

## Topics for Today:

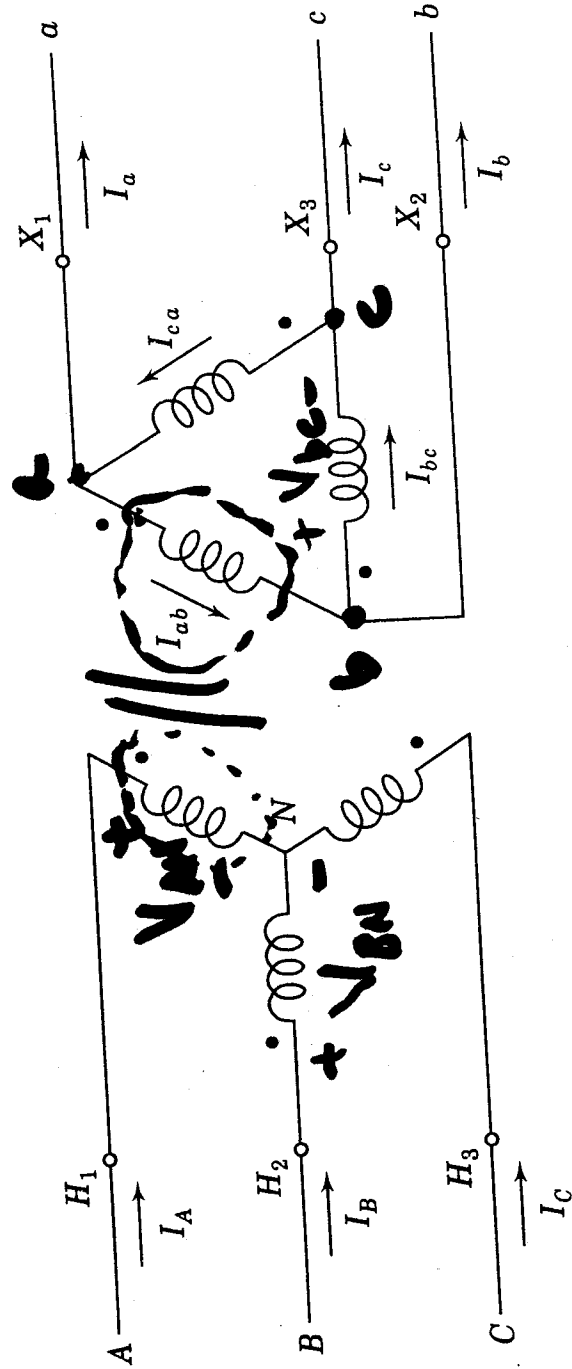
- Announcements
  - Software: Matlab? Will begin using as early as next week. —
  - Office hrs: 1:30-2:30pm, Mon, Wed, Fri
  - Office: EERC 623. Phone: 906.487.2857
  - Exercises posted on web page, check e-mail for details. —
  - Collected problems, solutions posted after collecting. —
  - Recommended problems from Ch.2, solutions posted —
- Chapter 2 - Transformers and circuits w/transformers
  - 3-phase transformer banks and phase shifts (ANSI/IEEE vs. IEC)
  - Standard 30° shift transformers, non-standard connections
  - Pos/neg sequence phase shifts
  - Autotransformers —
  - Load Tap Changing (LTC) transformers
  - Phase shifting transformers
  - Paralleling transformers with a) unlike impedances; b) unlike tap positions
  - Three-winding transformers

er by the per-unit  
is not important  
er unit with the  
rmer impedances,  
the resistance is

220 Y/22Δ kV. The  
-voltage side of the  
, this value may be  
per-unit reactance of  
insformer in a system  
MVA, 230 kV.

