

# Introductory R Tutorial 4: Aggregating and Summarizing

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## Aggregating and summarizing: Goals

The goals of this session are to introduce you to a few methods that help you aggregate data across conditions, compute statistics across variables. These are powerful approaches for data management that are difficult or impossible to do in many other stats packages, but are indispensable if you understand them.

This lesson covers a number of different functions that serve different purposes.

## The summarize function

In Lesson 2, we looked at applying the `mean`, `range`, and `sd` to individual data columns of a data frame. This is such a common thing to do that R has a built-in function to do this called `summary`. R's function system is object-oriented, so that there are actually many different `summary` functions (which are technically called *methods*). When called on a data structure, R finds the right version of the function to run. If we have a data frame (or vector or matrix), it calls a method that calculates a number of statistics on each column of data.

We will start by loading a fairly complicated data file that contains the play-by-play records of an NCAA basketball game between Purdue and Michigan.

```
bball <- read.csv("basketball.csv")
head(bball)
```

```
##      game_id      date   home   away play_id half time_remaining_half secs_remaining secs_remaining
## 1 401166238 2020-02-22 Purdue Michigan      1    1           20:00             2400
## 2 401166238 2020-02-22 Purdue Michigan      2    1           20:00             2400
## 3 401166238 2020-02-22 Purdue Michigan      3    1           19:34             2374
## 4 401166238 2020-02-22 Purdue Michigan      4    1           19:34             2374
## 5 401166238 2020-02-22 Purdue Michigan      5    1           19:19             2359
## 6 401166238 2020-02-22 Purdue Michigan      6    1           19:19             2359
##              description home_score away_score score_diff play_length win_prob naive_win_prob home
## 1              PLAY              0          0          0          0 0.6368015          0.5
## 2  Jump Ball won by Purdue              0          0          0          0 0.6368015          0.5
## 3   Matt Haarms Turnover.              0          0          0         26 0.6364613          0.5
## 4   Franz Wagner Steal.              0          0          0          0 0.6364613          0.5
## 5  Jon Teske missed Jumper.              0          0          0         15 0.6362600          0.5
```

```
## 6      Matt Haarms Block.      0      0      0      0 0.6362600      0.5
## away_time_out_remaining home_favored_by shot_x shot_y shot_team shot_outcome shooter assist th
## 1      4      3.5      NA      NA      <NA>      <NA>      <NA>      <NA>
## 2      4      3.5      NA      NA      <NA>      <NA>      <NA>      <NA>
## 3      4      3.5      NA      NA      <NA>      <NA>      <NA>      <NA>
## 4      4      3.5      NA      NA      <NA>      <NA>      <NA>      <NA>
## 5      4      3.5      18 11.48889 Michigan missed Jon Teske <NA>
## 6      4      3.5      NA      NA      <NA>      <NA>      <NA>      <NA>
## possession_before possession_after
## 1      <NA>      Purdue
## 2      Purdue      Purdue
## 3      Purdue      Michigan
## 4      Purdue      Michigan
## 5      Michigan      Michigan
## 6      Michigan      Michigan
```

We can see that this data file is pretty complex. To get a quick snapshot of what is going on in each column, we can use `summary`:

```
summary(bball)
```

```
##      game_id      date      home      away      play_id      half      t
## Min. :401166238 2020-02-22:330 Purdue:330 Michigan:330 Min. : 1.00 Min. :1.000 9
## 1st Qu.:401166238      1st Qu.: 83.25 1st Qu.:1.000 1
## Median :401166238      Median :165.50 Median :2.000 0
## Mean :401166238      Mean :165.70 Mean :1.573 1
## 3rd Qu.:401166238      3rd Qu.:247.75 3rd Qu.:2.000 0
## Max. :401166238      Max. :332.00 Max. :2.000 1
##
## secs_remaining secs_remaining_absolute      description      home_score      a
## Min. : 0 Min. : 0 Evan Boudreaux Defensive Rebound. : 12 Min. : 0.00 Min
## 1st Qu.: 419 1st Qu.: 419 Isaiah Livers made Free Throw. : 8 1st Qu.:11.00 1st
## Median :1011 Median :1011 Official TV Timeout : 7 Median :27.00 Med
## Mean :1069 Mean :1069 Trevion Williams missed Jumper. : 7 Mean :25.93 Mea
## 3rd Qu.:1739 3rd Qu.:1739 Trevion Williams Defensive Rebound.: 6 3rd Qu.:36.00 3rd
## Max. :2400 Max. :2400 Foul on Sasha Stefanovic. : 5 Max. :63.00 Max
##
## (Other) :285
## score_diff play_length win_prob naive_win_prob home_time_out_remaining away
## Min. :-15.000 Min. : 0.000 Min. :0.00000 Min. :0.00000 Min. :3.000 Min.
## 1st Qu.: -13.000 1st Qu.: 0.000 1st Qu.:0.03636 1st Qu.:0.02794 1st Qu.:4.000 1st
## Median :-10.000 Median : 1.000 Median :0.13642 Median :0.09205 Median :4.000 Medi
## Mean : -8.236 Mean : 7.236 Mean :0.26016 Mean :0.20035 Mean :3.924 Mean
## 3rd Qu.: -4.000 3rd Qu.:13.000 3rd Qu.:0.48149 3rd Qu.:0.36628 3rd Qu.:4.000 3rd
## Max. : 4.000 Max. :33.000 Max. :0.72269 Max. :0.60416 Max. :4.000 Max.
##
## home_favored_by shot_x shot_y shot_team shot_outcome shooter
## Min. :3.5 Min. : 1.00 Min. : 2.089 Michigan: 88 made : 74 Trevion Williams: 25
## 1st Qu.:3.5 1st Qu.:24.00 1st Qu.: 6.267 Purdue : 74 missed: 88 Isaiah Livers : 19
## Median :3.5 Median :25.00 Median :28.722 NA's :168 NA's :168 Xavier Simpson : 18
## Mean :3.5 Mean :25.77 Mean :44.181 Franz Wagner : 15
## 3rd Qu.:3.5 3rd Qu.:27.00 3rd Qu.:83.764 Jon Teske : 14
## Max. :3.5 Max. :47.00 Max. :90.867 (Other) : 71
## NA's :168 NA's :168 NA's :168
## assist three_pt free_throw possession_before possession_after
## Xavier Simpson: 6 Mode :logical Mode :logical Michigan:165 Michigan:173
```

