

Reminder

- Homework 1 due Friday (Oct 2nd)

Previous class

- Interval algebra (IA)

Today

- Point algebra (PA)
- Quantitative Temporal Networks: Temporal CSP (TCSP)
- Simple Temporal Problems (STPs)

Interval Algebra



non-zero
duration

[48, 55] numbers

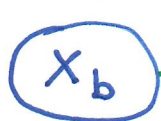
nodes in the
graph

Point Algebra

nodes represent time points in IA



IA



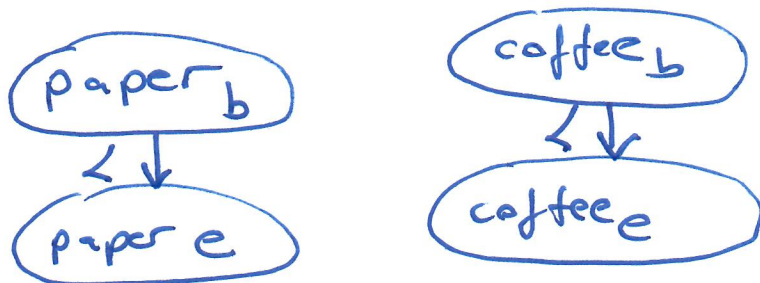
PA

$\langle = \rangle$

time points that
represent event
beginning and
ending points.
(still no numbers)

Fred put down the paper and
drank the last of his coffee.

(2)

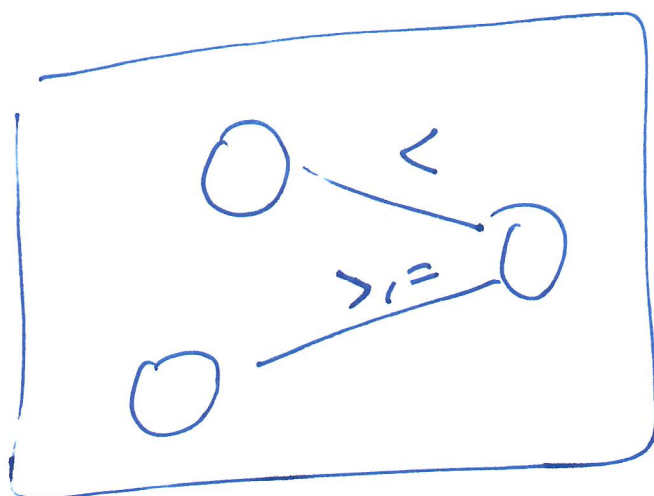


$<, >, =$

$$p_b < c_b$$

$$p_e < c_e$$

$$c_b < p_e$$



entire
set of
constraints
is
AND'ed

I before
or
after J I b, b_i J

Home exercise: Why is this the case?
Why can't we represent
I b, b_i J using PA?
I will ask on Wednesday.

IA / PA
common: qualitative (no numbers)

IA: NP-complete

PA: less expressive

Temporal Constraint Satisfaction Problems
(TCSPs)

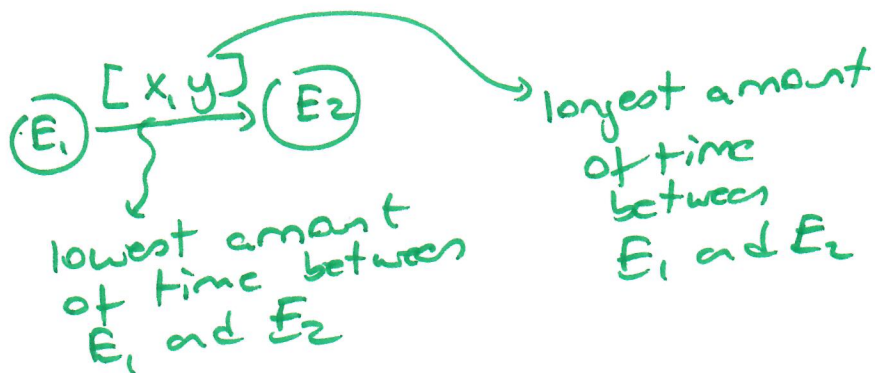
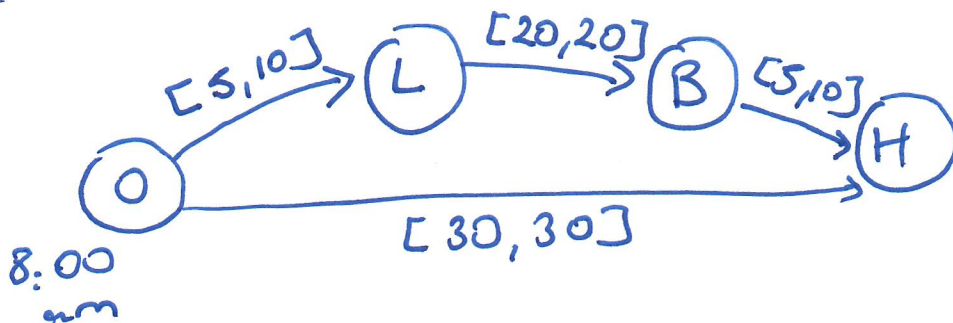
STN: simple temporal networks (special (reduced) case)

