## Logarithmic Functions Worksheet

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- 1. Solve for x in each of the following equations. Find an exact solution.
  - (a)  $3 \cdot 2^x + 8 = 25$
  - (b)  $5 \cdot 2^x = 4 \cdot e^{3x}$
  - (c)  $ab^x = c$
  - (d)  $ax^b = c$
- 2. Let  $p = \log m$  and  $q = \log n$ . Write each of the following in terms of p and q so that logarithms don't appear in your final answer.
  - (a)  $m^4$
  - (b)  $\log(\frac{1}{n})$
  - (c)  $\frac{\log m}{\log n}$
  - (d)  $\log(n^3)$
- 3. A cup of coffee contains 100 mg of caffeine, which leaves the body at a continuous rate of 17% per hour.
  - (a) Write a formula for the amount, A mg, of caffeine in the body t hours after drinking a cup of coffee.
  - (b) Graph the function from part (a). Use the graph to estimate the half-life of caffeine.
  - (c) Use logarithms to find the half-life of caffeine.