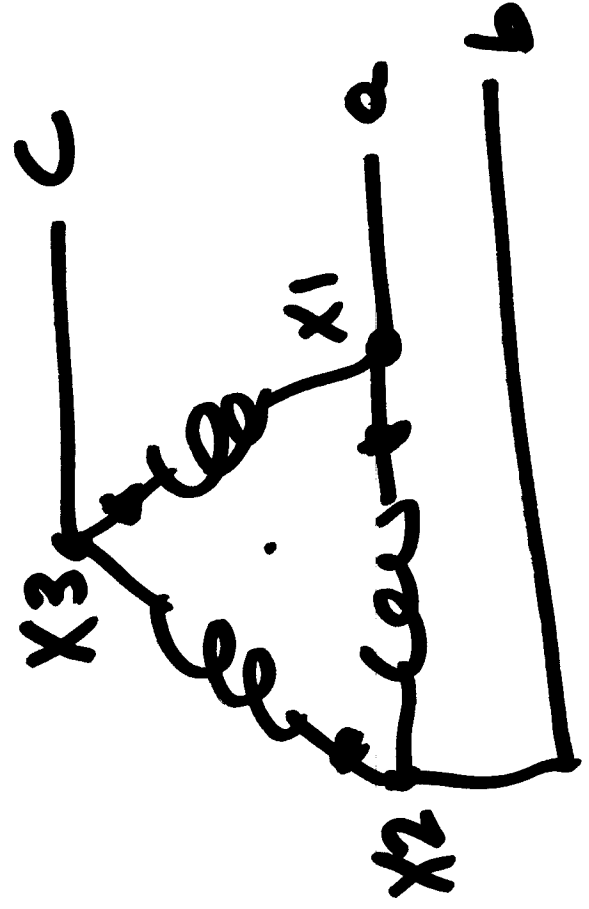
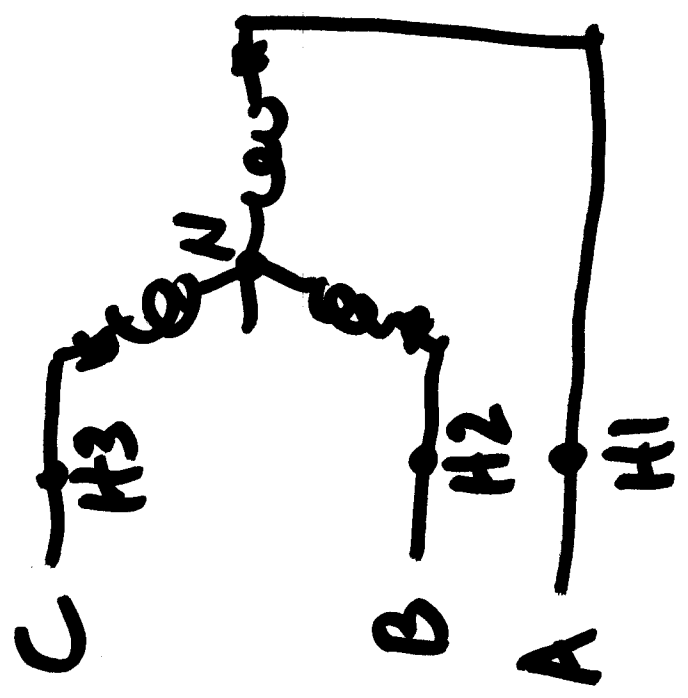
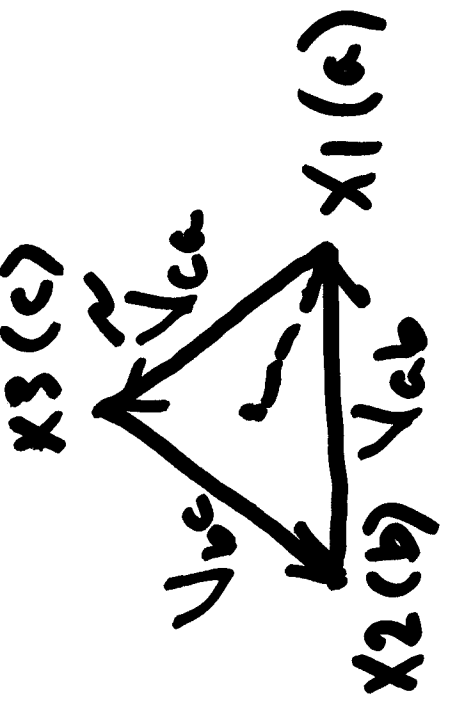
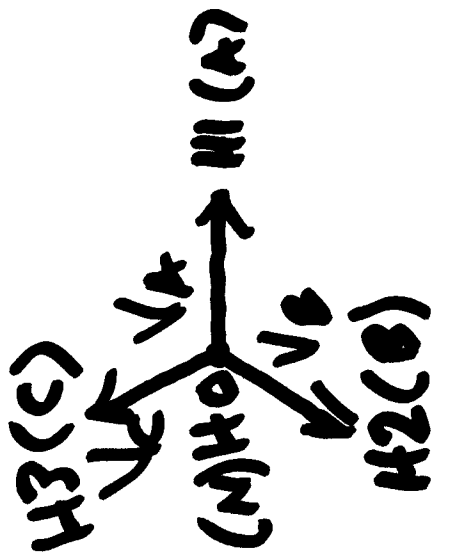
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2.6 THREE-PHASE TRANSFORMERS: PHASE SHIFT AND EQUIVALENT CIRCUITS **65**