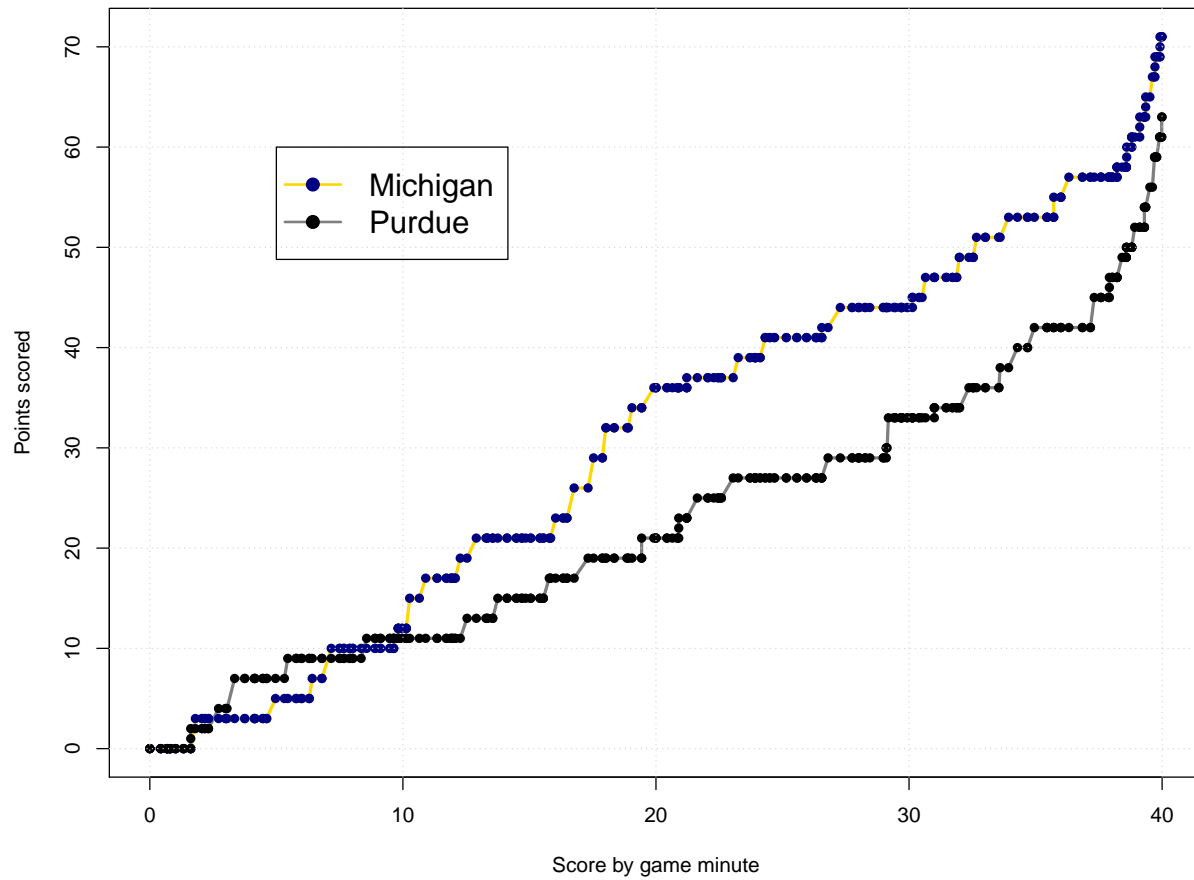
```
## Jon Teske      : 4  FALSE:122      FALSE:127      Purdue   :163      Purdue   :155
## David DeJulius: 3  TRUE :40        TRUE :35        NA's     : 2       NA's     : 2
## Franz Wagner  : 3  NA's :168      NA's :168
## Jahaad Proctor: 2
## (Other)       : 7
## NA's          :305
```

Take a look at the variables, and see what summary does for each one. The data file is very detailed, but makes it difficult to understand anything. Using selection, we can plot home vs. away scores by time in matplot

```
gametime = (2400 - bball$secs_remaining)/60
scores <- data.frame(  MI=bball$away_score,
                      PU=bball$home_score)
matplot(gametime,scores,
        col=c("gold","grey50"),type="l",lwd=2.5,lty=1,
        xlab="Score by game minute",ylab="Points scored",main="Michigan at Purdue, 2-22-2020")
matplot(gametime,scores,
        col=c("navy","black"),type="p",pch=16,add=T)
grid()

##Legend can't handle mixed colors, so we need to plot it twice:
legend(5,60,c("Michigan","Purdue"),pch=NA,lty=1,col=c("gold","grey50"),lwd=2,cex=1.5)
legend(5,60,c("", ""),pch=16,lty=0,lwd=2.5,col=c("navy","black"),bty="n",cex=1.5)
```

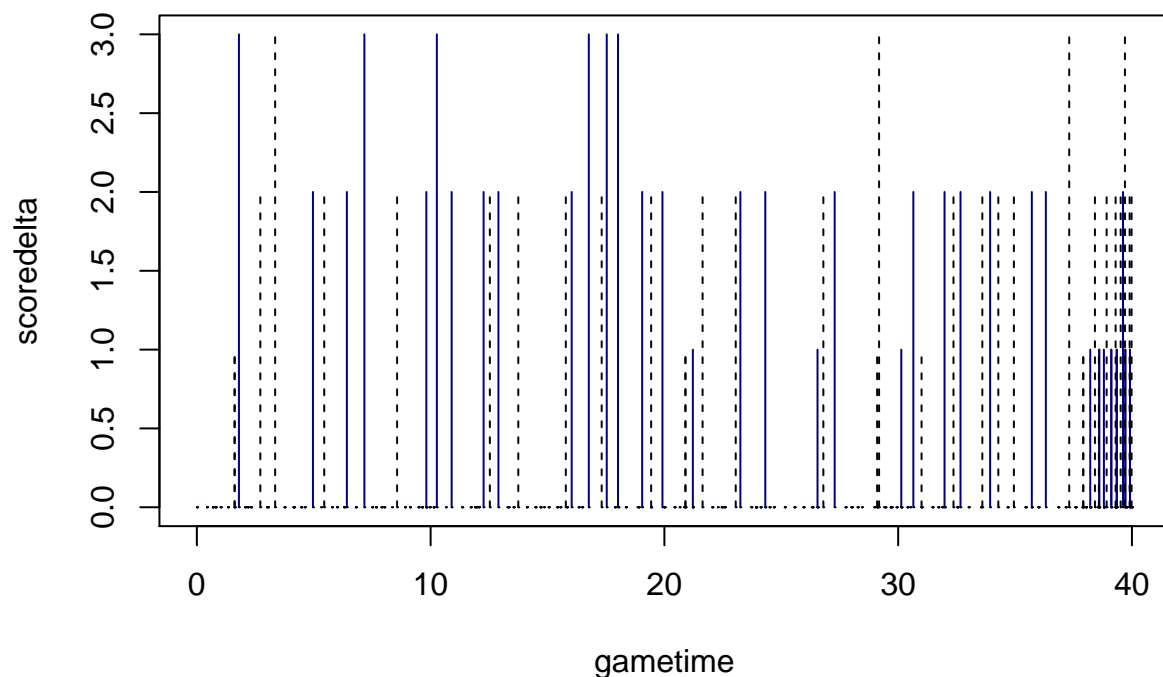
Michigan at Purdue, 2-22-2020



We'd also like to keep track of how many points were scored at each timepoint. Most of the time this will be 0, but sometimes 1, 2, or 3. The original data doesn't have this in it. I'll simply calculate the differential and add it to our new data set. This is sort of like how we computed outliers in the body temp data set.

```
scoredelta <- rbind(c(0,0),
                    scores[-1,] - scores[-nrow(scores),])

matplot(gametime,scoredelta,col=c("navy","black"),type="h")
```



