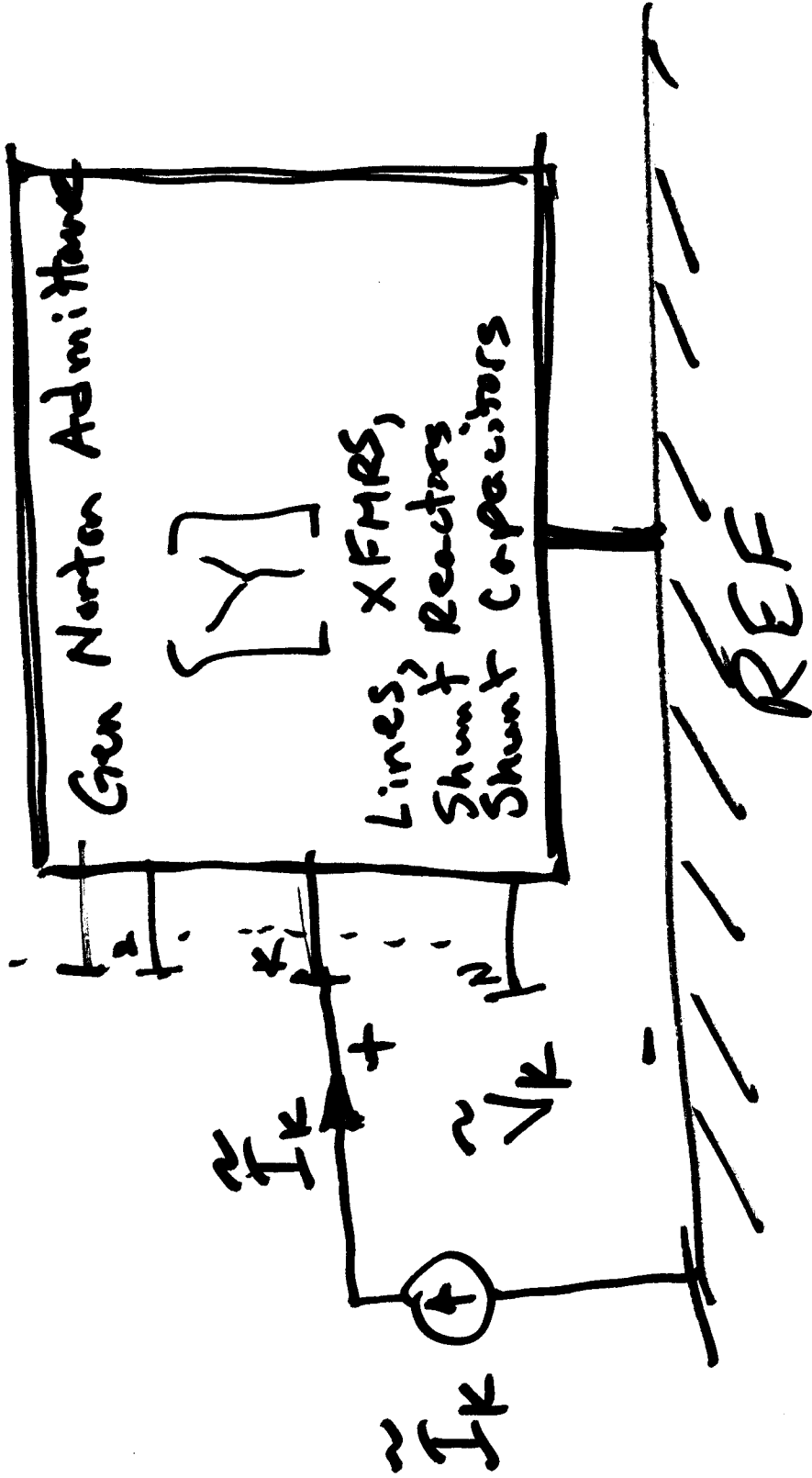


$\tau = 0.165$

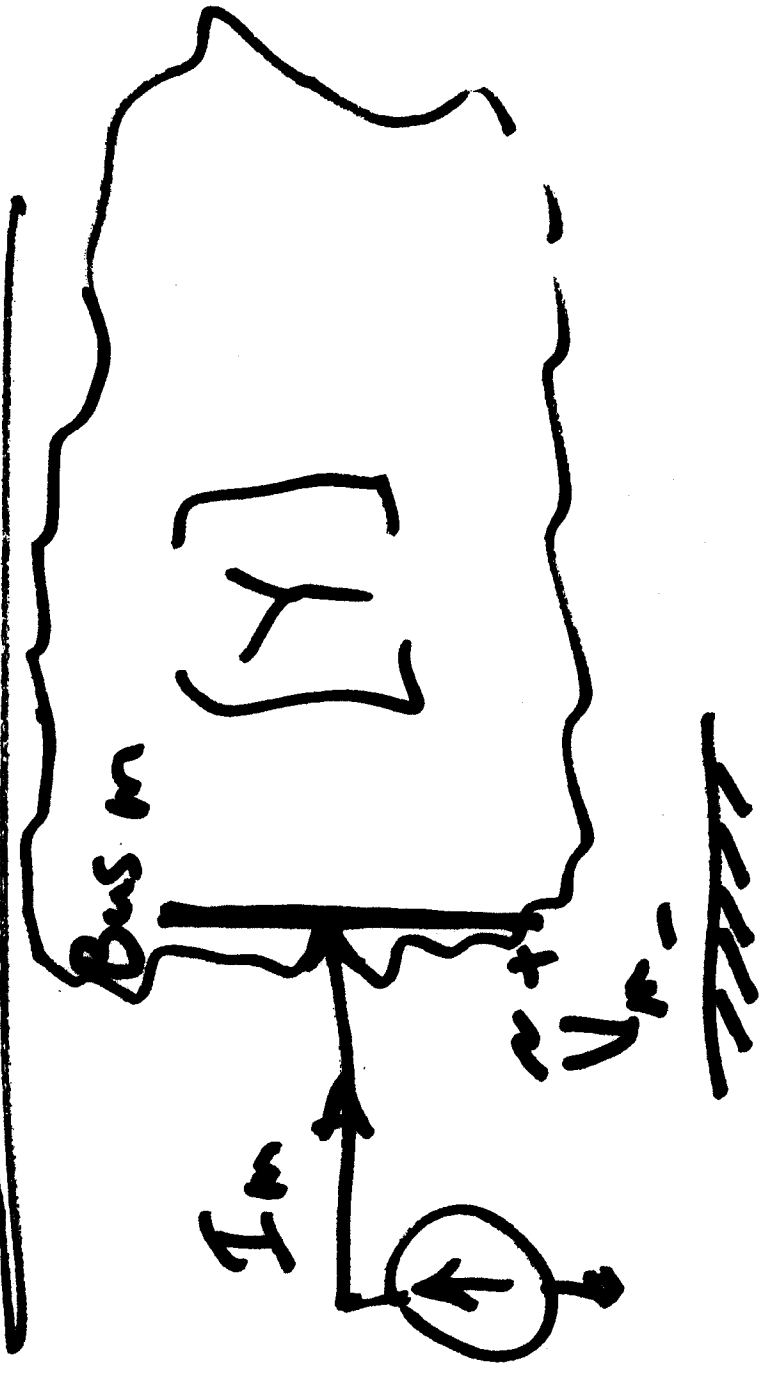


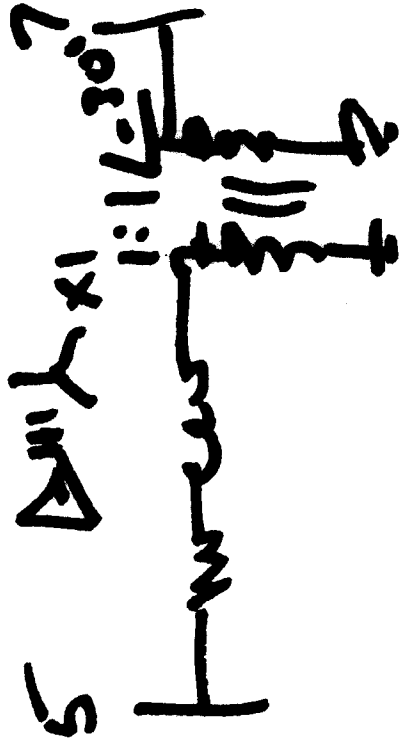
Basic Idea:

Per-Phase A-N

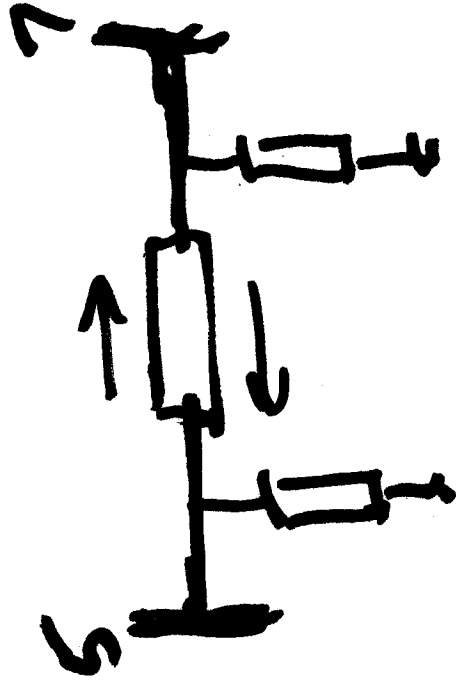


$$[Y][V] = [I_{inj}]$$



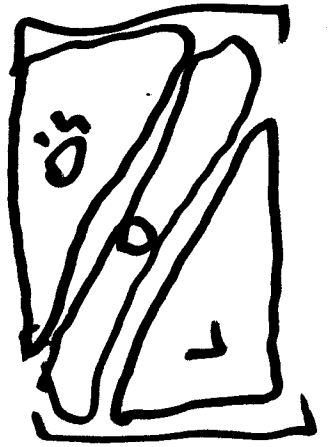


treat as
off-nominal
turns ratio.