(a) Wiring diagram

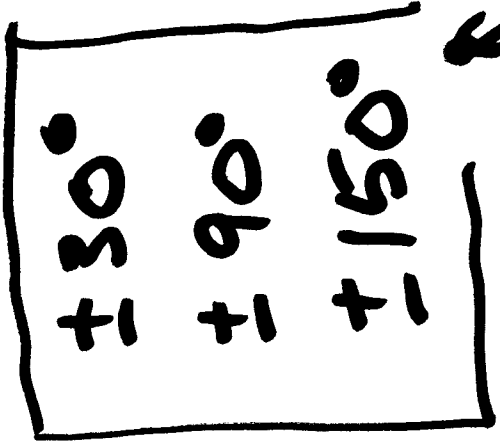
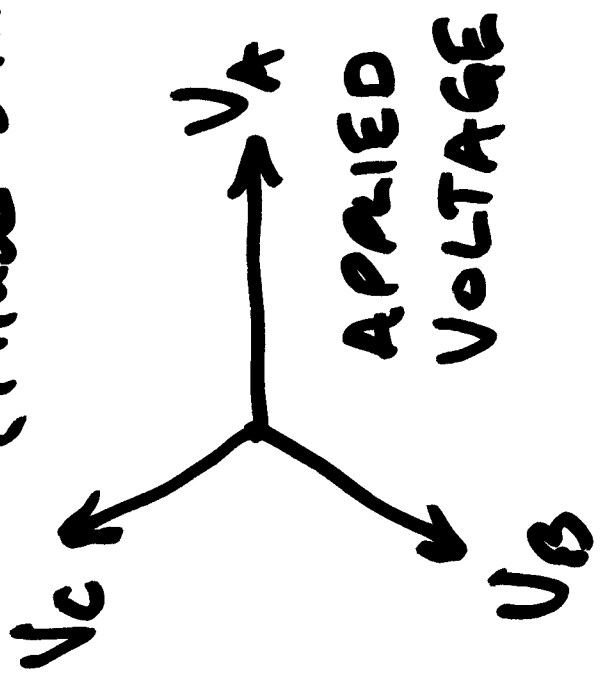
Note: Phasor diagrams in text do not follow  
Common practice.



# Possible Connections for (Phase-Shifts)

$\Delta$ -Y or Y $\Delta$  XFMRs?

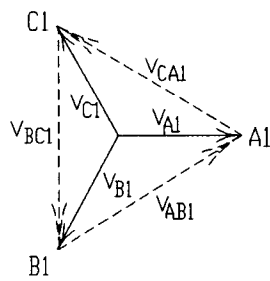
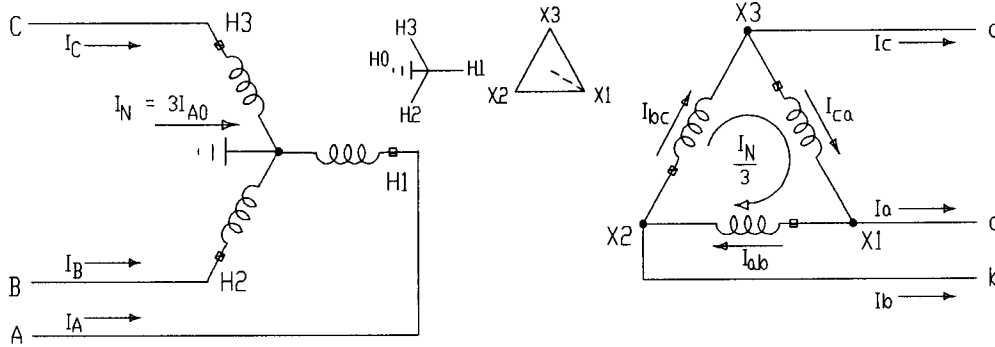
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Note: Textbook "cookbook" eqns are set up to assume 30° phase shift.

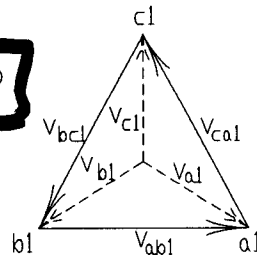
But - many transformers are non-std phase shift required by the grid tie requirements. ∴ learn to use phasor diagrams to figure out correct phase shifts!

