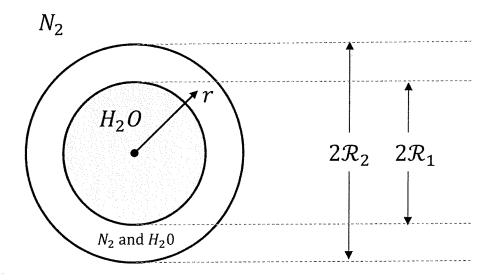


**Example 2**: A water mist forms in an industrial printing operation. Spherical water droplets slowly and steadily evaporate into the air (mostly nitrogen). The evaporation creates a film around the droplets through which the evaporating water diffuses. What is the rate of evaporation and how does the water concentration vary as a function distance from the droplet? You may assume ideal gas properties for air.



Ver 2



## The Equation of Species Mass Balance in Terms of Combined

Molar quantities in Cartesian, cylindrical, and spherical coordinates for binary mixtures of A and B.

The general case, where the combined molar flux with respect to molar velocity  $(\overline{N}_A)$ , is given on page 1

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Microscopic species mass balance, in terms of molar flux; Gibbs notation

$$\frac{\partial c_A}{\partial t} = -\nabla \cdot \underline{N}_A + R_A$$

Microscopic species mass balance, in terms of combined molar flux; Cartesian coordinates

$$\frac{\partial c_A}{\partial t} = -\left(\frac{\partial N_{A,x}}{\partial x} + \frac{\partial N_{A,y}}{\partial y} + \frac{\partial N_{A,z}}{\partial z}\right) + R$$

Microscopic species mass balance, in terms of combined molar flux; cylindrical coordinates

$$\frac{\partial c_A}{\partial t} = -\left(\frac{1}{r}\frac{\partial (rN_{A,r})}{\partial r} + \frac{1}{r}\frac{\partial N_{A,\theta}}{\partial \theta} + \frac{\partial N_{A,z}}{\partial z}\right) + R_A$$

Microscopic specie mass balance, in terms of combined molar flux; spherical coordinates

$$\frac{\partial c_A}{\partial t} = -\left(\frac{1}{r^2}\frac{\partial (r^2 N_{A,r})}{\partial r} + \frac{1}{r\sin\theta}\frac{\partial (N_{A,\theta}\sin\theta)}{\partial \theta} + \frac{1}{r\sin\theta}\frac{\partial N_{A,\phi}}{\partial \phi}\right) +$$

Fick's law of diffusion, Gight hotation:  $\underline{N}_A = x_A(\underline{N}_A + \underline{N}_B) - cD_{AB}\nabla$ 

$$= c_A \underline{\nu}^* - c D_{AB} \nabla x_A$$

Fick's law of diffusion, Cartesian coordinates:

tes: 
$$\begin{pmatrix} N_{A,x} \\ N_{A,y} \\ N_{A,z} \end{pmatrix} = \begin{pmatrix} x_A (N_{A,x} + N_{B,x}) - cD_{AB} \frac{\partial x_A}{\partial x} \\ x_A (N_{A,y} + N_{B,y}) - cD_{AB} \frac{\partial x_A}{\partial y} \\ x_A (N_{A,z} + N_{B,z}) + cD_{AB} \frac{\partial x_A}{\partial z} \end{pmatrix}$$

Fick's law of diffusion, cylindrical coordinates:  $\begin{pmatrix} N_{A,r} \\ N_{A,\theta} \\ N_{A,z} \end{pmatrix}_{r\theta z} =$ 

Fick's law of diffusion, cylindrical coordinates: 
$$\begin{pmatrix} N_{A,\theta} \\ N_{A,z} \end{pmatrix} = \begin{pmatrix} x_A (N_{A,\theta} + N_{B,\theta}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_A (N_{A,z} + N_{B,z}) - cD_{AB} \frac{\partial x_A}{\partial z} \end{pmatrix}_{r\theta z}$$
Fick's law of diffusion, spherical coordinates: 
$$\begin{pmatrix} N_{A,r} \\ N_{A,\theta} \\ N_{A,\theta} \end{pmatrix}_{r\theta \phi} = \begin{pmatrix} x_A (N_{A,r} + N_{B,r}) - cD_{AB} \frac{\partial x_A}{\partial r} \\ x_A (N_{A,\theta} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_A (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{AB}}{r} \frac{\partial x_A}{\partial \theta} \\ x_B (N_{A,\phi} + N_{B,\phi}) - \frac{cD_{$$

 $\chi_A(N_{A,Z}+N_{B,Z})$ 

 $x_A(N_{A,\theta}+N_{B,\theta})$ 

 $x_A(N_{A,r}+N_{B,r})$ 

 $CD_{AB} \frac{\partial x_A}{\partial r}$ 

Microscopic species A mass bul - Stedy - no rxn - 0, \$ symmetry (See p2) 0 = + / dr (12 NAr) d\$ = 0 V2 NAr = T = C

NAT = SI

Fick's Law of Diffusion - Stesment B - Ø, @ Symmtic NAr = XA NAr -C= T=P=const Solve