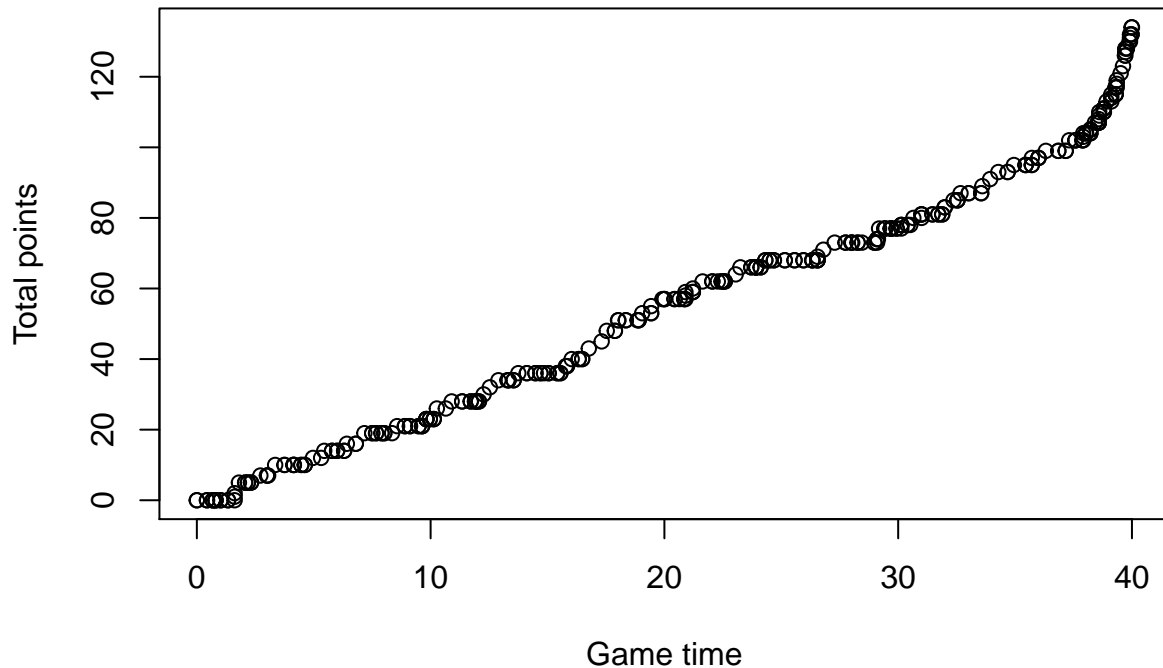
```
newdat <- data.frame(gametime,
                     quarter = floor(gametime/10.001)+1,
                     points=scores,scores=scoredelta)
```

## The rowSums, colSums, and apply

Now that we have some data, let's say we want to know how many total points were scored, or know the total score (MI+PURDUE) at any time point. Or the average score of both teams at each time point. Previously, we did this with something like `scores[1]+scores[2]`, but the `rowSums` and `rowMeans` functions do this easily as well, and will work well if we more than two columns

```
plot(gametime, rowSums(scores),main="Total points (MI + PURDUE)",xlab="Game time",ylab="Total points")
```

## Total points (MI + PURDUE)



Maybe we want to know the number of points scored during the game by each team. We can use `colSums`

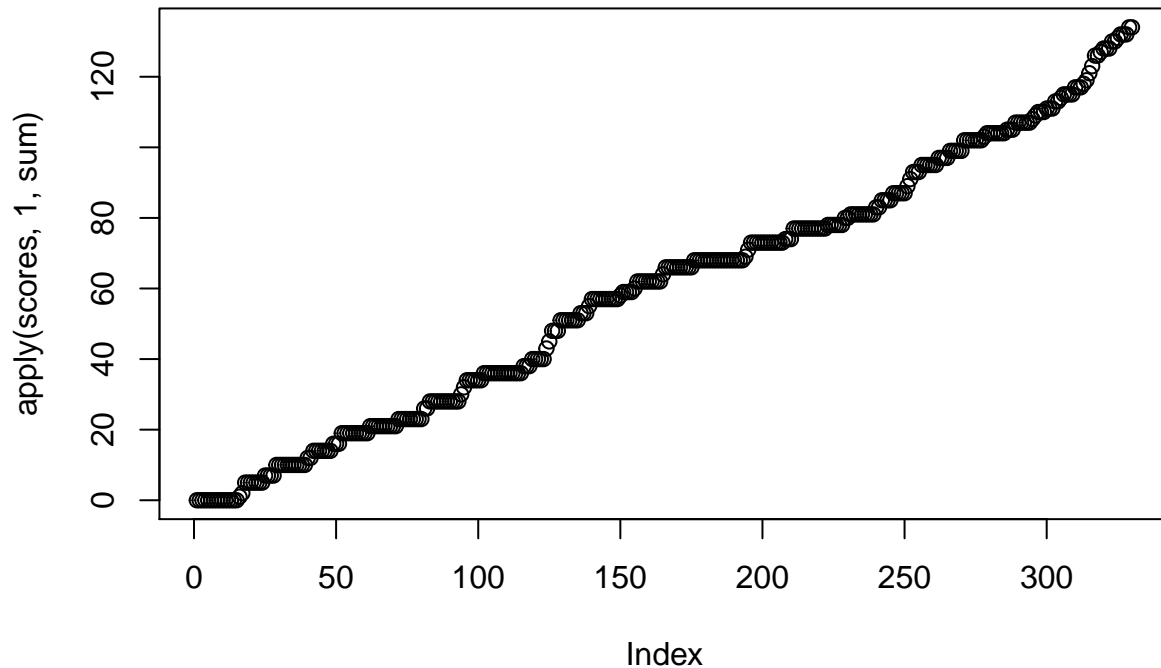
```
colSums(scoredelta)
```

```
## MI PU  
## 71 63
```