$$[Z_B] = [Y_B]^{-1}$$

.... still only need modify



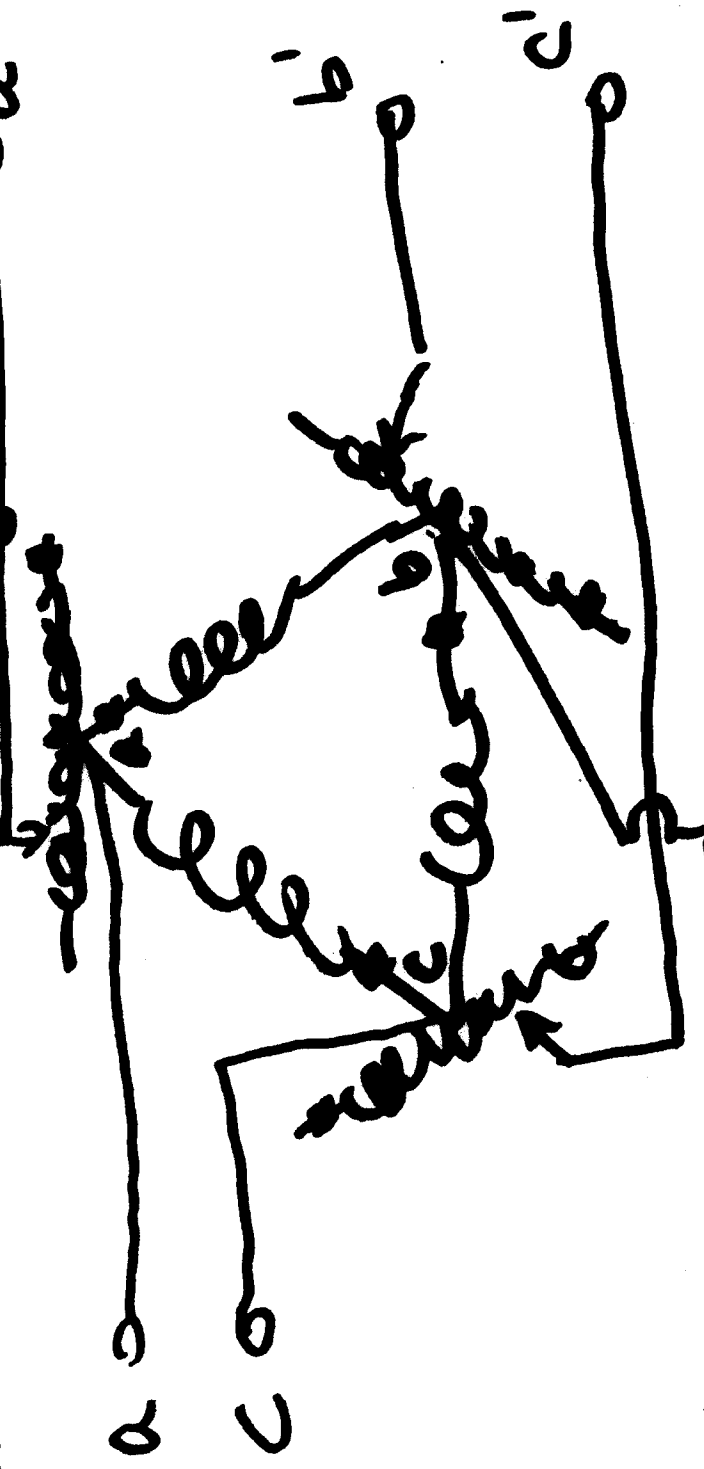
y_{57}

y_{55}

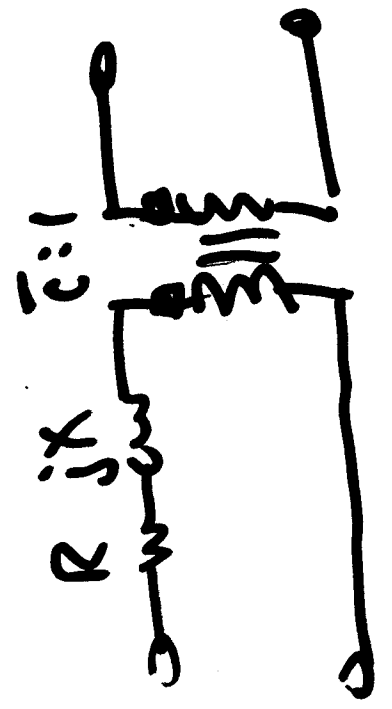
y_{75}

y_{77}

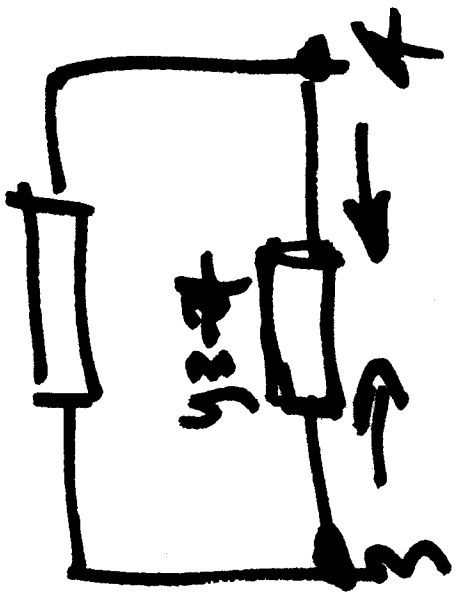
Phase Shift XFMRs (Fig. 2.22) a' 12



b a' Read §2.9!



→ $[Y_{Bus}]$



Building
by inspection:

$$\begin{bmatrix}
 1 & 0 & 0 & 0 \\
 0 & y_{12} & -y_{12} & 0 \\
 0 & -y_{12} & y_{12} + y_{23} & 0 \\
 0 & 0 & 0 & y_{43}
 \end{bmatrix}$$

$$\begin{array}{r}
 -y_{3-4} \\
 \hline
 \text{From KCL} \\
 \hline
 \sum I_s \text{ in} = 0
 \end{array}$$

$$\begin{array}{r}
 1 \\
 1 \\
 2 \\
 3 \\
 4 \\
 \hline
 1 \\
 1 \\
 2 \\
 3 \\
 4 \\
 \hline
 -y_{4-3}
 \end{array}$$

$$y_{33} = y_{33} + y_{3-4}$$

$$y_{44} = y_{44} + y_{4-3}$$

$$y_{34} = y_{34} - y_{3-4}$$

$$y_{43} = y_{43} - y_{4-3}$$

$$y_{3-4} = y_{4-3}$$

if bilateral.

FACTS -

ex:

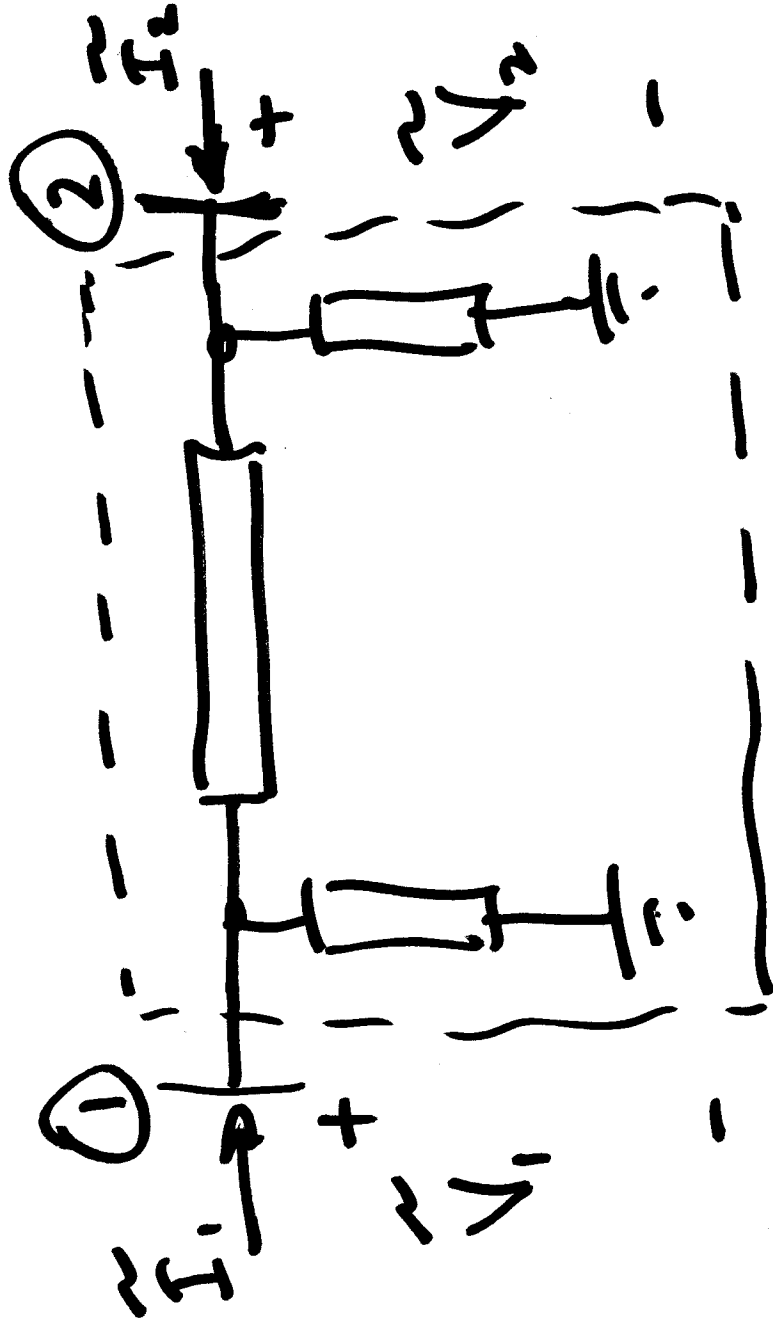
SUPFC - P & Q

SVC - Shunt Q

P.S. Transformer

non-bilateral
 $y_{mn} \neq y_{nm}$

$$\begin{bmatrix} \bar{y}_{11} & \bar{y}_{12} \\ \bar{y}_{21} & \bar{y}_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$



$$\bar{y}_{11} = \frac{\bar{I}_1}{\bar{V}_1} \Big|_{\bar{V}_2=0}$$

$$\bar{y}_{12} = \frac{\bar{I}_1}{\bar{V}_2} \Big|_{\bar{V}_1=0}$$

$$\bar{y}_{21} = \frac{\bar{I}_2}{\bar{V}_1} \Big|_{\bar{V}_2=0}$$

$$\bar{y}_{22} = \frac{\bar{I}_2}{\bar{V}_2} \Big|_{\bar{V}_1=0}$$

OPEN- and SHORT-CIRCUIT TESTS

Four Cases

R jx \overline{C}

 \overline{C}
 jx

R jx $i:\overline{C}$

 $i:\overline{C}$
 jx

\overline{C}

 R jx
 $i:\overline{C}$

$i:\overline{C}$

 R jx
 $i:\overline{C}$

Next:

XFMRS

$\left[\begin{matrix} jx \\ i:\overline{C} \end{matrix} \right]$

Basic Approach: Develop π -Equiv and handle just like T-Line.

One-Line:



Per-unit per-phase



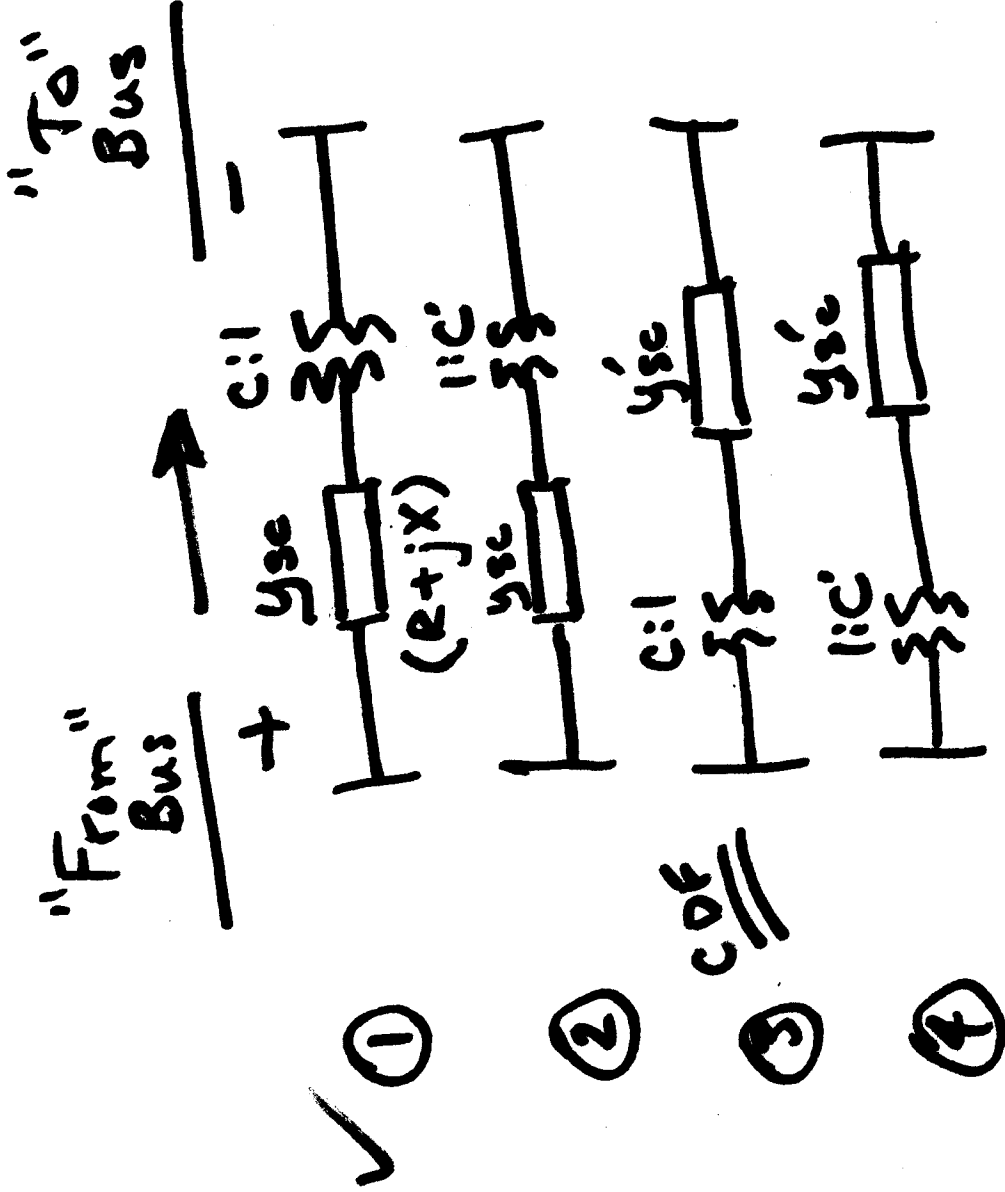
Top-Changers

- LTC's
- Phase-Shift



NOMINAL TRANS RATIO \uparrow \pm Adjustment (PS) in phase angle (LTC) OR VOLT MAG (LTC)

Tap Changing XFMRs - Variations (P.u. representations)



