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$$y'' - 4y' + 3y = x$$

$$m^2 - 4m + 3 = 0 \quad m = 3 \text{ or } 1$$

~~$$y = c_1 e^{3x} + c_2 e^x$$~~

$$y = c_1 e^{3x} + c_2 e^x$$

$$y_p = Ax + B \quad 0 - 4A + 3(Ax + B) = x + 0$$

$$y_p' = A$$

$$y_p'' = 0$$

$$3A = 1$$

$$-4A + 3B = 0$$

$$A = \frac{1}{3}$$

$$3B = \frac{4}{3} \Rightarrow$$

$$B = \frac{4}{9}$$

$$y = c_1 e^{3x} + c_2 e^x + \left(\frac{1}{3}x + \frac{4}{9} \right)$$