These are special-purpose functions that apply the function (mean or sum) along all the rows or columns of a matrix or data frame. What if we want to apply a different function, like standard deviation (`sd`)? We can do the same thing with “`apply`”, which takes the data frame/matrix, the dimension we want to apply to (1=row, 2=column), and the name of the function

```
plot(apply(scores,1,sum),main="Using apply to calculate the sum of two columns")
```

## Using apply to calculate the sum of two columns



```
##The sum of two rows:  
apply(scoredelta,2,sum)
```

```
## MI PU  
## 71 63
```

```
apply(scoredelta,2,sd)
```

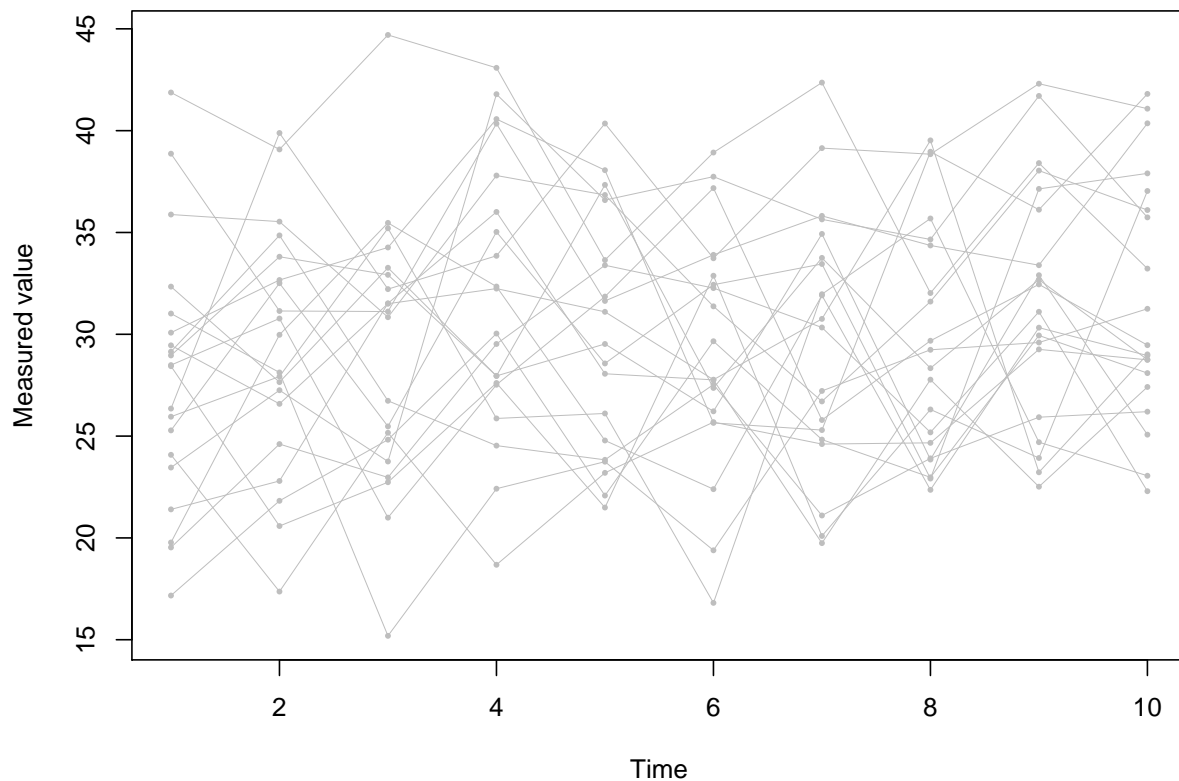
```
## MI PU  
## 0.6279320 0.5962719
```

The last one shows the standard deviation of the points earned on each possession change. We'd probably want to filter out to calculate this just for each team's own possessions, but that

### Exercise 1:

For the following matrix of numbers might be a series of 10 observations made over time of 20 independent participants. We can plot the entire noisy data using `matplot`. Find the mean, max, and min values of each row, put them together in a data frame and plot them using `matplot`. Use the `add=T` argument to overplot these onto the original data.

```
set.seed(10)  
dat <- outer(10+c(1,1.5,1.6,1.9,2.0, 1.2,1.4,1.8,2.1,2.2), 2+runif(20)*1.5) + rnorm(200)*5  
  
matplot(dat,pch=16,cex=.5,col="grey",type="o",lty=1,lwd=.3,  
        xlab="Time",ylab="Measured value")
```



## Computing tabulations and cross-tabulations with table

If we have a categorical variables, we often just want to know what the levels are, and how many of them are there. We can use `table` for that, which will just create an integer vector with the counts of each category, and label each row with the category name. IF we look at the description variable, there might be a lot of unique descriptions of plays, but are there any repetitions? Let's look. I will use `order()` to pick out only the most common labels.

```
tab <- table(bball$description)
length(tab)
```

```
## [1] 164
```

```
tab[order(-tab)[1:20]]
```

```
##
##      Evan Boudreaux Defensive Rebound.      Isaiah Livers made Free Throw.
##                                12                                8
##      Official TV Timeout      Trevion Williams missed Jumper.
##                                7                                7
##      Trevion Williams Defensive Rebound.      Foul on Sasha Stefanovic.
##                                6                                5
##      Franz Wagner Defensive Rebound.      Isaiah Livers Defensive Rebound.
##                                5                                5
```



```
##                Purdue Defensive Rebound.                Xavier Simpson Defensive Rebound.
##                                5                                5
##  Xavier Simpson missed Three Point Jumper.                Foul on Austin Davis.
##                                5                                4
##                Foul on Eric Hunter Jr..  Isaiah Livers missed Three Point Jumper.
##                                4                                4
##                Jon Teske missed Jumper.                Purdue Timeout
##                                4                                4
##          Sasha Stefanovic Defensive Rebound.                Sasha Stefanovic made Free Throw.
##                                4                                4
##          Trevion Williams missed Layup.                Trevion Williams Offensive Rebound.
##                                4                                4
```

It turns out that there were 164 unique descriptions for 330 plays.

In addition, `table` allows us to calculate cross-tabs: the number of cases that match a pair of IVs. Let's look at `possession_before` and `shot_outcome` variables. It is good to label the row and column to make it easier to interpret:

```
table(team=bball$possession_before,outcome=bball$shot_outcome)
```

```
##                outcome
## team          made missed
##  Michigan     40      48
##  Purdue       34      40
```

Note that this only adds up to 162, even though there are 300+ plays. The rest of the plays did not end in a shot and were coded as NA; `table` ignores these NAs by default. But these are interesting in this case, and we can get them back with the `useNA` argument (check the help).

```
table(team=bball$possession_before,outcome=bball$shot_outcome, useNA="always")
```

```
##                outcome
## team          made missed <NA>
##  Michigan     40      48     77
##  Purdue       34      40     89
##  <NA>         0        0      2
```

This shows how 89 plays ended for Purdue without a shot, compared to 77 for Michigan. The 2 NA/NA values are probably just the first play of each half, which always end with a possession by one of the teams.

