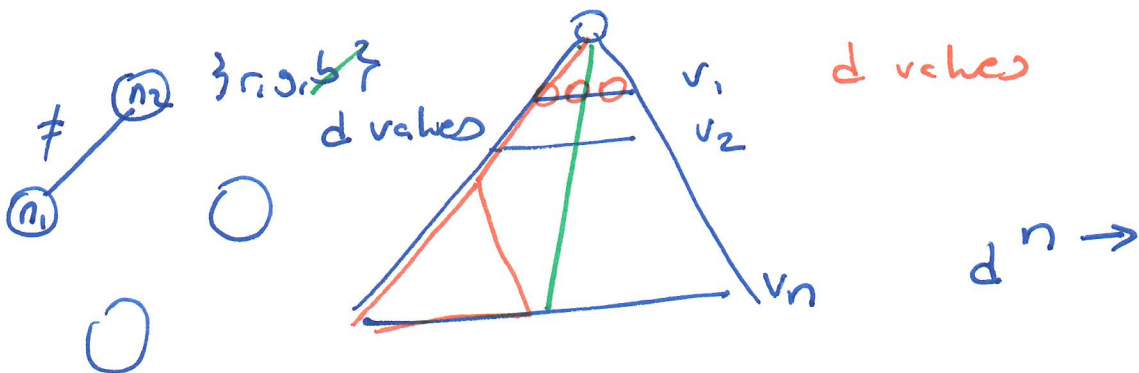
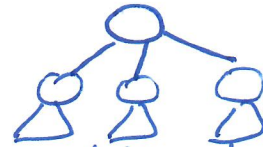


Reminders

- Attendance is required and will be graded
- Please keep the video on during class.
Brief time outs are OK.
- Please keep the microphone muted. You may unmute any time to add a comment or ask a question.
Interrupting me is OK.

Previous classes

- Constraint satisfaction problems (CSPs): search problems defined in terms of variables, domains of variables, and constraints over variables.
- Use backtracking search (recursive implementation of depth-first search)
- Define heuristics to
 - move the path containing the solution to the left
 - detect failures early (prune the path)
- The search tree grows dynamically as before
- The constraints are static, they do not change during the search
- Binary constraints are represented using a constraint graph.



Heuristics

(2)

cost

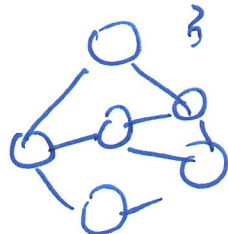
- which variable? choose a variable

most constrained	fewest values possible
most constraining	most constraints to other variables

n

n

d values in each domain
 n variables



remaining values possible

for each variable: n

fewest values
of values

- choose value

rules out the fewest values from other variables

d^2

for each value d

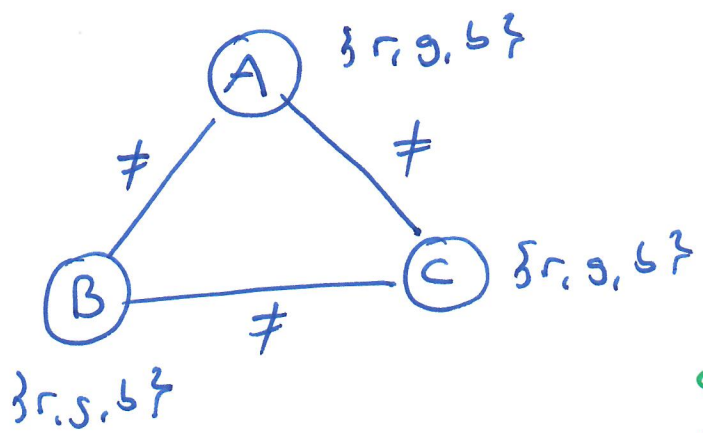
for each value of the other variable d

d^2

- forward checking

keep track of remaining values for the other variables

3



check arcs (directed arcs)