Left home: 8:05 - 8:10 L

Drive to the bridge: 20 minutes (exactly)

I waited 5-10 minutes at the bridge (B)

I was in Houghton at 8:30 (H)



$$x_1 \xrightarrow{[a,b]} x_2$$

means

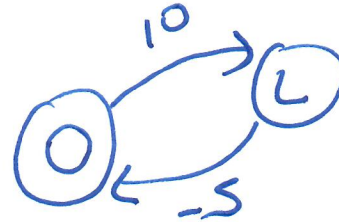
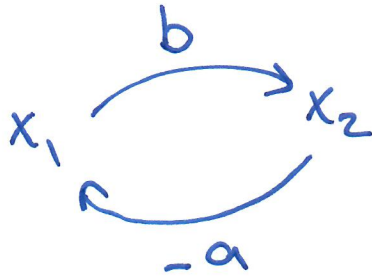
(4)

$$a \leq x_2 - x_1 \leq b$$

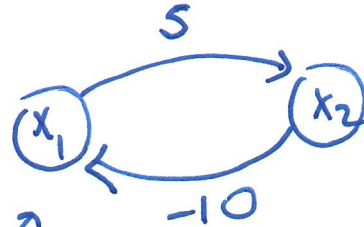
$$a \leq x_2 - x_1$$

$$x_2 - x_1 \leq b$$

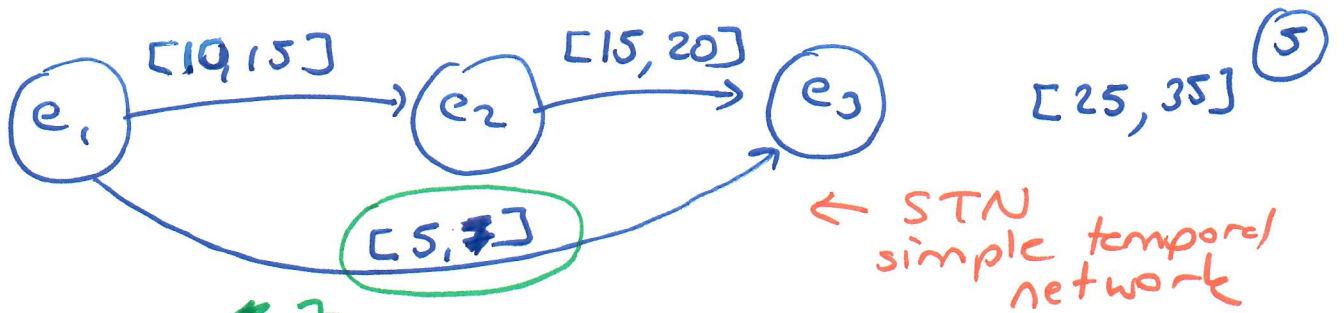
$$-a \geq x_1 - x_2$$



$$x_1 \xrightarrow{[10,5]} x_2$$



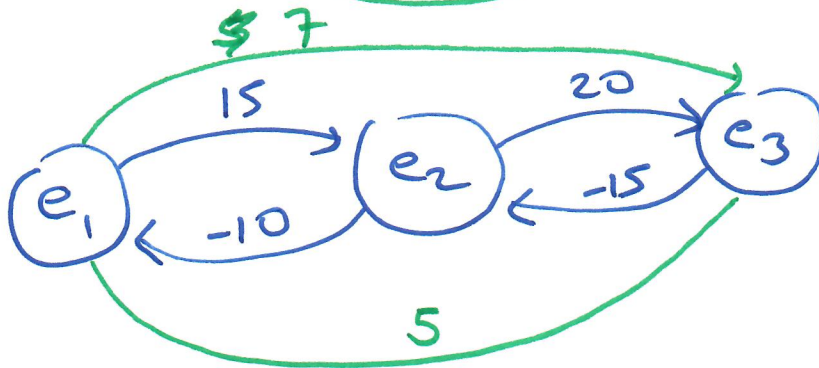
The existence of a negative cycle from x_1 to x_1 shows that this graph is inconsistent.



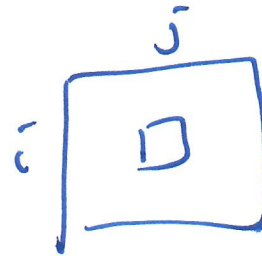
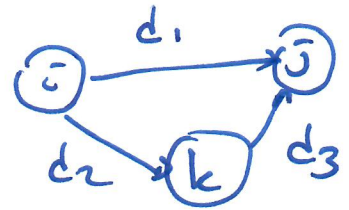
← STN
simple temporal
network

negative
cycle

$$e_1 \ 7 \ e_3 \ -15 \ e_2 \ -10 \ e_1$$



	e_1	e_2	e_3
e_1	0	15	
e_2		0	
e_3			0



$$d_1 \ d_2 + d_3$$

$$n_2 \ n_3 \ n_2$$