## Exercise 2

Use `table` to calculate cross-tabulation of the following variables in `bball`:

- `possession_before` and `possession_after`
- `shot_team` and `free_throw`
- `shot_team` and `three_pt`
- `shooter` and `shot_outcome`

## Finding condition means and summaries with `aggregate` and `tapply`

We often have data organized in columns so that one column is a measure we care about, and other columns are IVs, conditions, or categories we want to organize by. For example, in the basketball data, we can compute a column regarding how many points were scored on any position, which is like a DV. We also have a column showing which team was in possession (`bball$shot_team`). We often want to collect all the data for each level of an IV, and apply some function to that data set. For example, we might want to find the sum of the

points scored by each team. This is what a pivot table in spreadsheet programs permit, but these don't get used very frequently. There are two common approaches to doing this in R: **aggregate** and **tapply**.

## Using aggregate to collapse a data set.

We use aggregate when we want to organize functions of one or more DVs by one or more levels of IVs, and we want the resulting table to retain the IV and DV data frame columns. Here are some examples using aggregate and different functions and IVs to compute different statistics about the game:

First, we will calculate the points scored on each possession, and aggregate finding the sum of the points scored by each team. There are two ways to call aggregate, one using a ~formula. The main difference is the name of the values in the data frame.

```
points <- rowSums(scoredelta)
newdat$points <- points

aggregate(points,list(team=bball$shot_team),sum)
```

```
##      team x
## 1 Michigan 71
## 2  Purdue 63
```

```
aggregate(points~shot_team,data=bball,FUN=sum)
```

```
##  shot_team points
## 1  Michigan      71
## 2   Purdue      63
```

This shows the final score was 71 to 63. But what if we also want to know how many points each player scored?

```
aggregate(points,list(player=bball$shooter,team=bball$shot_team),sum)
```

```
##           player      team x
## 1    Austin Davis Michigan 3
## 2 Brandon Johns Jr. Michigan 2
## 3   David DeJulius Michigan 6
## 4     Eli Brooks Michigan 4
## 5   Franz Wagner Michigan 22
## 6   Isaiah Livers Michigan 19
## 7      Jon Teske Michigan 11
## 8   Xavier Simpson Michigan 4
## 9    Aaron Wheeler  Purdue 0
## 10  Eric Hunter Jr.  Purdue 7
## 11   Evan Boudreaux  Purdue 4
## 12  Isaiah Thompson  Purdue 5
## 13   Jahaad Proctor  Purdue 6
## 14    Matt Haarms    Purdue 4
## 15   Nojel Eastern    Purdue 6
## 16  Sasha Stefanovic  Purdue 13
## 17 Trevion Williams  Purdue 18
```

But we might also want to know how many times a player was credited with the possession. We can determine this by finding the length of the vector specified by each combination of team and player:

```
aggregate(points,list(player=bball$shooter,team=bball$shot_team),length)
```

```
##           player      team x
```

```
## 1      Austin Davis Michigan 5
## 2 Brandon Johns Jr. Michigan 3
## 3      David DeJulius Michigan 7
## 4      Eli Brooks Michigan 7
## 5      Franz Wagner Michigan 15
## 6      Isaiah Livers Michigan 19
## 7      Jon Teske Michigan 14
## 8      Xavier Simpson Michigan 18
## 9      Aaron Wheeler  Purdue 1
## 10 Eric Hunter Jr.  Purdue 10
## 11      Evan Boudreaux  Purdue 5
## 12      Isaiah Thompson  Purdue 5
## 13      Jahaad Proctor  Purdue 6
## 14      Matt Haarms  Purdue 5
## 15      Nojel Eastern  Purdue 8
## 16      Sasha Stefanovic  Purdue 9
## 17      Trevion Williams  Purdue 25
```

Similarly, we could calculate average number of points scored per possession by each player by giving it mean instead of length or sum:

```
aggregate(points,list(player=bball$shooter,team=bball$shot_team),mean)
```

```
##           player      team      x
## 1      Austin Davis Michigan 0.6000000
## 2 Brandon Johns Jr. Michigan 0.6666667
## 3      David DeJulius Michigan 0.8571429
## 4      Eli Brooks Michigan 0.5714286
## 5      Franz Wagner Michigan 1.4666667
## 6      Isaiah Livers Michigan 1.0000000
## 7      Jon Teske Michigan 0.7857143
## 8      Xavier Simpson Michigan 0.2222222
## 9      Aaron Wheeler  Purdue 0.0000000
## 10 Eric Hunter Jr.  Purdue 0.7000000
## 11      Evan Boudreaux  Purdue 0.8000000
## 12      Isaiah Thompson  Purdue 1.0000000
## 13      Jahaad Proctor  Purdue 1.0000000
## 14      Matt Haarms  Purdue 0.8000000
## 15      Nojel Eastern  Purdue 0.7500000
## 16      Sasha Stefanovic  Purdue 1.4444444
## 17      Trevion Williams  Purdue 0.7200000
```

## Using tapply to make an aggregate matrix

Sometimes we want the values aggregated into a table, with levels of one IV along the rows, and another along the columns. This would be nice for making a `matplot`. The `tapply` works a lot like `aggregate`, but organizes the results into a matrix. Here is the same aggregation of points per player.

```
x <- tapply(points,list(player=bball$shooter,team=bball$shot_team),sum)
x
```

```
##           team
## player      Michigan Purdue
## Aaron Wheeler      NA      0
## Austin Davis        3      NA
## Brandon Johns Jr.    2      NA
```

```
## David DeJulius      6    NA
## Eli Brooks          4    NA
## Eric Hunter Jr.    NA     7
## Evan Boudreaux     NA     4
## Franz Wagner       22    NA
## Isaiah Livers       19    NA
## Isaiah Thompson     NA     5
## Jahaad Proctor      NA     6
## Jon Teske          11    NA
## Matt Haarms         NA     4
## Nojel Eastern       NA     6
## Sasha Stefanovic    NA    13
## Trevion Williams    NA    18
## Xavier Simpson      4    NA
```