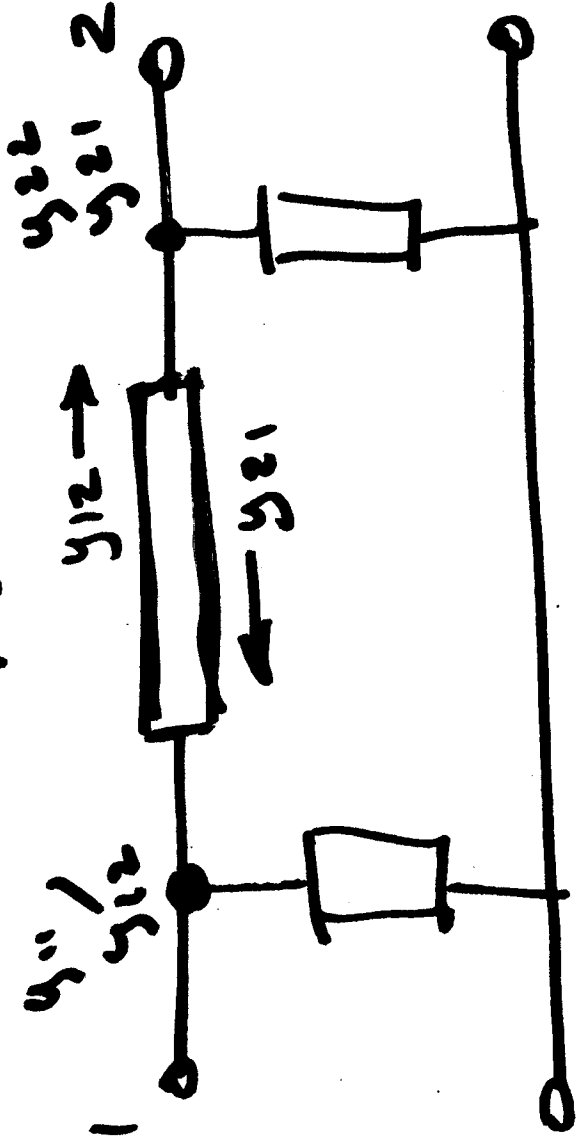
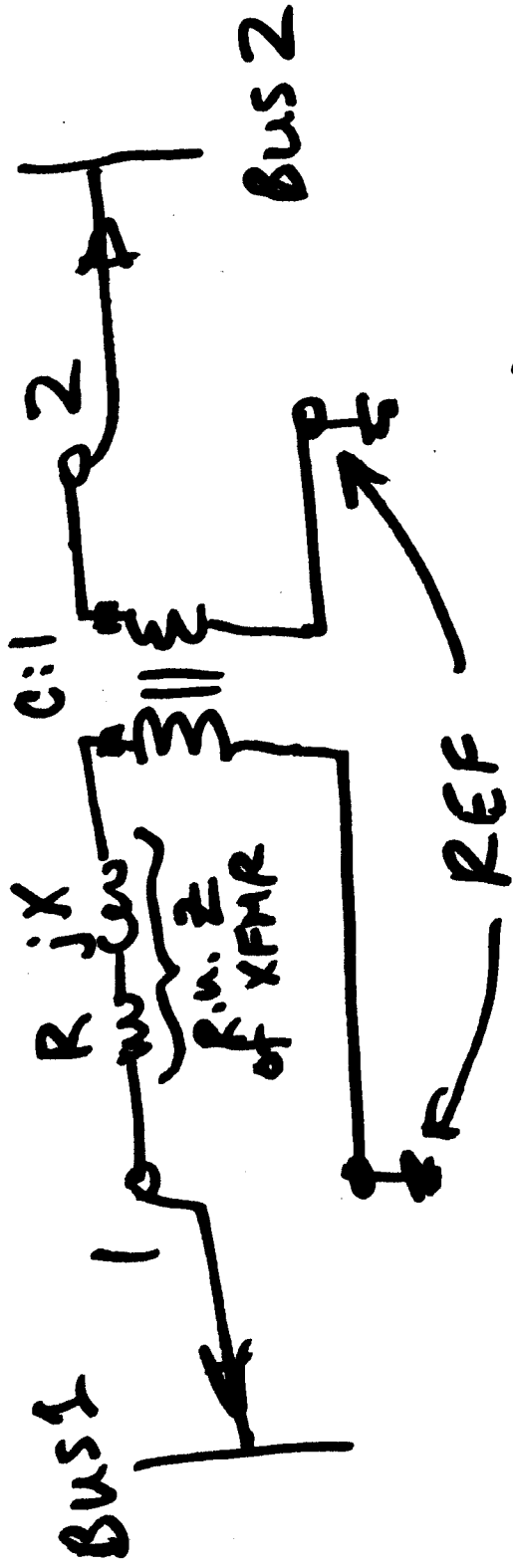
$$y_{sc} = \frac{1}{R+jX}$$

"C" is off-nominal turns ratio. In general C is complex.

C is real for LTC.
C is complex for PS.

If $|C| \neq 1$ then magnitude change.

If C is complex, Phase Shift.



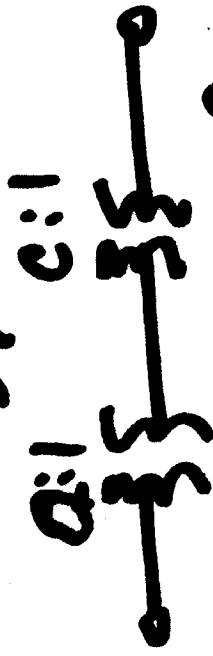
TAP-CHANGERS

a

On One-Line Diagrams:

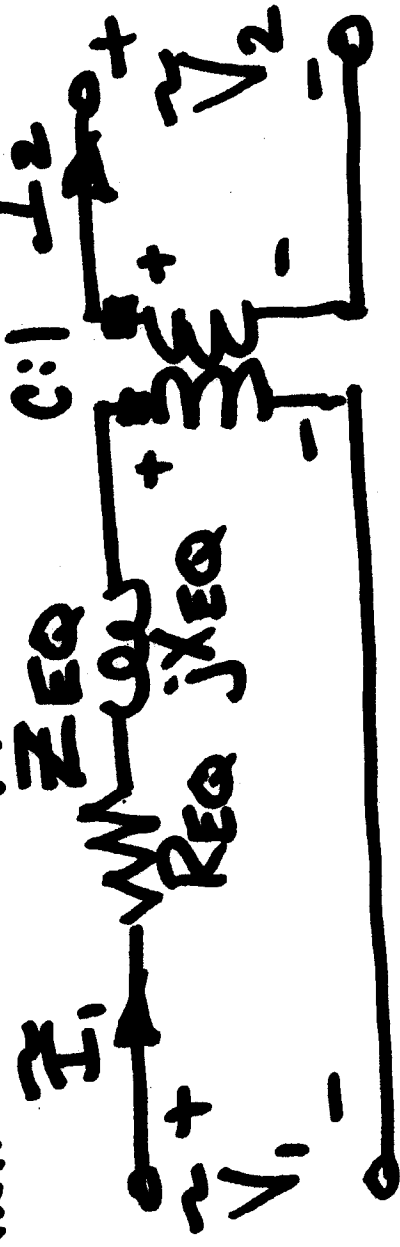


Conceptually:

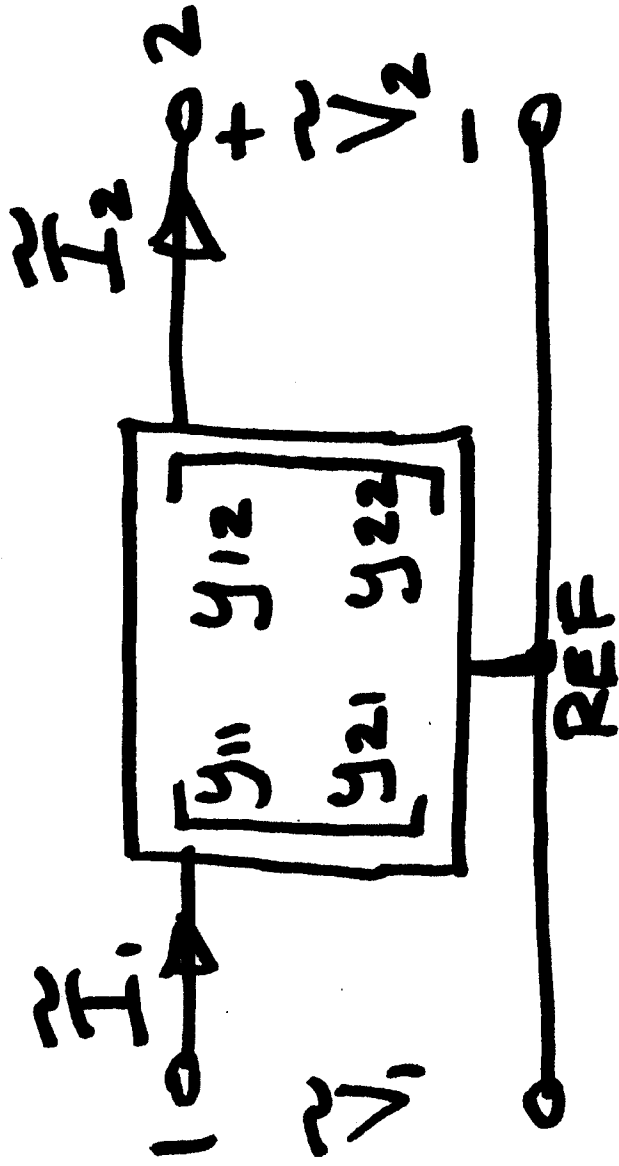


Nominal Voltage Ratio \uparrow off-nominal turns ratio due to Tap changer

In per unit, nominal transformation "disappears"



Generically, we can describe this as a 2-node [Y]

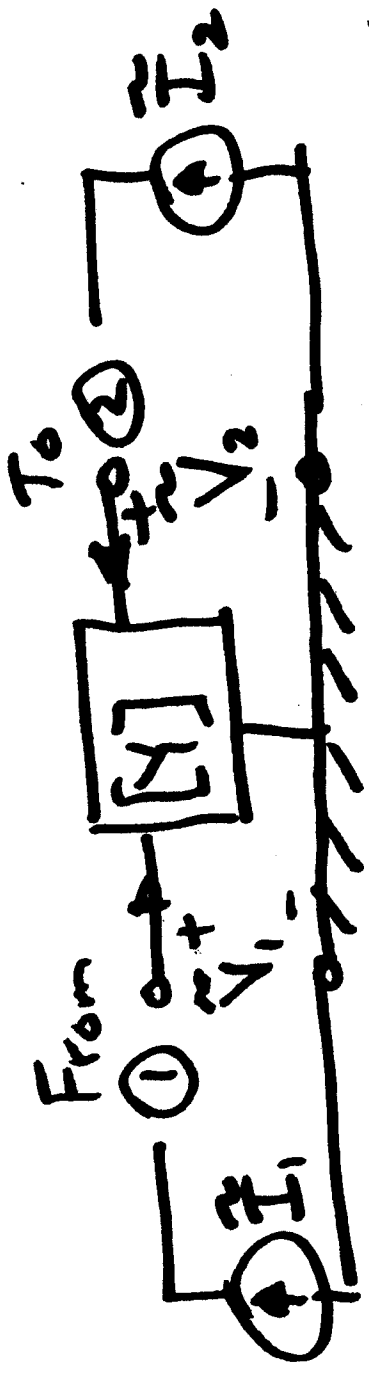


where

$$\begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ -I_2 \end{bmatrix}$$

$$\vec{I} = -\vec{I}_2$$

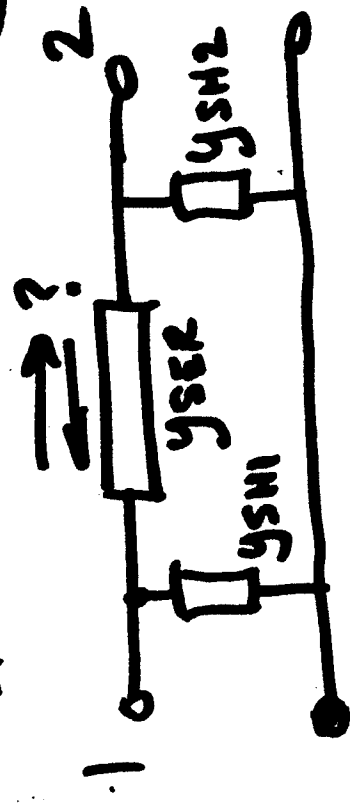
Standard Approach:



injected currents!

