

## Exam 2

CM3120

Wednesday 3 March 2021

Name: \_\_\_\_\_

- |           |            |
|-----------|------------|
| 1.        | /20        |
| 2.        | /20        |
| 3.        | /20        |
| 4.        | /20        |
| <u>5.</u> | <u>/20</u> |

### Rules:

- Closed book, closed notes.
- Two-page 8.5" by 11" study sheet allowed, double sided; you may use a calculator; you may not search the internet or receive help from anyone.
- Please text clarification questions to Dr. Morrison 906-487-9703. I will respond if I am able.
- All work submitted for the exam must be your own.
- Do not discuss the contents of the exam with anyone before midnight Wednesday 3 March 2021.
- ***Please copy the following Honors Pledge onto the first page of your exam submission and sign and date your agreement to it.***

Honor's Pledge:

On my honor, I agree to abide by the rules stated on the exam sheet.

Signature \_\_\_\_\_

Date \_\_\_\_\_

### Exam Instructions:

- You may work on the exam for up to two hours and 30 minutes (150 minutes).
- Please be neat. Only neat answers will be granted partial credit. Please use a dark pencil or pen so that your work is readable once scanned.
- Significant figures always count.**
- Please box your final answers.
- Submit your work as a single PDF file; put your name on every page. (Genius Scan is a free app that can create a PDF from photos taken by your phone). If you take photos of your work, insert them into Word or Google Docs and create a PDF.
- Submit your exam study sheet as a separate PDF file; put your name on the first page (at a minimum)

1. (20 points) For the scenario described in the box below, answer the questions that follow. You do not need to solve the scenario; just answer the two questions.

Scenario: If a cube of lead of (volume=  $a^3$ ) at uniform temperature  $T_0$  is dropped into a large, stirred reservoir of oil (material properties known) at bulk temperature  $T_b$ , what is the temperature of the lead cube as a function of time?

- a. What is the formula for the Biot number for this scenario? Identify all quantities in the formula, including whether the quantity is a property of the lead or of the oil.
  - b. The Biot number may be thought of as the ratio of two resistances. In words, what are these two resistances and what is the formula for each?
2. (20 points) The Sieder & Tate equation for Nusselt number  $Nu$  for turbulent flow in pipes is given by

$$Nu_{tm} = \frac{h_{lm}D}{k} = 0.027 Re^{0.8} Pr^{\frac{1}{3}} \left( \frac{\mu_b}{\mu_w} \right)^{0.14}$$

Answer the following two questions (part a and part b):

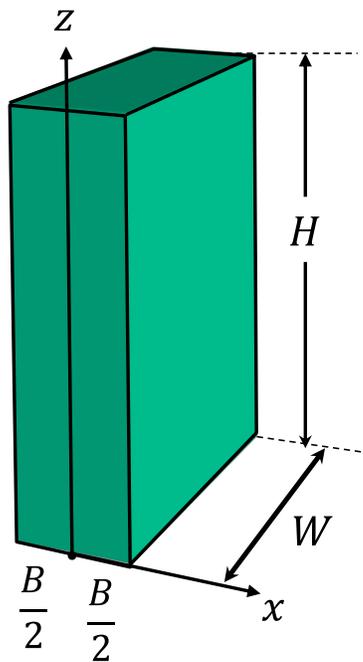
- a. Identify following symbols in this equation and provide SI units for the quantity:

Symbol	Name/formula	SI units
$D$		
$k$		
Re		
Pr		
$\mu_b/\mu_w$		

- b. Describe a situation when you would use this equation.

3. (20 points) What is the partial differential equation that we need to solve in order to determine the temperature as a function of time and position for the situation described in the box below? Indicate the assumptions you used to eliminate terms from the general microscopic energy balance. I am not asking for the boundary or initial conditions; I am only asking for the simplified partial differential equation and the reason for eliminating any terms. Use the coordinate system shown;  $y$  is the direction in the depth direction.

A tall and deep slab (height  $H$ , depth  $W$ , thickness  $B$ ) is initially at uniform temperature  $T_0$ . Suddenly, a fan is switched on creating a convective stream of air on all surfaces at a bulk air temperature of  $T_b$ . What is the temperature distribution as a function of time and position through the thickness direction of the slab?



4. (20 points) A large, thick plate of lead is initially at a uniform temperature of  $300.^{\circ}C$ . One broad surface is suddenly exposed to a liquid coolant at  $20.^{\circ}C$ . The heat transfer coefficient in the coolant in this scenario is  $1.00 \times 10^2 W/m^2K$ . At a distance  $5.5 cm$  into the plate from the surface exposed to coolant, calculate the lead temperature after three minutes.
5. (20 points) A copper sphere (outer diameter  $2.0cm$ ) initially at a uniform temperature of  $32^{\circ}C$  is placed in a precisely constructed spherical oven chamber (chamber inner diameter is  $2.0cm$ ) that instantly and precisely holds the outer surface of the enclosed sphere at  $82^{\circ}C$ . How long does it take for the center of the copper sphere to reach  $81^{\circ}C$ ? Show your supporting calculations.