This would make a lot more sense if the two IVs were not nested like team/player. For example, maybe we want to look at each team or each player and find out how many possessions ended in 0, 1, 2, or 3 points, or how many points were gained in each of those conditions. Using `sum` as the function will show total point earned by each player/team in each scoring category:

```
tapply(points,list(team=bball$shot_team,gain=points),sum)
```

```
##           gain
## team      0  1  2  3
## Michigan 0 15 38 18
## Purdue   0  9 42 12
```

```
tapply(points,list(shooter=bball$shooter,gain=points),sum)
```

```
##           gain
## shooter      0  1  2  3
## Aaron Wheeler 0 NA NA NA
## Austin Davis  0  1  2 NA
## Brandon Johns Jr. 0 NA 2 NA
## David DeJulius 0  1  2  3
## Eli Brooks     0 NA 4 NA
## Eric Hunter Jr. 0  1  6 NA
## Evan Boudreaux 0  2  2 NA
## Franz Wagner   0  1 12  9
## Isaiah Livers  0  8  8  3
## Isaiah Thompson 0 NA 2  3
## Jahaad Proctor 0 NA 6 NA
## Jon Teske      0 NA 8  3
## Matt Haarms    0 NA 4 NA
## Nojel Eastern  0 NA 6 NA
## Sasha Stefanovic 0  4 NA  9
## Trevion Williams 0  2 16 NA
## Xavier Simpson 0  4 NA NA
```

Using `length()` will show the number of possessions in each category

```
tapply(points,list(team=bball$shot_team,gain=points),length)
```

```
##           gain
## team      0  1  2  3
## Michigan 48 15 19  6
## Purdue   40  9 21  4
```

```
tapply(points,list(shooter=bball$shooter,gain=points),length)
```

```
##               gain
## shooter      0  1  2  3
## Aaron Wheeler  1 NA NA NA
## Austin Davis   3  1  1 NA
## Brandon Johns Jr. 2 NA  1 NA
## David DeJulius  4  1  1  1
## Eli Brooks     5 NA  2 NA
## Eric Hunter Jr. 6  1  3 NA
## Evan Boudreaux  2  2  1 NA
## Franz Wagner   5  1  6  3
## Isaiah Livers  6  8  4  1
## Isaiah Thompson 3 NA  1  1
## Jahaad Proctor 3 NA  3 NA
## Jon Teske      9 NA  4  1
## Matt Haarms    3 NA  2 NA
## Nojel Eastern  5 NA  3 NA
## Sasha Stefanovic 2  4 NA  3
## Trevion Williams 15 2  8 NA
## Xavier Simpson 14  4 NA NA
```

We can see that NAs fill the cells that were empty,

### Exercise 3

Although college basketball does not have quarters, we can divide the time into 4 equal 10-minute bins we call quarter, which I did above and saved in `newdat$quarter`. Find the number of points scored by each team in each quarter, using both `tapply` and `aggregate`.

```
aggregate(points,list(
  team=bball$shot_team,
  quarter=newdat$quarter),sum)
```

```
##      team quarter  x
## 1 Michigan      1 12
## 2  Purdue      1 11
## 3 Michigan      2 24
## 4  Purdue      2 10
## 5 Michigan      3  8
## 6  Purdue      3 12
## 7 Michigan      4 27
## 8  Purdue      4 30
```

```
tapply(points,list(
  team=bball$shot_team,
  quarter=newdat$quarter),sum)
```

```
##      quarter
## team      1  2  3  4
## Michigan 12 24  8 27
## Purdue   11 10 12 30
```

## Putting it all together

For a final exercise, let's try to integrate several of these.

- First, look at `play_id`, which identifies the unique row number/possession number.

```
bball$play_id
```

```
##      [1]      1      2      3      4      5      6      7      8      9     10     11     12     13     14     15     16     17     18     19     20     21     22     23     24
## [30]    30    31    32    33    34    35    36    37    38    39    40    41    42    43    44    45    46    47    48    49    50    51    52    53    54
## [59]    59    60    61    62    63    64    65    66    67    68    69    70    71    72    73    74    75    76    77    78    79    80    81    82    83
## [88]    88    89    90    91    92    93    94    95    96    97    98    99   100   101   102   103   104   105   106   107   108   109   110   111   112
## [117]   117   118   119   120   121   122   123   124   125   126   127   128   129   130   131   132   133   134   135   136   137   138   139   140   141
## [146]   146   147   148   149   150   151   152   153   154   155   156   157   158   159   160   161   162   163   164   165   166   167   168   169   170
## [175]   175   176   177   178   179   180   181   182   183   184   185   186   187   188   189   190   191   192   193   194   195   196   197   198   199
## [204]   204   205   206   207   208   209   210   211   212   213   214   215   216   217   218   219   220   221   222   223   224   225   226   227   228
## [233]   233   234   235   236   237   238   239   240   241   242   243   244   245   246   247   248   249   250   251   252   253   254   255   256   257
## [262]   262   263   264   265   266   267   268   269   270   271   272   273   274   275   276   277   278   279   280   281   282   283   284   285   286
## [291]   291   292   293   294   295   296   297   300   301   302   303   304   305   306   307   308   309   310   311   312   313   314   315   316   317
## [320]   322   323   324   325   326   327   328   329   330   331   332
```

- Next, we will use `tapply` to create a table that has `play_id` along the rows, `player` as a column, and number of points scored in the cells. Use the `I()` function to simply pass through the `play_outcome` variable, as you are summarizing a single value in each row. I will use the default argument `=0` to make any missing data default to 0 instead of NA.

```
playerbyplay <- tapply(points,list(bball$play_id,bball$shooter),I,default=0)
playerbyplay[20:30,]
```

```
##      Aaron Wheeler Austin Davis Brandon Johns Jr. David DeJulius Eli Brooks Eric Hunter Jr. Evan Boudreau
## 20              0              0              0              0              0              0              0
## 21              0              0              0              0              0              0              0
## 22              0              0              0              0              0              0              0
## 23              0              0              0              0              0              0              0
## 24              0              0              0              0              0              0              0
## 25              0              0              0              0              0              0              0
## 26              0              0              0              0              0              0              0
## 27              0              0              0              0              0              0              0
## 28              0              0              0              0              0              0              0
## 29              0              0              0              0              0              0              0
## 30              0              0              0              0              0              0              0
##      Isaiah Livers Isaiah Thompson Jahaad Proctor Jon Teske Matt Haarms Nojel Eastern Sasha Stefanovic
## 20              0              0              0              0              0              0              0
## 21              0              0              0              0              0              0              0
## 22              0              0              0              0              0              0              0
## 23              0              0              0              0              0              0              0
## 24              0              0              0              0              0              0              0
## 25              0              0              2              0              0              0              0
## 26              0              0              0              0              0              0              0
## 27              0              0              0              0              0              0              0
## 28              0              0              0              0              0              0              0
## 29              0              0              0              0              0              0              3
## 30              0              0              0              0              0              0              0
##      Xavier Simpson
## 20              0
## 21              0
## 22              0
```

```
## 23      0
## 24      0
## 25      0
## 26      0
## 27      0
## 28      0
## 29      0
## 30      0
```

