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Decomposition of product graphs into 4-kites

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Abstract. An n-kite is an n-cycle with a tail consisting of a single edge. In this paper, it is shown that the necessary conditions are sufficient for the existence of 4-kite decompositions of tensor and Cartesian products of complete graphs. Further we extend the existence of such decompositions in regular m-partite graphs.

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