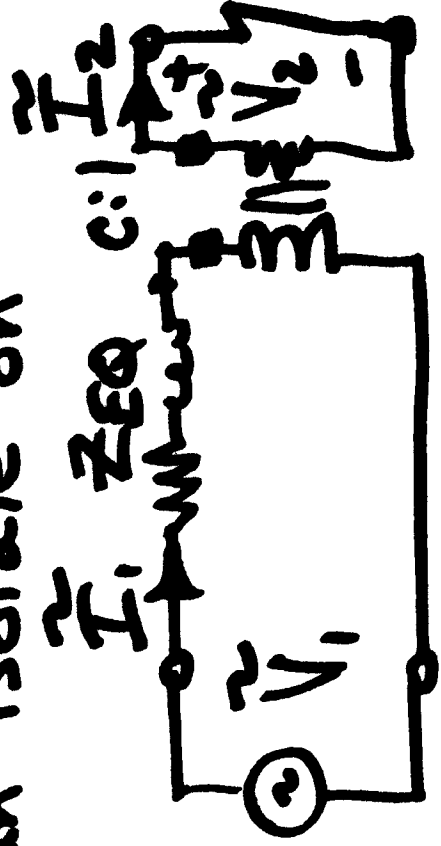
$$\begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\begin{aligned} y_{11} &= y_{SER} + y_{SH1} \\ y_{12} &= -y_{SER} \\ y_{21} &= -y_{SER} \\ y_{22} &= y_{SER} + y_{SH2} \end{aligned}$$



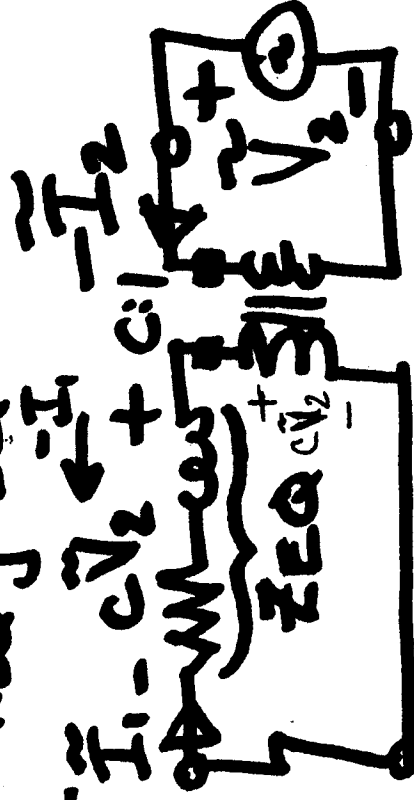
Goal:

Strategically using shorts ~~on~~
~~the~~ values of $[Y]$, we can isolate on



$$y_{11} = \frac{\tilde{I}_1}{\tilde{V}_1} \Big|_{\tilde{V}_2=0}$$

$$= \frac{1}{Z_{EQ}} = Y_{EQ}$$



$$y_{22} = \frac{-\tilde{I}_2}{\tilde{V}_2} \Big|_{\tilde{V}_1=0}$$

$$= \frac{1}{Z_{EQ}/|c|^2} = |c|^2 Y_{EQ}$$

$$\vec{I}_1 = -\frac{c\vec{V}_2}{z_{EQ}}; -\vec{I}_2 = -\frac{\vec{I}_1 * c^*}{z_{EQ}} = -\left[\frac{c\vec{V}_2}{z_{EQ}}\right] c^*$$

$$= \frac{|c|^2 \vec{V}_2}{z_{EQ}}$$

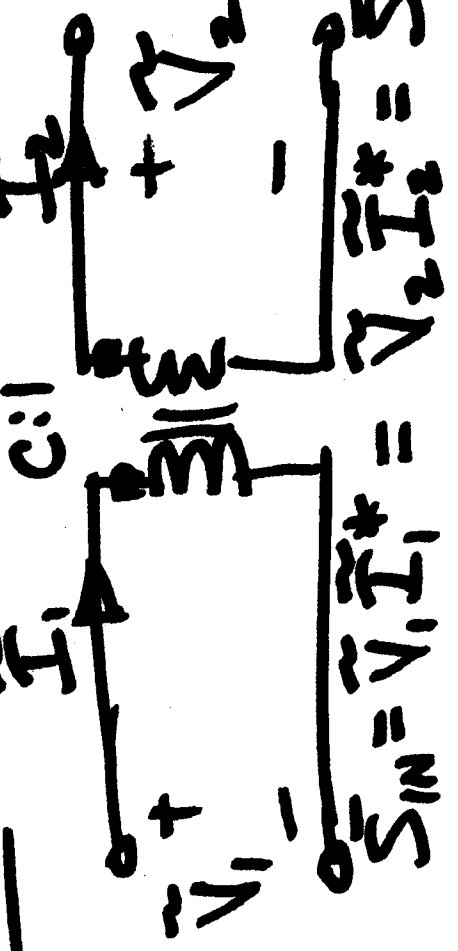
Note: $\frac{I_2}{I_1} = c^*$

$$y_{12} = \frac{\tilde{I}_1}{\tilde{V}_2} \Big|_{\tilde{V}_1=0} = \frac{-C \tilde{V}_2 / Z_{EQ}}{\tilde{V}_2} = -C Y_{EQ}^d$$

$$y_{21} = -\frac{\tilde{I}_2}{\tilde{V}_1} \Big|_{\tilde{V}_2=0} = \frac{-C^* \tilde{I}_1}{\tilde{V}_1} = -C^* Y_{EQ}$$

Note: Ideal XFR, by definition, has

"C" is voltage ratio.