MORK

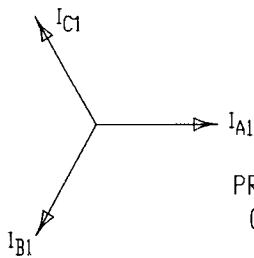


$$V_{A1} = V_{a1} \angle 30^\circ$$

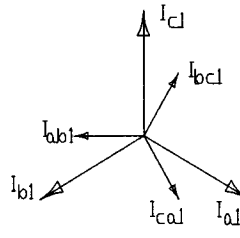
PRI POS SEQ VOLTAGES



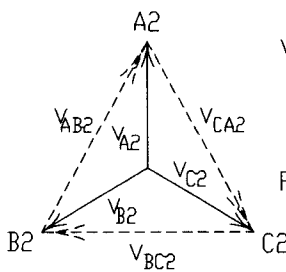
SEC POS SEQ VOLTAGES



PRI POS SEQ CURRENTS

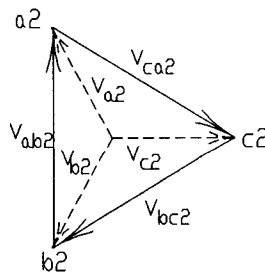


SEC POS SEQ CURRENTS

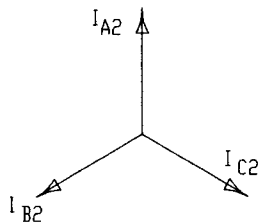


$$V_{A2} = V_{a2} \angle -30^\circ$$

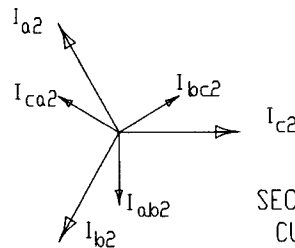
PRI NEG SEQ VOLTAGES



SEC NEG SEQ VOLTAGES



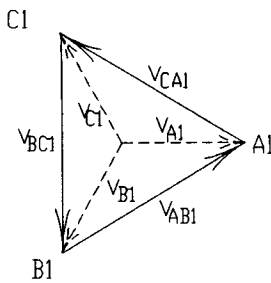
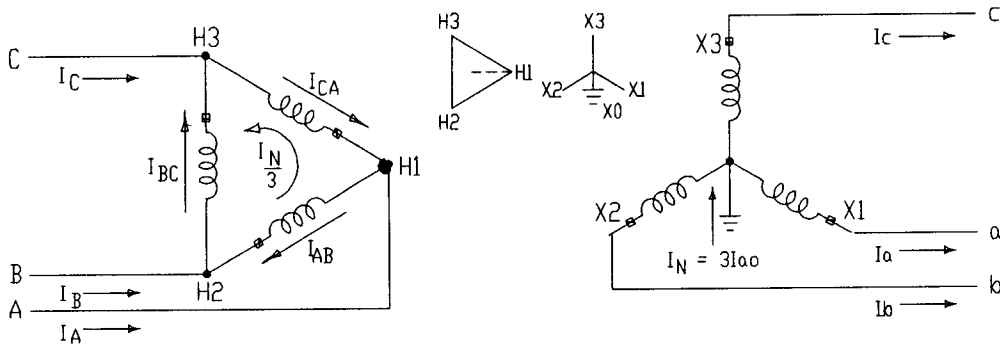
PRI NEG SEQ CURRENTS