- Then, use aggregate to create a data frame with possession number as the first column, and the possession team (stored in possession\_before) as the variable. Use the I() function as the function argument to simply pass through the label.

```
teambyplayer <- table(bball$shooter,bball$possession_before)
(teambyplayer)
```

```
##
##           Michigan Purdue
## Aaron Wheeler      0      1
## Austin Davis       5      0
## Brandon Johns Jr.  3      0
## David DeJulius     7      0
## Eli Brooks        7      0
## Eric Hunter Jr.    0     10
## Evan Boudreaux     0      5
## Franz Wagner      15      0
## Isaiah Livers      19      0
## Isaiah Thompson    0      5
## Jahaad Proctor     0      6
## Jon Teske         14      0
## Matt Haarms        0      5
## Nojel Eastern      0      8
## Sasha Stefanovic   0      9
## Trevion Williams   0     25
## Xavier Simpson     18      0
```

Let's create a vector which tells us which team each player plays for.

```
team.membership <- apply(teambyplayer,1,which.max)
team.membership
```

```
## Aaron Wheeler      Austin Davis Brandon Johns Jr.      David DeJulius      Eli Brooks      Eric Hun
##           2           1           1           1           1
## Evan Boudreaux      Franz Wagner      Isaiah Livers      Isaiah Thompson      Jahaad Proctor      Jon
##           2           1           1           2           2
## Matt Haarms      Nojel Eastern      Sasha Stefanovic      Trevion Williams      Xavier Simpson
##           2           2           2           2           1
```

Next, we can use apply with cumsum to look at cumulative points for each player. This looks like magic, but what we are doing is finding the cumulative sum of values in each column, for each column separately. We can use team.membership to color each series, and put player names based on their final points at the right side.

```
cumulative.pbp <- apply(playerbyplay,2,cumsum)

purdue.cumulative <- cumsum(rowSums(playerbyplay[,team.membership==2]))
michigan.cumulative <- cumsum(rowSums(playerbyplay[,team.membership==1]))
```

```

matplot(gametime,cumulative.pbp,type="l",col=c("blue","black")[team.membership],lty=1,main="Cumulative points",
        xlab="Game time",ylab="Cumulative points",xlim=c(0,50),ylim=c(0,70))
lines(gametime,purdue.cumulative,lwd=3,col="black")
lines(gametime,michigan.cumulative,lwd=3,col="blue")

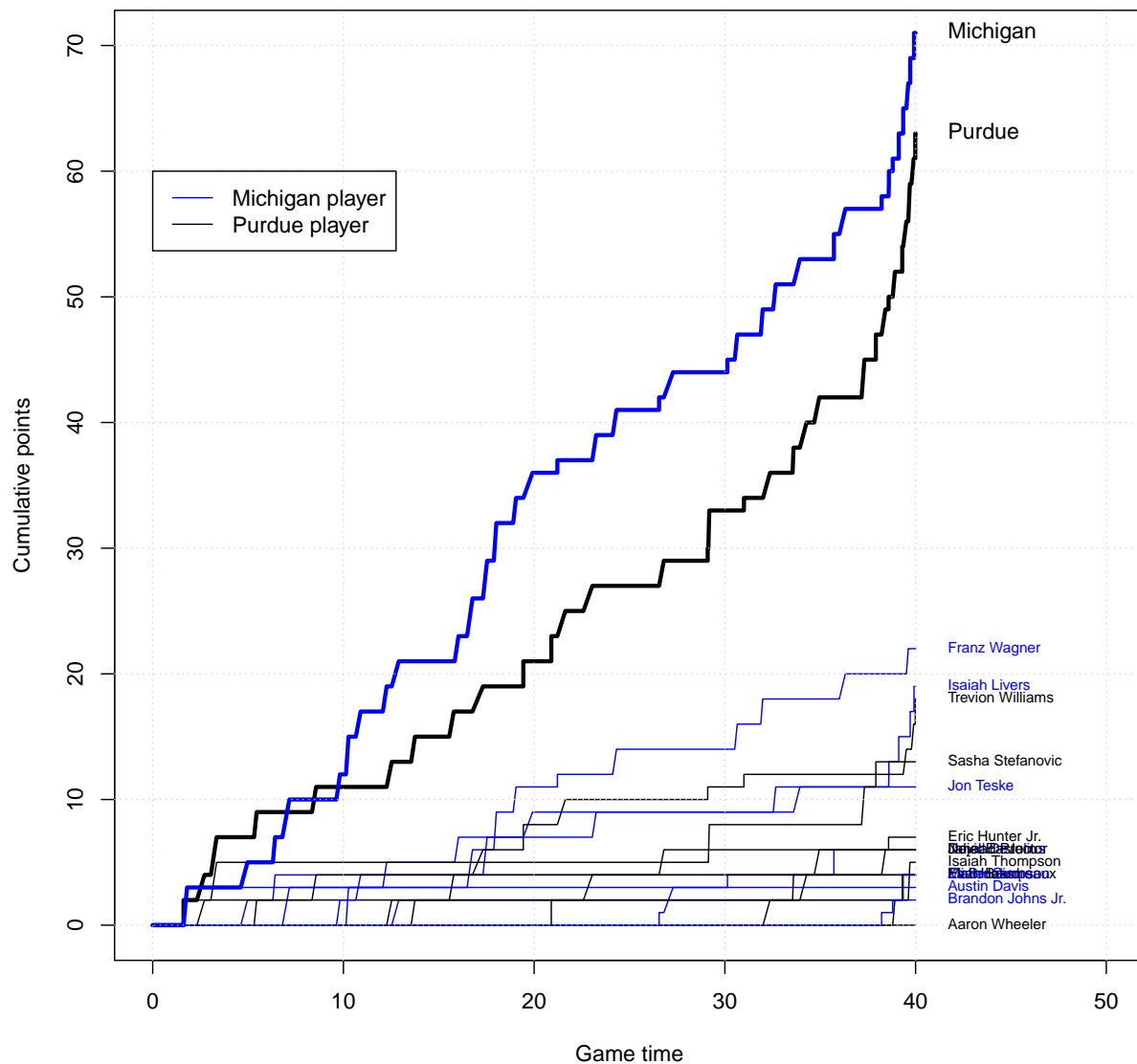
grid()
legend(0,60,c("Michigan player","Purdue player"),col=c('blue','black'),lty=1)

finalpoints <- aggregate(points,list(player=bball$shooter),sum)

text(41,finalpoints$x,finalpoints$player,pos=4,cex=.7,col=c("blue","black")[team.membership])
text(41,max(michigan.cumulative),"Michigan",pos=4)
text(41,max(purdue.cumulative),"Purdue",pos=4)

```

**Cumulative points scored by each player**





This isn't perfect because we have player names overlapping, but it shows how we used `apply`, `tapply`, `aggregate`, and `rowSums`, all together to create a comprehensive look at the game.