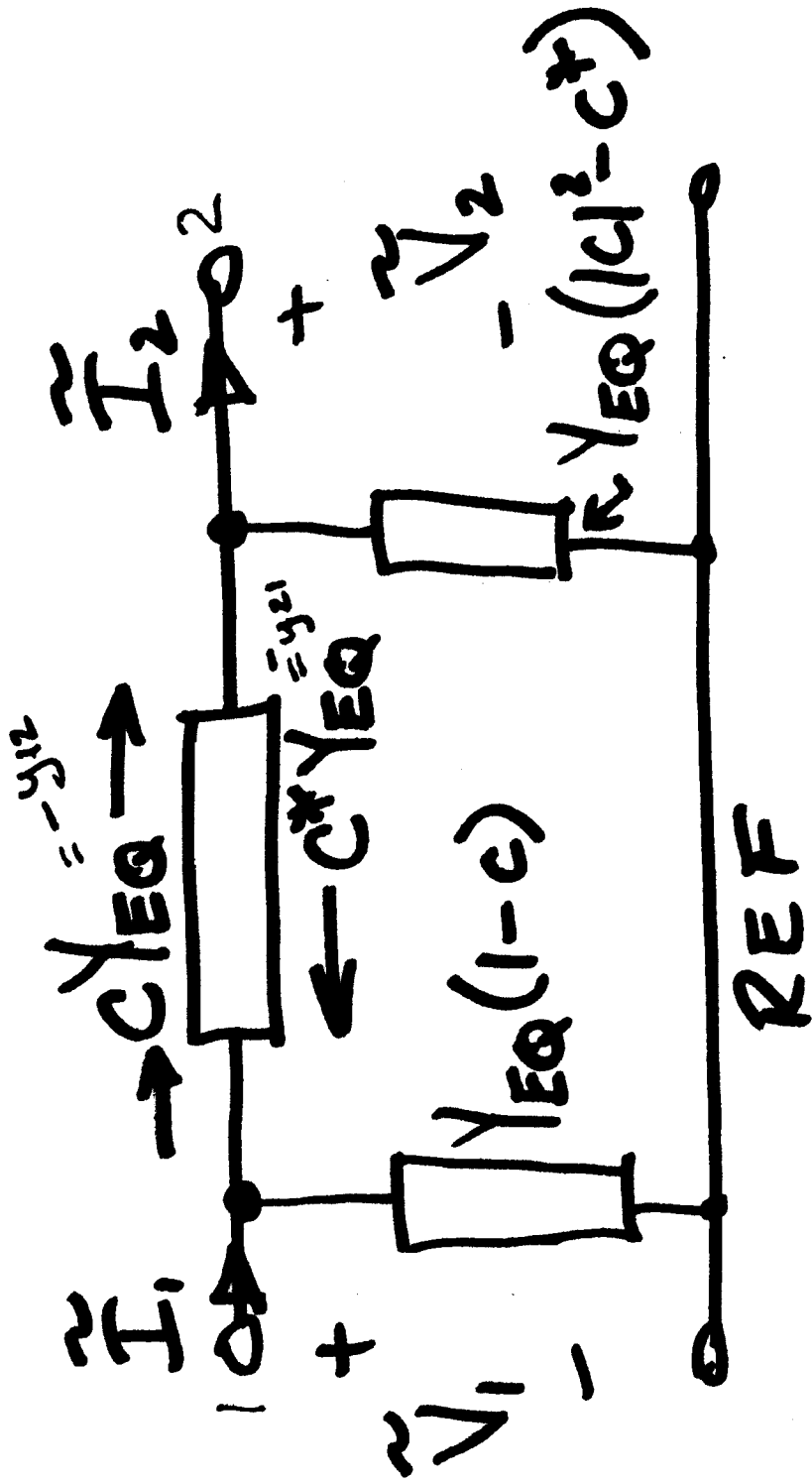


$$C = \frac{\tilde{V}_2}{\tilde{V}_1} = \frac{\tilde{I}_1}{\tilde{I}_2} \Rightarrow \tilde{I}_2 = \frac{\tilde{I}_1}{C} = C^* \tilde{I}_1$$

If we "reverse engineer" our e)

$[Y]$ into an equivalent 2-bus

network, then



f

Observations:

- LTC (TCL) has a C that is Real.

\therefore Transfer Admittances

$$C Y_{EQ} = C^* Y_{EQ} \Rightarrow \text{Bilateral. } (y_{12} = y_{21})$$

- Phase-Shifter (PS) has complex C .

\therefore Transfer admittances

$$C Y_{EQ} \neq C^* Y_{EQ}$$

$$y_{12} \neq y_{21}$$

Not Bilateral.

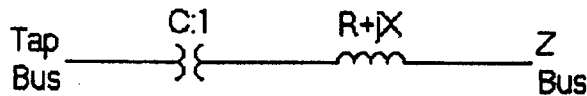
$[Y]$ not symm.
about main diag.

Transformer LTC's in the CDF File Format

Tap and impedance location specified in first two entries in branch data section.

- entry 1 is bus non-unity tap is connected to
- entry 2 is bus device impedance is connected to

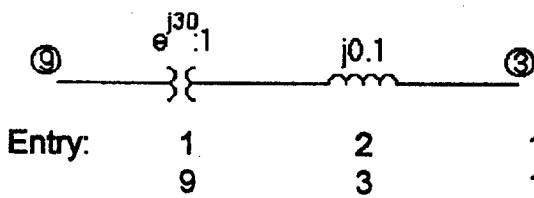
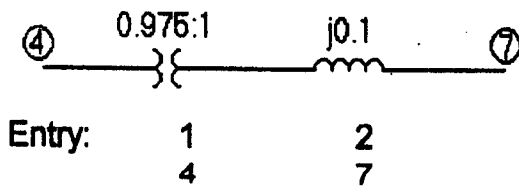
"From"



Complex turns ratio due to phase shifting transformer split to two entries

- entry 15 is transformer final turns ratio
- entry 16 is transformer (phase shifter) final angle

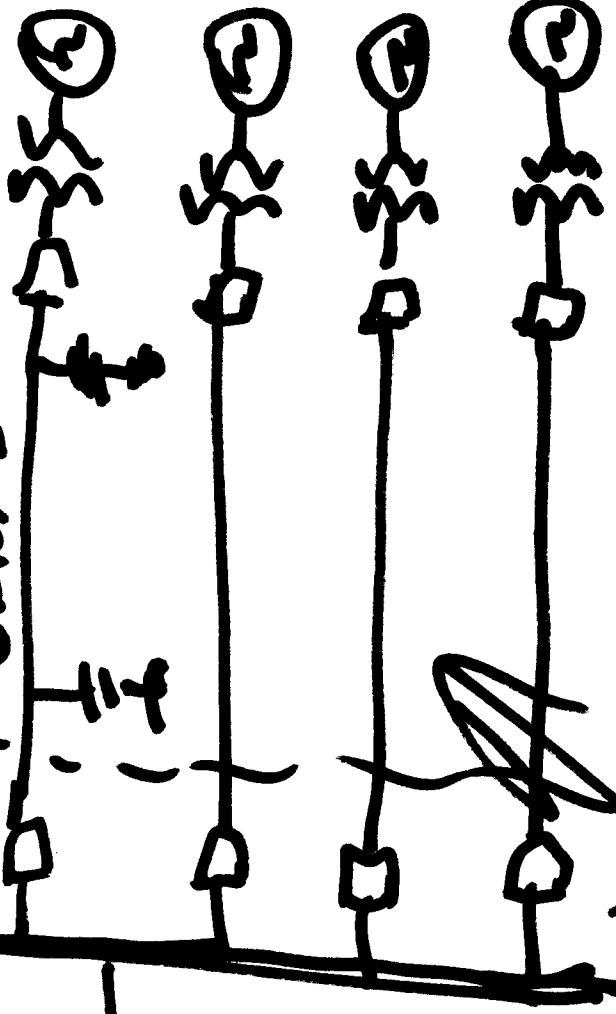
Examples:



151
 ↙
 Field no.