SEC NEG SEQ CURRENTS

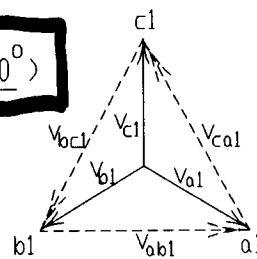
ANSI STANDARD 30-DEGREE SHIFT WYE-DELTA

MARK

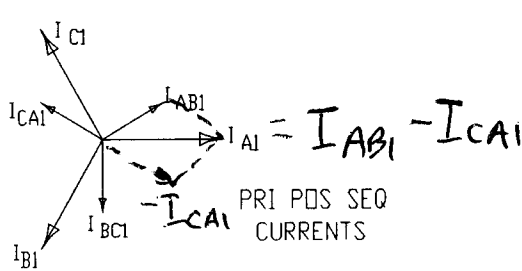


$$V_{A1} = V_{a1} (\angle 30^\circ)$$

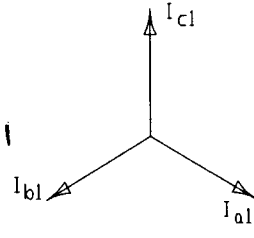
PRI POS SEQ VOLTAGES



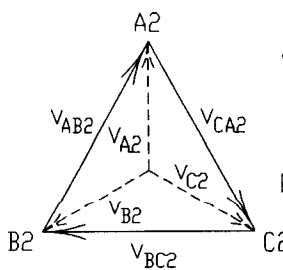
SEC POS SEQ VOLTAGES



PRI POS SEQ CURRENTS

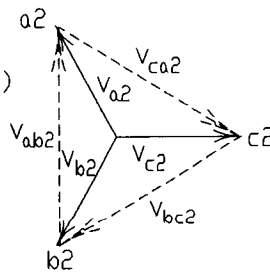


SEC POS SEQ CURRENTS

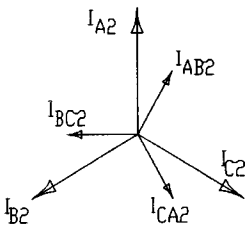


$$V_{A2} = V_{a2} (\angle -30^\circ)$$

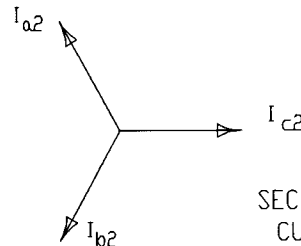
PRI NEG SEQ VOLTAGES



SEC NEG SEQ VOLTAGES



PRI NEG SEQ CURRENTS