## Exercise solutions

### Exercise 1

Use `table` to calculate cross-tabulation of:

- `possession_before` and `possession_after`
- `shot_team` and `free_throw`
- `shot_team` and `three_pt`
- `shooter` and `shot_outcome`

For each one, try to explain what the table is telling you.

```
table(before=bball$possession_before,after=bball$possession_after)
```

```
##           after
## before  Michigan Purdue
## Michigan      59    105
## Purdue       113     49
```

```
table(team=bball$shot_team,freethrow=bball$free_throw)
```

```
##           freethrow
## team      FALSE TRUE
## Michigan      65   23
## Purdue        62   12
```

```
table(team=bball$shot_team,three=bball$three_pt)
```

```
##           three
## team      FALSE TRUE
## Michigan      63   25
## Purdue        59   15
```

```
table(player=bball$shooter,outcome=bball$shot_outcome)
```

```
##           outcome
## player      made missed
## Aaron Wheeler      0      1
## Austin Davis       2      3
## Brandon Johns Jr.   1      2
## David DeJulius      3      4
## Eli Brooks         2      5
## Eric Hunter Jr.     4      6
## Evan Boudreaux      3      2
## Franz Wagner       10      5
## Isaiah Livers       13      6
## Isaiah Thompson      2      3
## Jahaad Proctor       3      3
## Jon Teske           5      9
## Matt Haarms         2      3
## Nojel Eastern        3      5
## Sasha Stefanovic     7      2
## Trevion Williams    10     15
## Xavier Simpson       4     14
```

## Exercise 2:

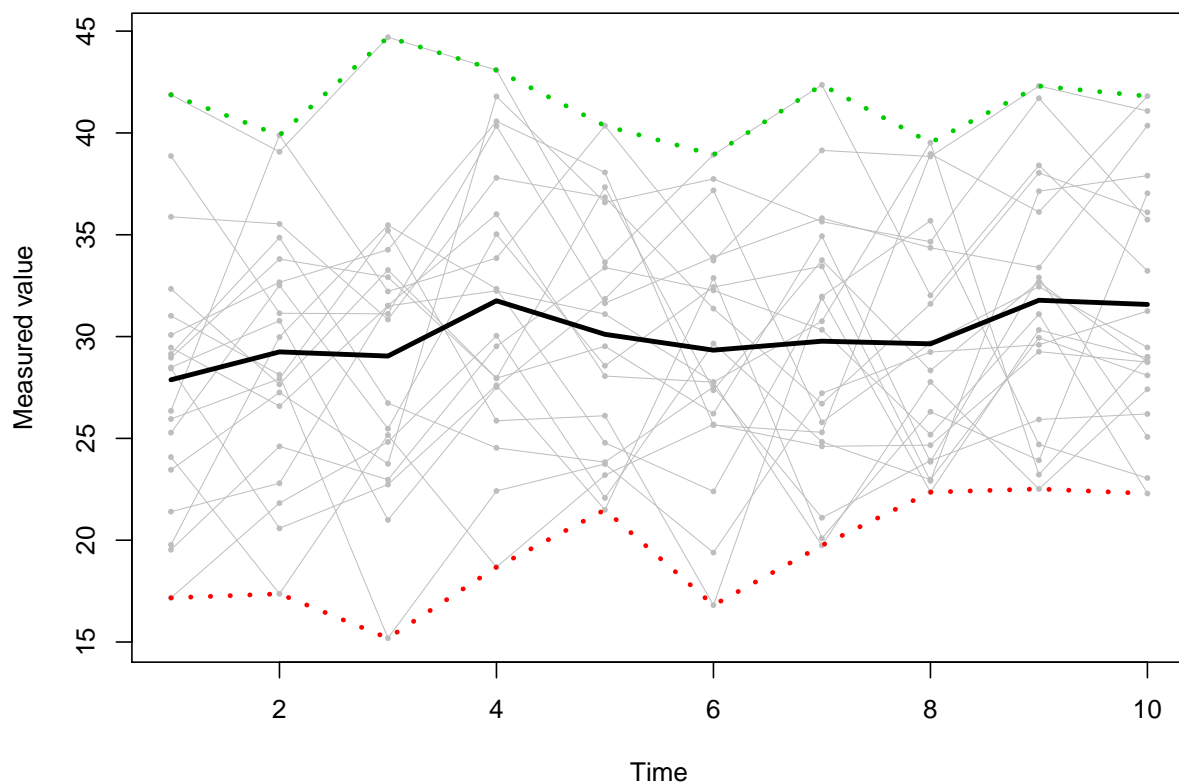
For the following matrix of numbers might be a series of 10 observations made over time of 20 independent participants. We can plot the entire noisy data using `matplot`. Find the mean, max, and min values of each row, put them together in a data frame and plot them using `matplot`. Use the `add=T` argument to overplot these onto the original data.

```
set.seed(10)
dat <- outer(10+c(1,1.5,1.6,1.9,2.0, 1.2,1.4,1.8,2.1,2.2), 2+runif(20)*1.5) + rnorm(200)*5

matplot(dat,pch=16,cex=.5,col="grey",type="o",lty=1,lwd=.3,
        xlab="Time",ylab="Measured value")

summarydat <- data.frame(mean=rowMeans(dat),
                        min=apply(dat,1,min),
                        max=apply(dat,1,max))

matplot(summarydat,add=T,type="l",lwd=3,lty=c(1,3,3))
```



### Exercise 3

Although college basketball does not have quarters, we can divide the time into 4 equal 10-minute bins we call *quarter*, which I did above and saved in `newdat$quarter`. Find the number of points scored by each team in each quarter, using both `tapply` and `aggregate`.

```
tapply(points, list(team=bball$shot_team,
                    quarter=newdat$quarter),length)
```

```
##           quarter
## team           1  2  3  4
##  Michigan 18 17 21 32
##  Purdue   18 16 15 25
```

```
aggregate(points, list(quarter=newdat$quarter,
                       team=bball$shot_team),length)
```

```
##  quarter      team  x
## 1         1 Michigan 18
## 2         2 Michigan 17
## 3         3 Michigan 21
## 4         4 Michigan 32
## 5         1  Purdue 18
## 6         2  Purdue 16
## 7         3  Purdue 15
## 8         4  Purdue 25
```