400-YV

! cables

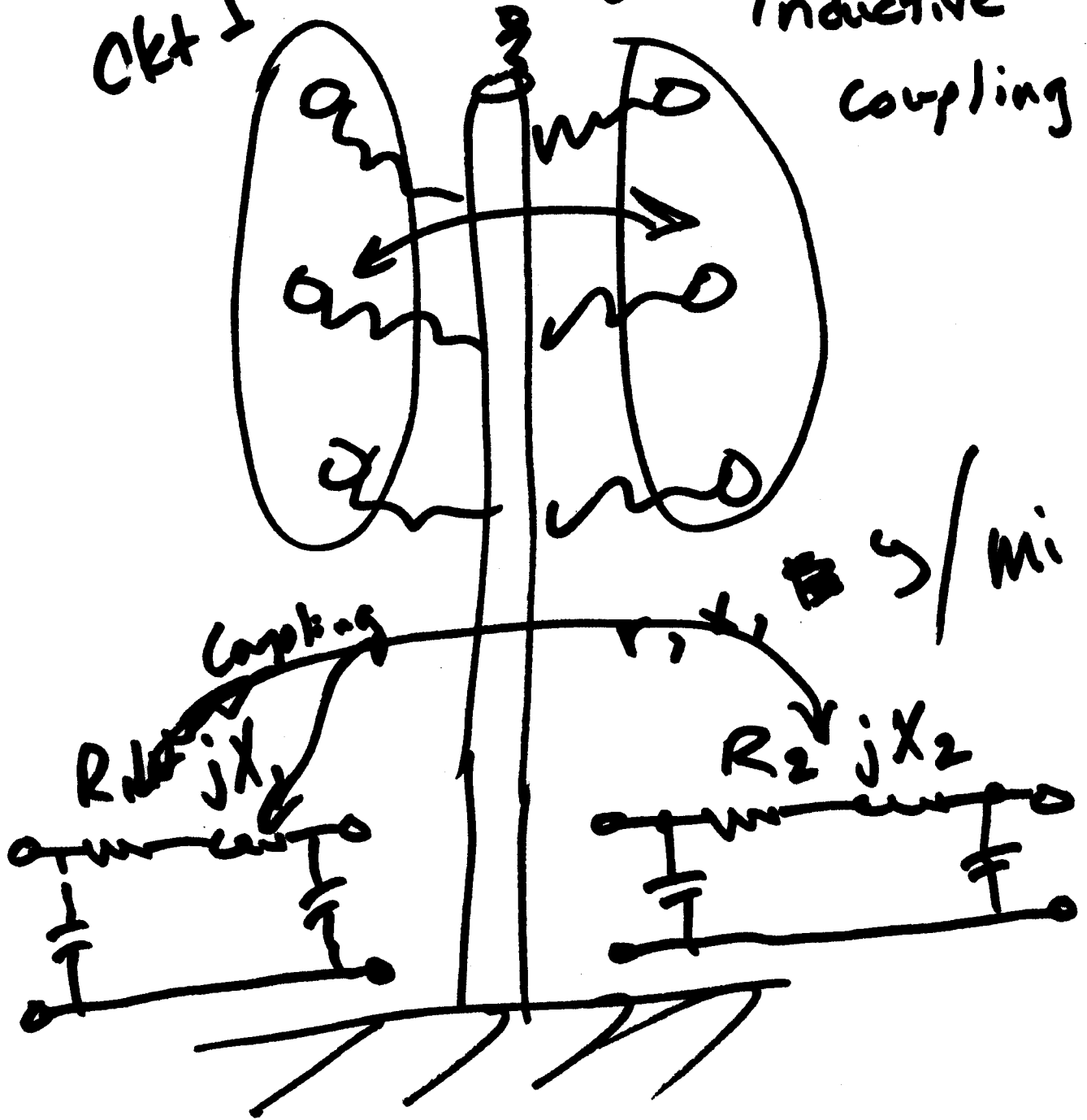


1 km

55 MWars

Ckt 1

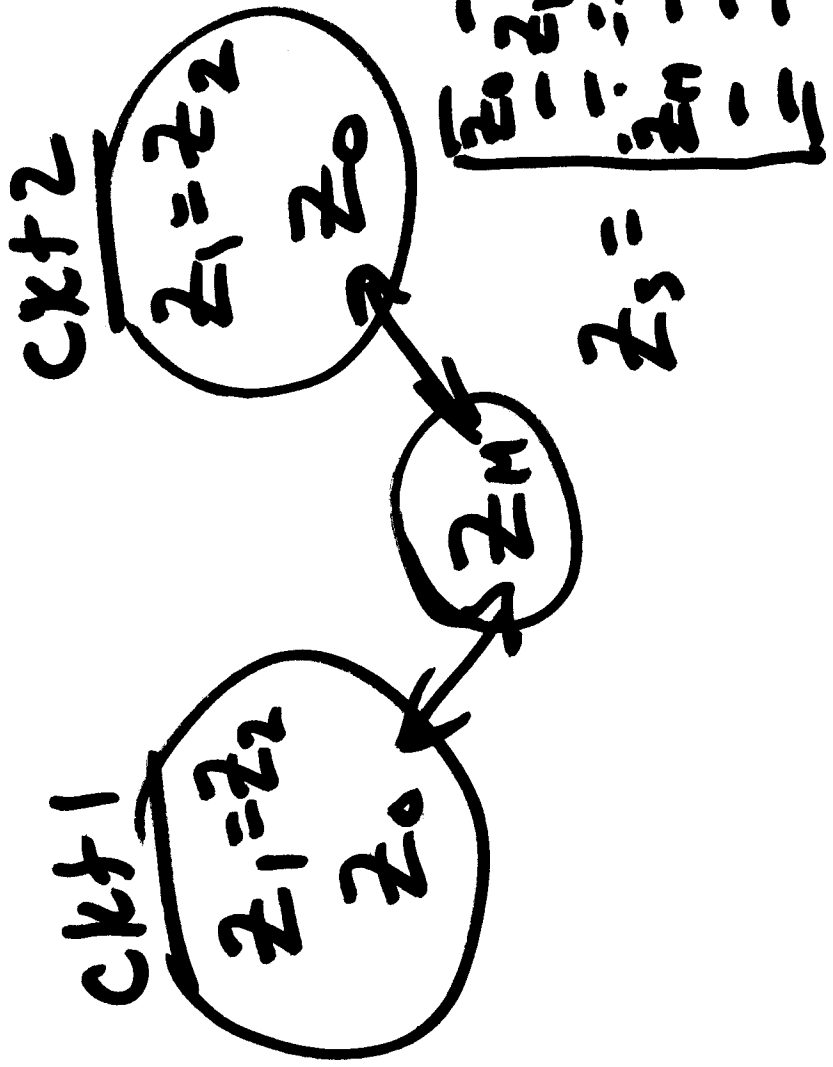
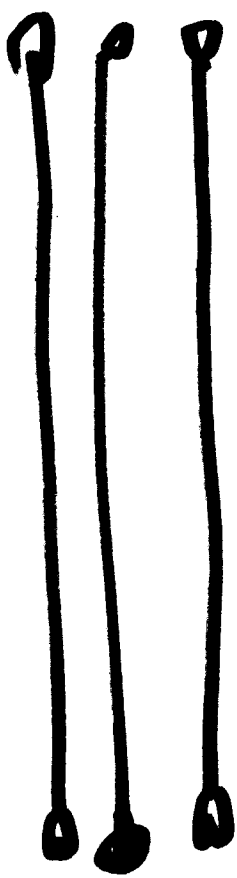
Ckt 2 inductive coupling!



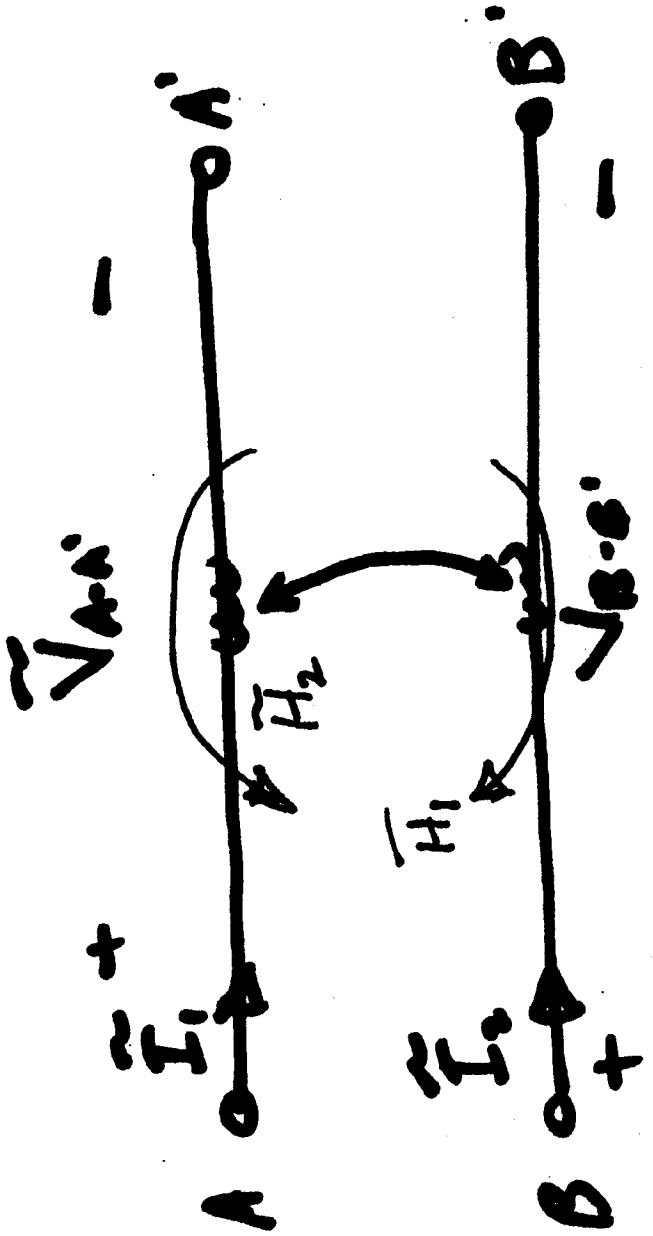
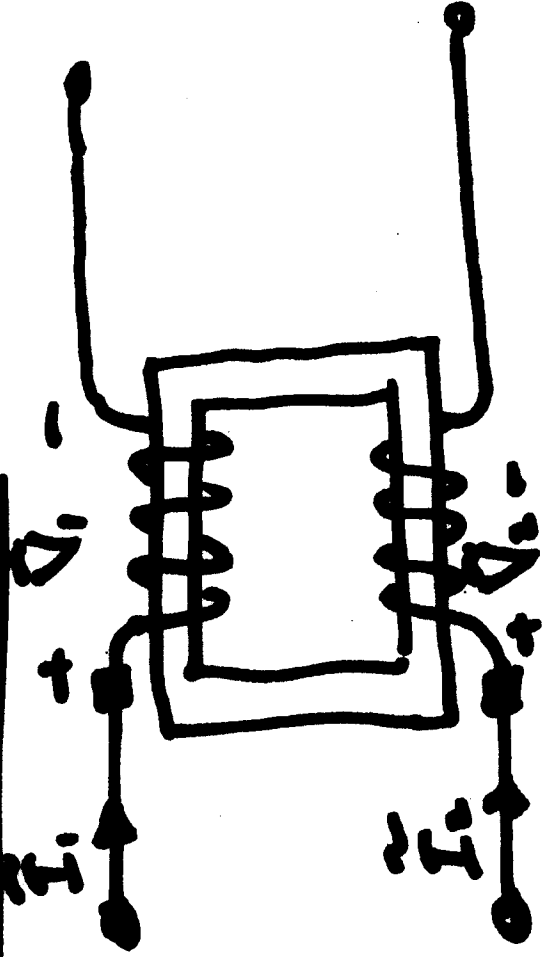
ckt 1



ckt 2



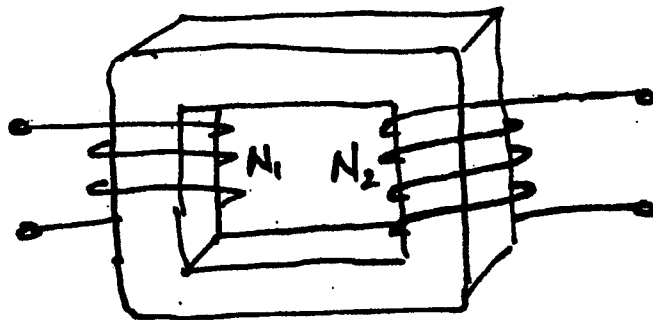
Mutual Inductance



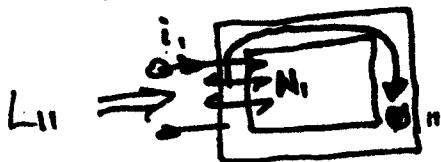
END
VIEW

MUTUAL INDUCTANCE

- see also handout on Basic Magnetic Circuits

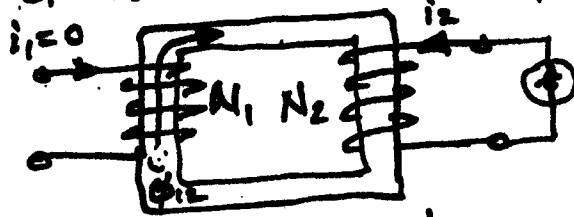


- Fundamental definition of inductance: $L = \frac{\lambda}{i} = \frac{N\Phi}{i}$