$v_1 \rightarrow v_2$

for each value of v_1 we need to find a value for v_2 legal

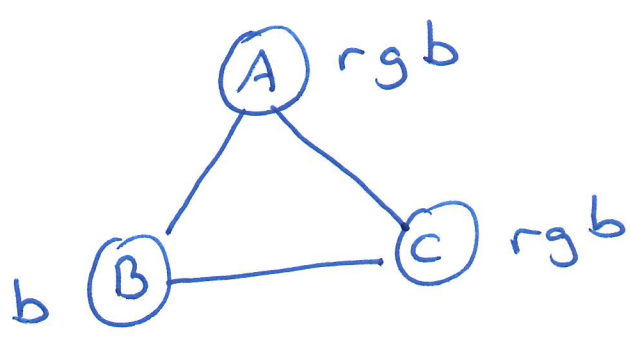
arc is consistent

only A can lose values

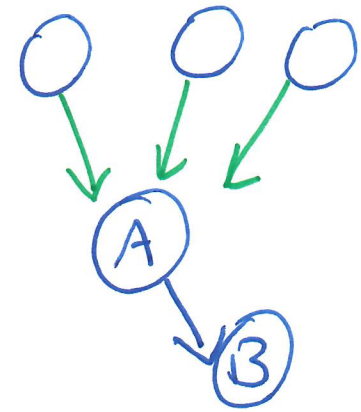
$A \rightarrow B$
 r g b
 r
 g
 b
~~x~~ g b ✓
 r ~~x~~ b ✓
 r g ~~x~~ ✓
 possible values exist

A	B
B	A
A	C
C	A
B	C
C	B

list of arcs to be checked (queue)



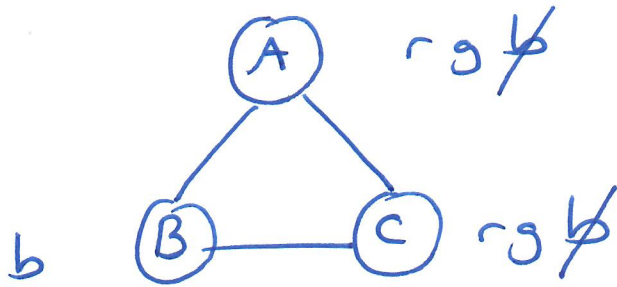
A	B
B	A
A	C
C	A
B	C
C	B



$A \rightarrow B$
 r b ✓
 g b ✓
~~x~~ b X

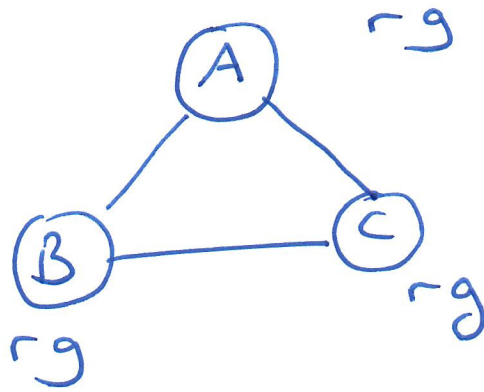
for A
 $\{r, g, b\} \rightarrow \{r, g\}$

re insert all arcs coming into A.



two solutions possible (4)

we need to continue expanding the search tree



is the graph arc consistent?

No $///$
Yes $||$
idk

but the future is not bright.

arc consistent

A	B	
r	g	✓
g	r	✓

$v_x \rightarrow$ ~~rx~~

time complexity

for each arc n^2
check each value of v_x
is there a value in v_y

$v_x \rightarrow v_y$

how many times can each arc be inserted into the queue

n^2
 $d \times$
 $d \times$
 d
 d

$n^2 d^2$

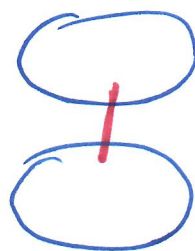
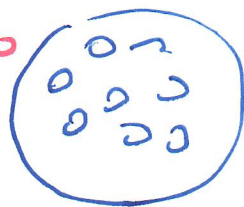
d times

$n^2 d^3$

Problem structure

5

can
separate into
subproblems



$$n = 80 \quad d = 2$$

$$d^n = 2^{80}$$

10 M nodes / second
4 billion years

$$n = 20$$

4

$$2^{20}$$

0.4 seconds

tree structured problems