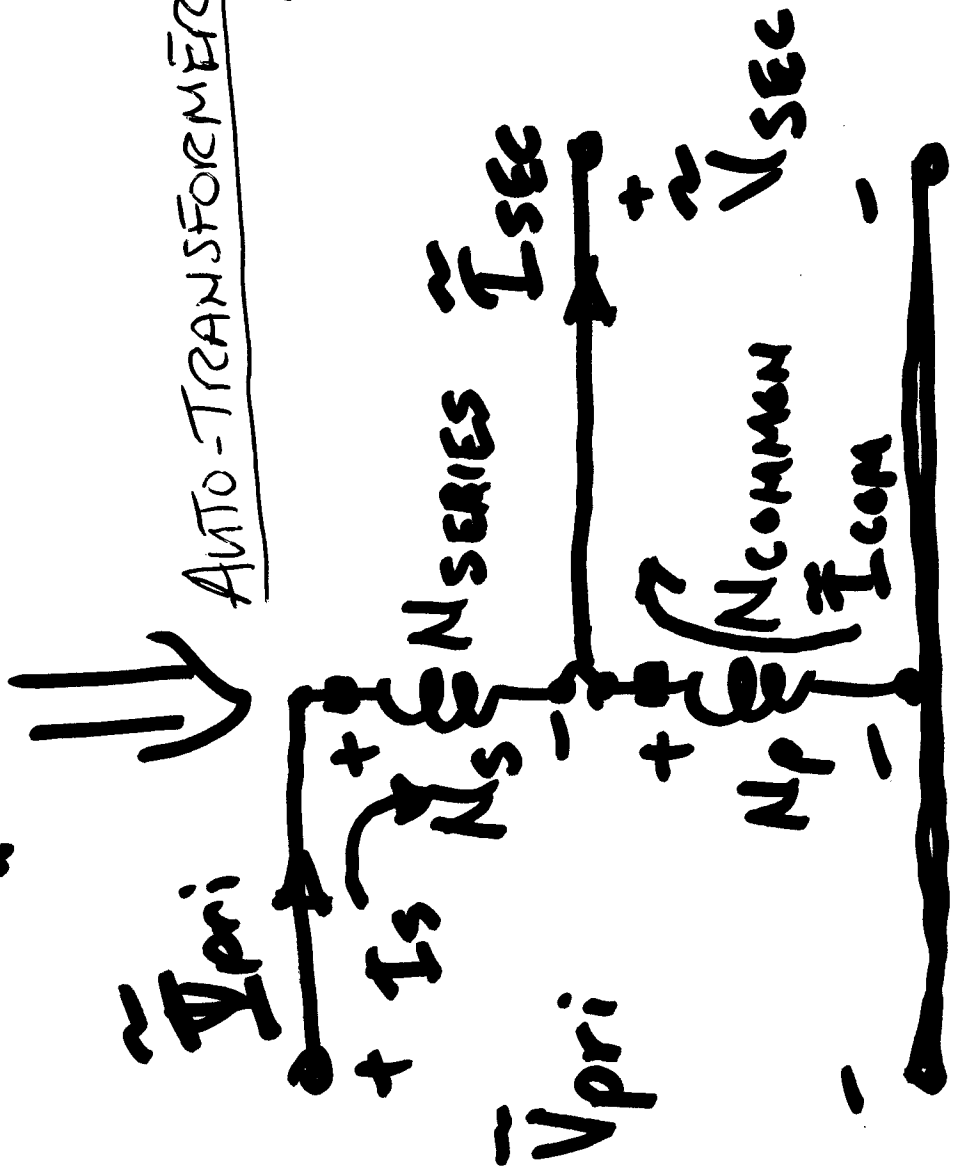
SEC NEG SEQ CURRENTS

ANSI STANDARD 30-DEGREE SHIFT DELTA-WYE

$$\tilde{V}_p \tilde{I}_p^* = \tilde{V}_s \tilde{I}_s^*$$



AUTO-TRANSFORMERS



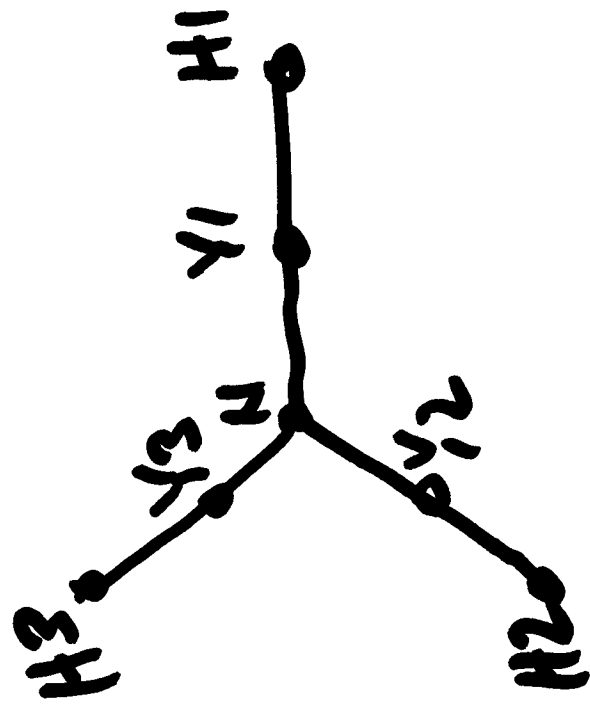
$$\tilde{V}_{pri} \tilde{I}_{pri}^* = \tilde{V}_{sec} \tilde{I}_{sec}^*$$

$$\tilde{I}_{sec} = \tilde{I}_s + \tilde{I}_{com}$$

- Auto: transform more VA for same coil ratings (i.e. cheaper than 2-winding)
- 2-Winding provides isolation between pri-sec.

- Auto doesn't.

- Auto transformer: no phase shift for 3-ph applications.

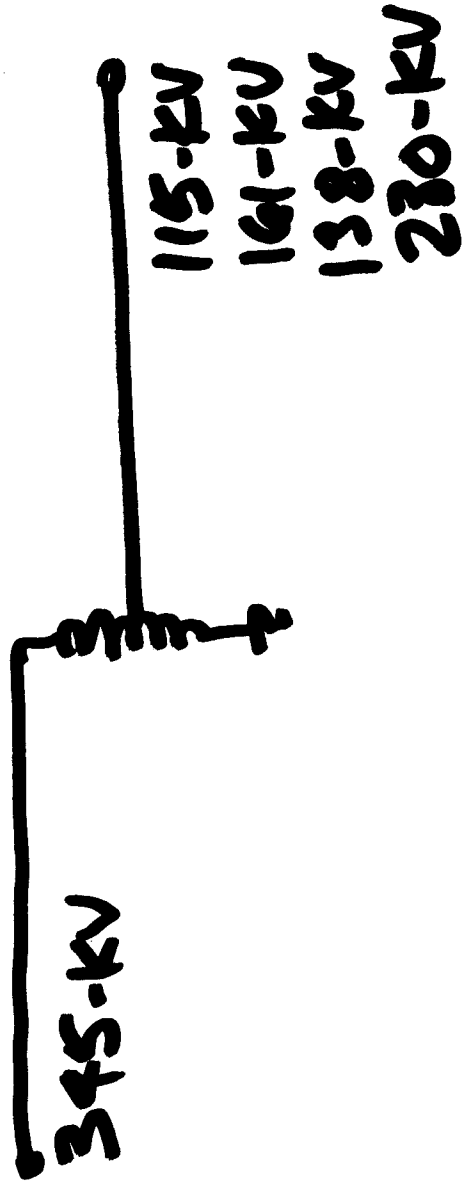


Tertiary:

- Station Service
- Local Distribution
- Reactors or Caps
- Relaying CTs
- Harmonic Containment  
Triplen Circulation.



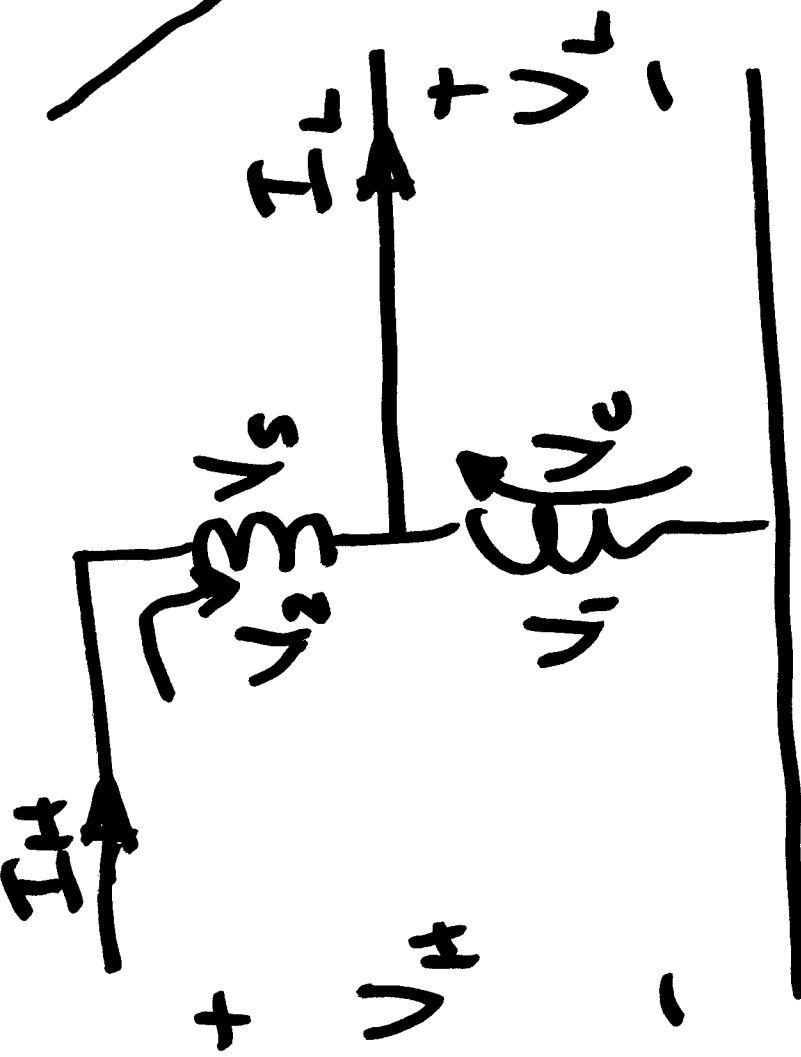
- Autotransformers usually limited to  $\leq 3:1$  voltage ratio. (leakage impedance)



"VOLT-AMP ADVANTAGE"