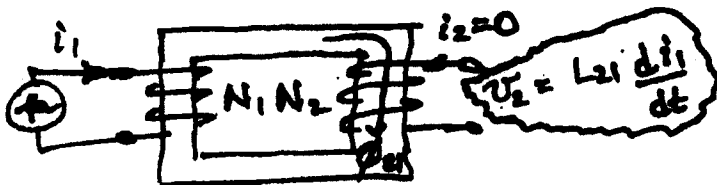
Self-Inductance

$$L_{11} = \frac{N_1 \Phi_{11}}{i_1} = \frac{\lambda_{11}}{i_1} = \frac{N_1^2}{\mathcal{R}}$$



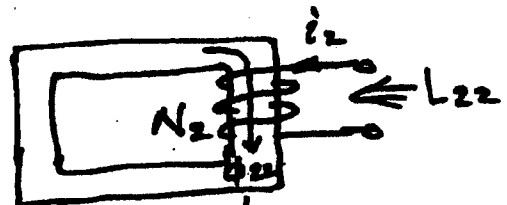
Mutual Inductance

$$L_{12} = \frac{N_1 \Phi_{12}}{i_2} = \frac{\lambda_{12}}{i_2} = \frac{N_1 N_2}{\mathcal{R}}$$



$$L_{21} = \frac{N_2 \Phi_{21}}{i_1} = \frac{\lambda_{21}}{i_1} = \frac{N_2 N_1}{\mathcal{R}}$$

Mutual Inductance

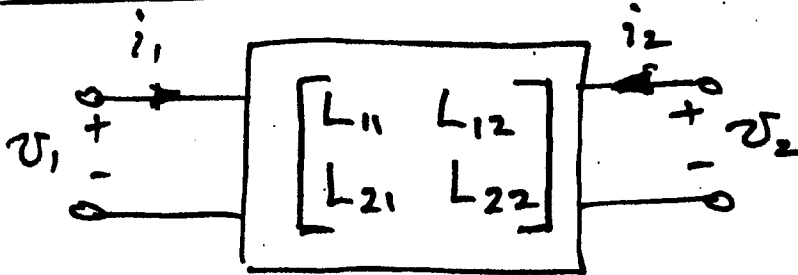


Self Inductance

$$L_{22} = \frac{N_2 \Phi_{22}}{i_2} = \frac{\lambda_{22}}{i_2} = \frac{N_2^2}{\mathcal{R}}$$

How to Use the Concept of Mutual Inductance

Two-Port Device:



Note: Reference direction of currents is into terminals at (+) side of voltage.

In time domain:

$$\begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} L_{11} & L_{12} \\ L_{21} & L_{22} \end{bmatrix} \begin{bmatrix} \frac{di_1}{dt} \\ \frac{di_2}{dt} \end{bmatrix}$$

In phasor domain:

$$\begin{bmatrix} \tilde{v}_1 \\ \tilde{v}_2 \end{bmatrix} = \underbrace{\begin{bmatrix} j\omega L_{11} & j\omega L_{12} \\ j\omega L_{21} & j\omega L_{22} \end{bmatrix}}_{[Z]} \begin{bmatrix} \tilde{I}_1 \\ \tilde{I}_2 \end{bmatrix}$$

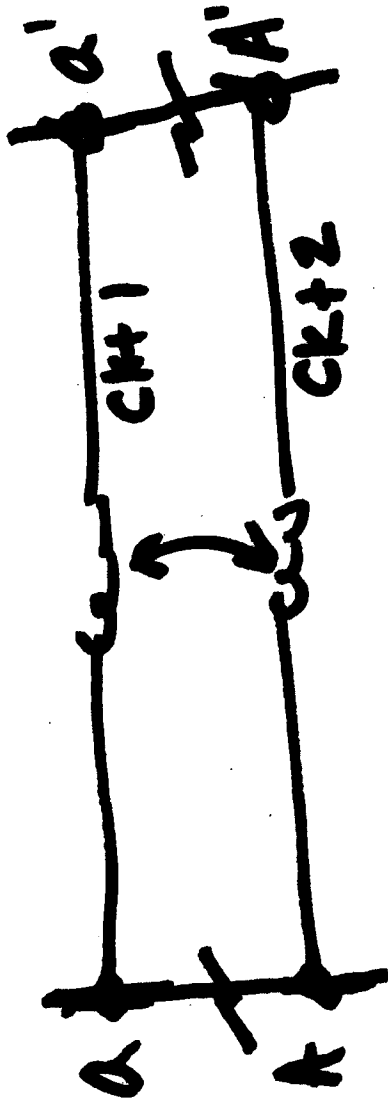
Also of note:

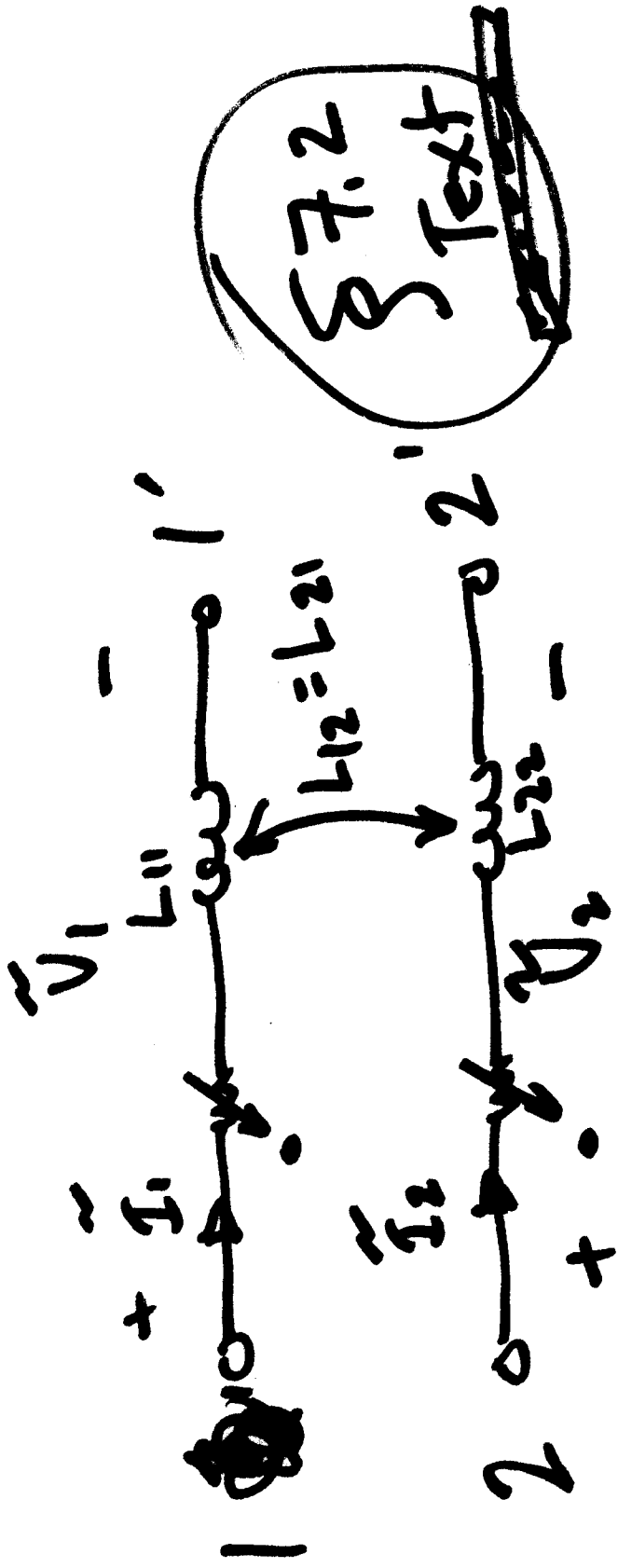
In some texts, since L_{12} and L_{21} are mutual inductances, they are called M_{12} and M_{21} . Same thing.

$$[Z] = [Y]$$

$$\begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

§ 7.2
of text.





Assume high $\frac{1}{R} (R \rightarrow 0)$

$$[v_i] = [Z] \begin{bmatrix} I_1' \\ I_2' \end{bmatrix} \Rightarrow [Y] [v_i] = [I_i]$$

pre-multiply
both sides by
 $[Z]^{-1}$

$$[I_i] = [Y] [v_i]$$