

Reordering

- It is strategic to reorder the (row,column) indices of the coefficient matrix to make LU factorization most efficient
- Basic Idea:
 - Move the buses that have the fewest connections to the top of [Y]. This reduces the number of fills when factorizing.
 - Constraints:
 - Buses of known voltage must stay at the bottom.
 - Augmented equations with zero main diagonal should remain toward the bottom to guarantee a fill of the main diagonal.

Reordering: (in-situ methods)

For: LU factorization
Gaussian Elim
Gauss-Jordan Elim

Strategy:
move rows
with most
zeros to top
i.e. least-
connected
buses to top)

$$\begin{bmatrix} \textcircled{X} & 0 & X & 0 & 0 & 0 & X \\ 0 & X & 0 & & & & \\ X & 0 & & & & & \\ 0 & & & & & & \\ 0 & & & & & & \\ X & & & & & & \end{bmatrix} \begin{bmatrix} X \\ X_1 \\ X_2 \\ X_3 \\ \vdots \\ X_n \end{bmatrix} = \begin{bmatrix} B \end{bmatrix}$$

A

Augmented [Yous]:
Move rows with
zero diagonal to
bottom, (and hope
for a fill before
normalization).

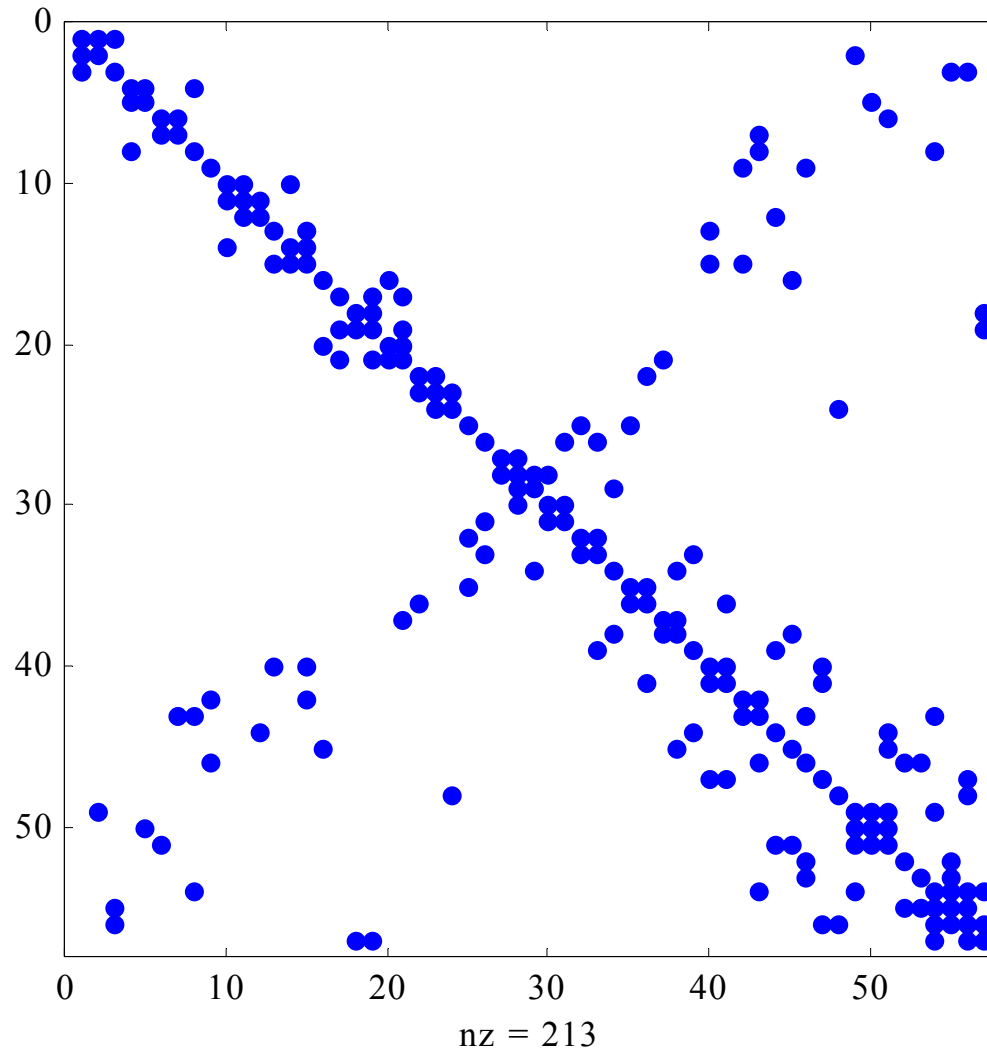
Helpful MatLab Commands

- General
 - save, load
 - who – lists variables
 - clear a, b, ..
 - inv(A) – inverts matrix
 - zeros, ones
 - find
 - **help xxx** to find help on a specific command
 - HTML help desk
- LU, sparse matrices
 - issparse, sparse, full
 - nnz, nonzeros
 - spy – shows topology
 - [L,U] = lu(A)
 - Reordering: **colmd, symmmd, symrcm, colperm, randperm, dmperm**

Use of the spy function

57-Bus
IEEE System

Sparsity:
93.44%



Exercise to Investigate Reordering

```
% COLMMD reordering:
flops(0);          %Reset floating point operations counter
%Reorder and fill new Y and I:
Y1=sparse(nbus,nbus);      %Change to Y1=zeros(nbus,nbus)to give slower full matrix
I1=zeros(nbus,1);
Reord1=colmmd(Y);
for n=1:nbus
    I1(n) = I(Reord1(n));
    for m=1:nbus
        Y1(n,m)=Y(Reord1(n),Reord1(m));
    end
end
end
BV1 = inv(Y1)*I1;

```

We would not in a real case
create duplicate matrices for
the reordering.

Improve this part

```
% Un-Reorder and recover correctly-indexed bus voltages:
BV_1 = zeros(nbus,1);
for n=1:nbus
    BV_1(Reord1(n)) = BV1(n);
end
nflops(1)=flops;
```