Ratio of

$$\frac{VA_{\text{Auto}}}{VA_{2\text{-winding}}} = VA \text{ Advantage}$$



$$I_1 = \frac{N_1}{N_2} I_2 = \frac{I_2}{n}$$

$$VA_{2-ws} = V_1 I_1 = V_2 I_2$$

$$VA = V_H I_H = V_L I_L$$

$$VA_{NOV} = \frac{V_H I_H}{V_1 I_1} = \frac{V_1 I_1 (2n+1) I_2}{V_1 I_1}$$

$$I_H = I_2$$

$$V_L = V_1$$

$$V_H = V_1 + V_2$$

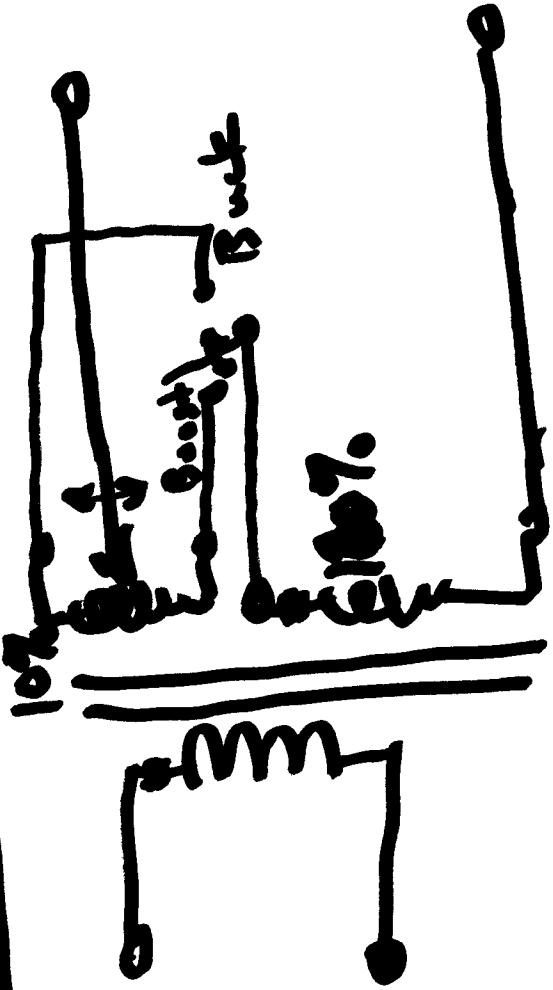
$$I_L = I_1 + I_2$$

$$= \frac{(V_1 + V_2) I_1 \left(\frac{V_2}{V_1}\right)}{V_1 I_1} = \boxed{\frac{(V_1 + V_2)}{V_2}}$$

VOLT-AMPS  
ADVANTAGE

# TAP-CHANGERS (LTC)

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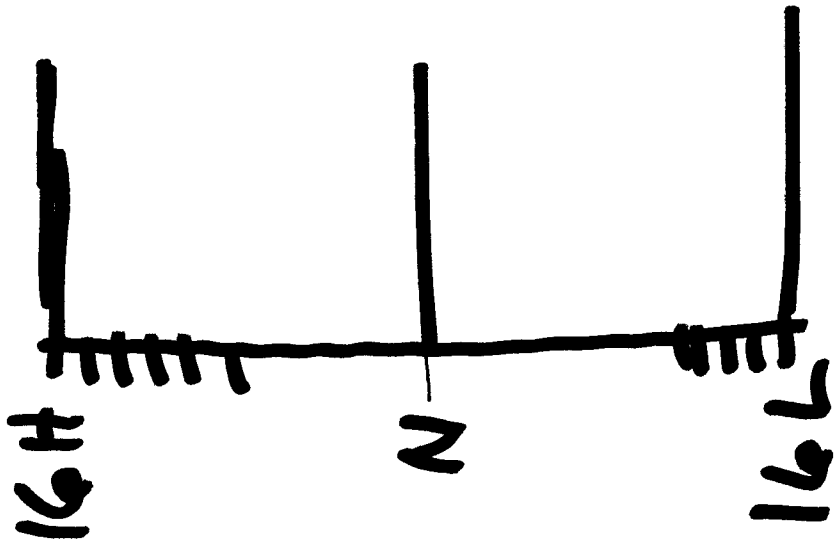
→ boost or "buck"  
Nominal voltage  
by 10%.

Thus:  $V_{\text{Nominal}} \pm 10\%$

16 tap positions

33 total positions

5/8% each step.



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# APPENDIX

# A

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From  
EE 5200 text

**TABLE A.1**  
**Typical range of transformer reactances†**  
Power transformers 25,000 kVA and larger

Nominal system voltage, kV	Forced-air-cooled, %	Forced-oil-cooled, %
34.5	5-8	9-14
69	6-10	10-16
115	6-11	10-20
138	6-13	10-22
161	6-14	11-25
230	7-16	12-27
345	8-17	13-28
500	10-20	16-34
700	11-21	19-35

† Percent on rated kilovoltampere base. Typical transformers are now designed for the minimum reactance value shown. Distribution transformers have considerably lower reactance. Resistances of transformers are usually lower than 1%.